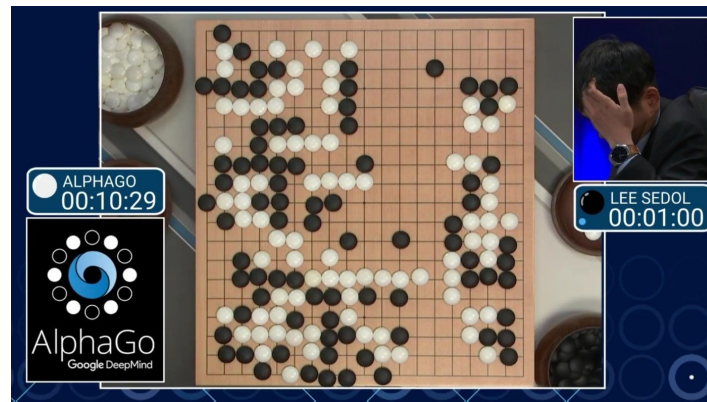
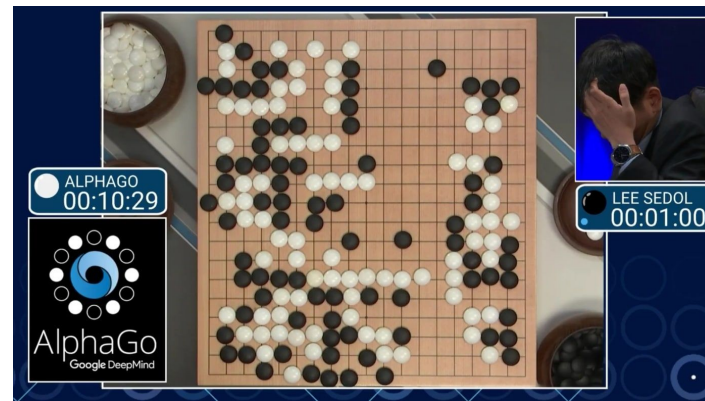


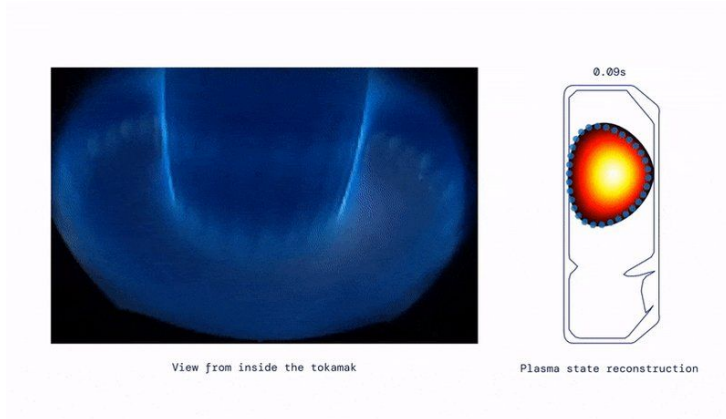
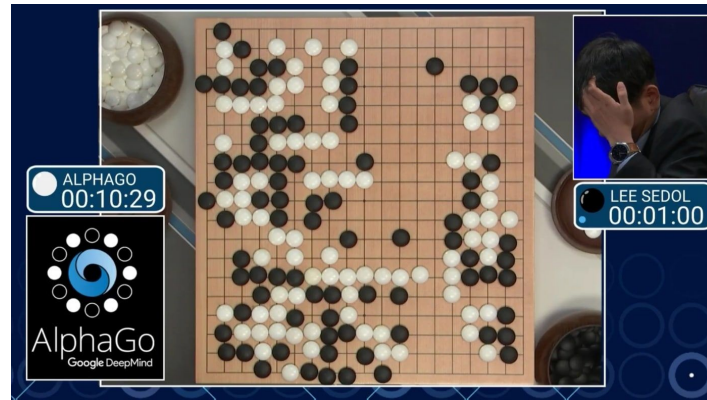
A Brief Introduction To Reinforcement Learning

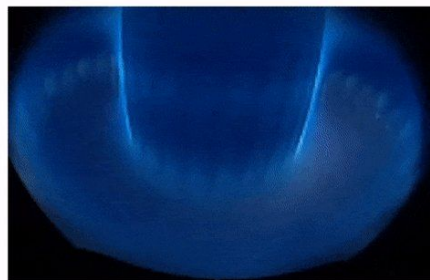
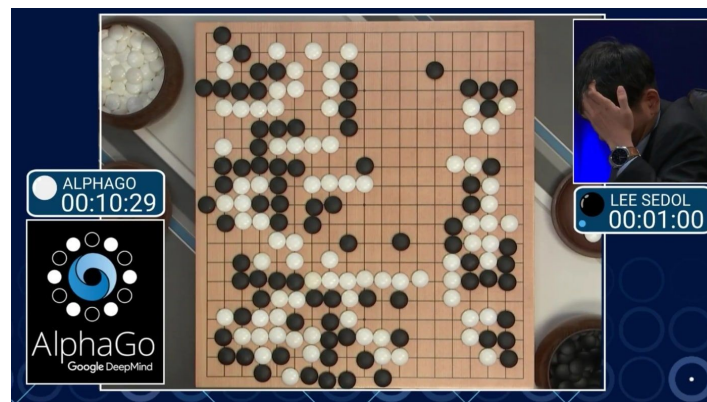


Thomas Moerland

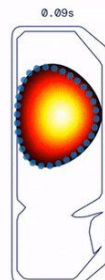






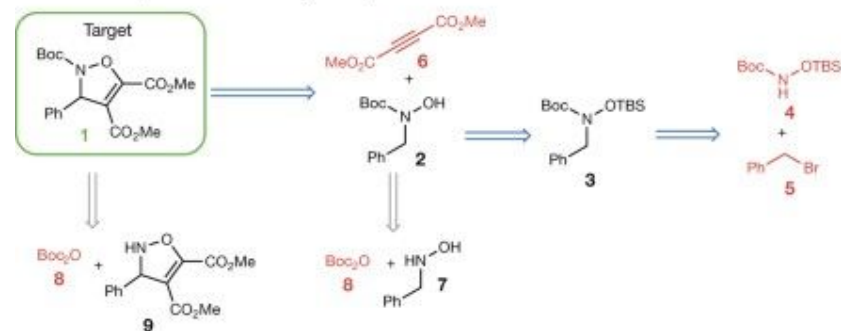


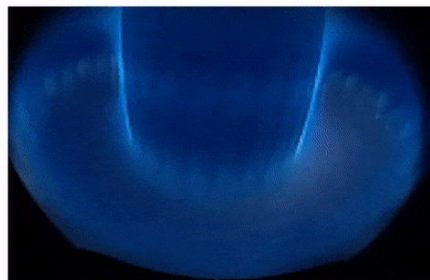
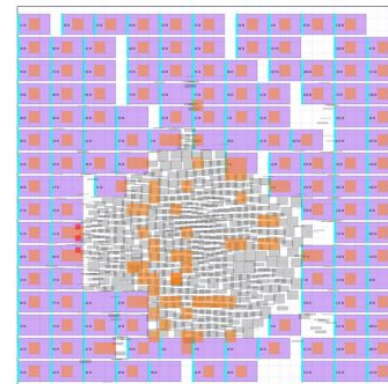
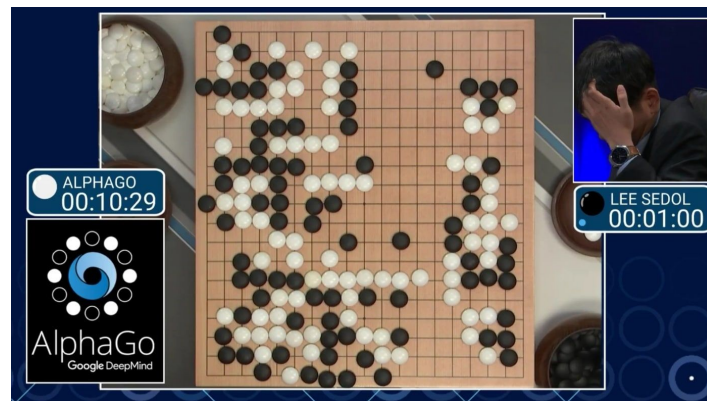
View from inside the tokamak



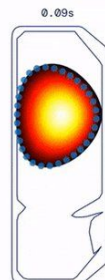
Plasma state reconstruction

a Chemical representation of the synthesis plan



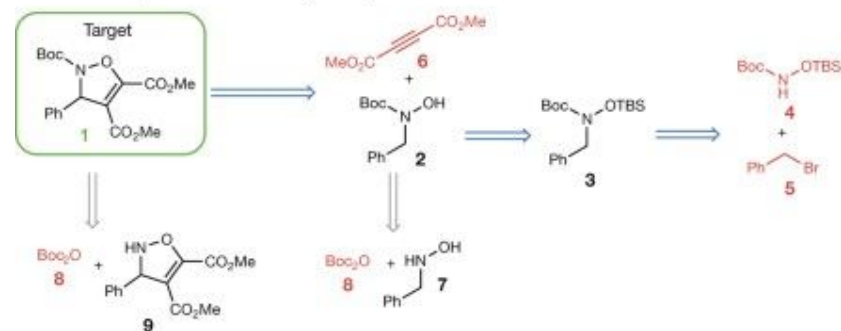


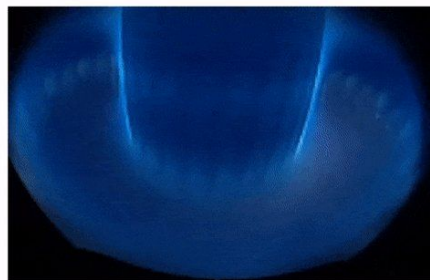
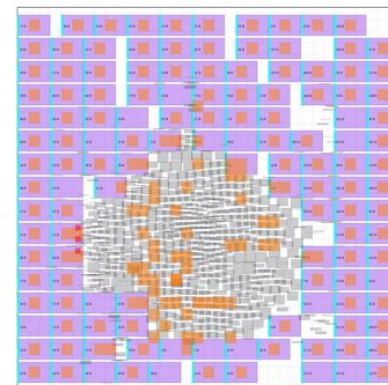
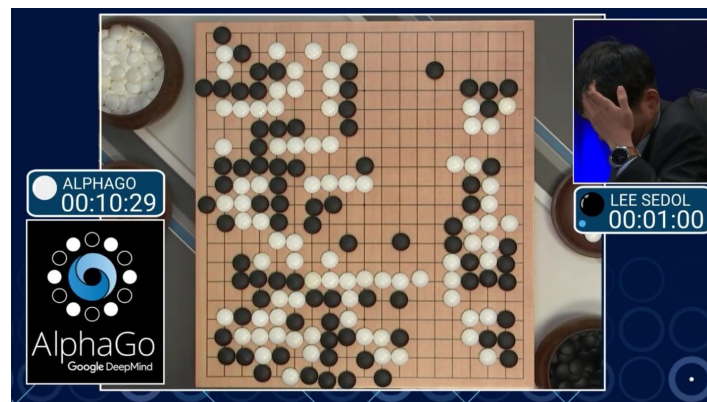
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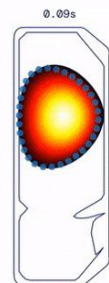
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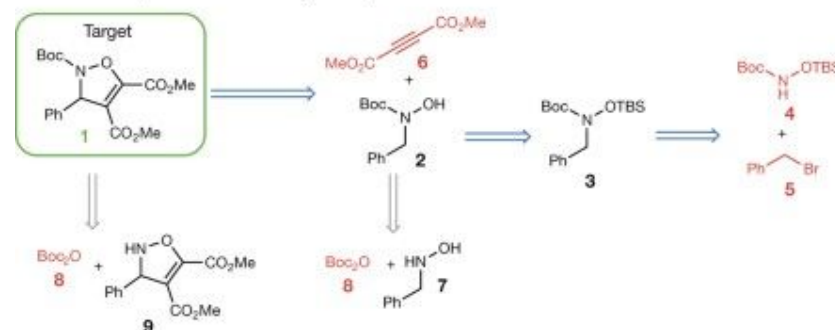


View from inside the tokamak



Plasma state reconstruction

a Chemical representation of the synthesis plan



- Silver, David, et al. "Mastering the game of Go with deep neural networks and tree search." *Nature* 529.7587 (2016): 484-489.
- Fawzi, Alhussein, et al. "Discovering faster matrix multiplication algorithms with reinforcement learning." *Nature* 610.7930 (2022): 47-53.
- Degrave, Jonas, et al. "Magnetic control of tokamak plasmas through deep reinforcement learning." *Nature* 602.7897 (2022): 414-419.
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- Mirhoseini, Azalia, et al. "A graph placement methodology for fast chip design." *Nature* 594.7862 (2021): 207-212.

Many (real-world) problems can be formulated as a

sequential decision-making problem

Many (real-world) problems can be formulated as a

sequential decision-making problem

which may be solved through reinforcement learning.

Content

- I. Introduction
- II. Problem Formulation
- III. Reinforcement Learning Cycle
 - A. Learning Update
 - B. Credit assignment
 - C. Exploration
- IV. Deep Reinforcement Learning

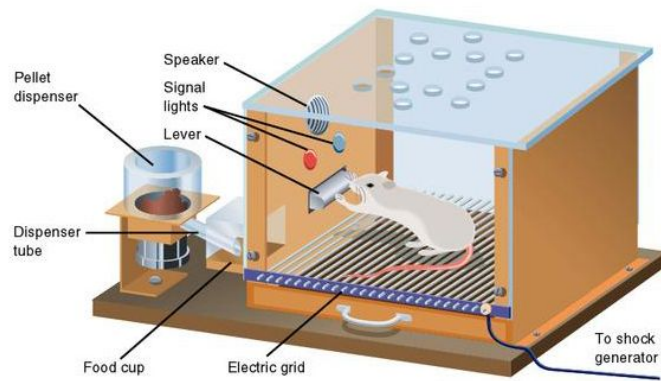
Part I

Introduction

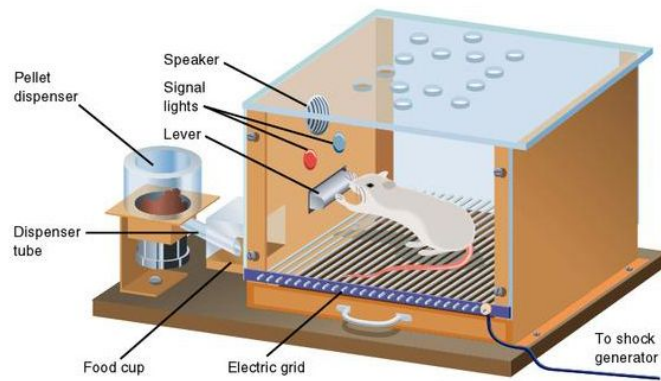
Biology



Biology



Biology

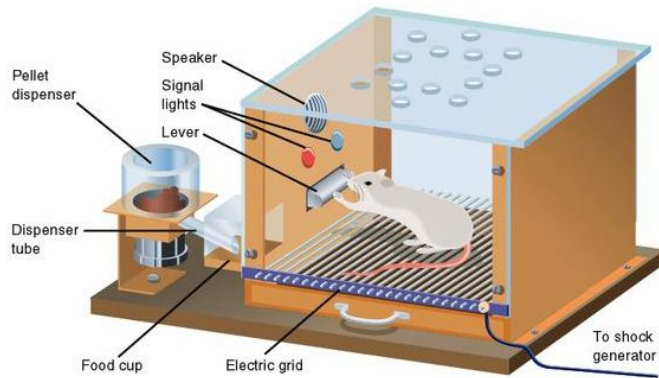


Skinner box



B.F. Skinner (1904 – 1990)

Biology



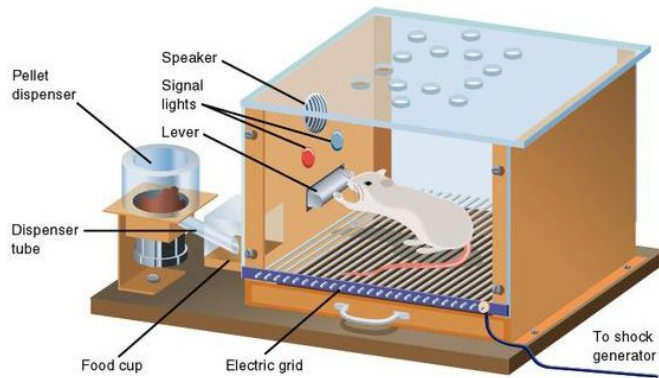
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Instrumental conditioning:
Learning behaviour based on reward and punishment (trial and error)

Biology



Skinner box



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Instrumental conditioning:
Learning behaviour based on reward and punishment (trial and error)

RL is the computational specification of this idea

Supervised versus reinforcement learning



Supervised versus reinforcement learning

Supervised learning

Reinforcement learning

Dataset

Feedback

Supervised versus reinforcement learning

Supervised learning

Reinforcement learning

Dataset

Given

Feedback

Supervised versus reinforcement learning

Supervised learning

Reinforcement learning

Dataset

Given

Active collection

Feedback

Supervised versus reinforcement learning

	Supervised learning	Reinforcement learning
<u>Dataset</u>	Given	Active collection
<u>Feedback</u>	Full (x with correct y)	

Supervised versus reinforcement learning

	Supervised learning	Reinforcement learning
<u>Dataset</u>	Given	Active collection
<u>Feedback</u>	Full (x with correct y)	Partial (state with correct action) (feedback on some outcomes)

Benefits of Reinforcement Learning



Benefits of Reinforcement Learning

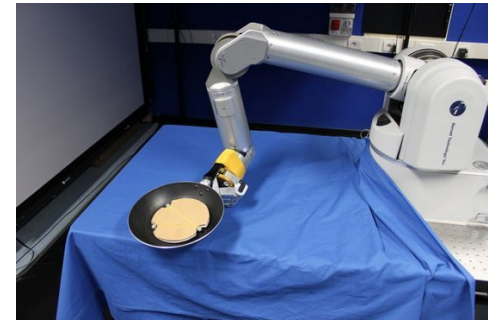


Autonomous behaviour/learning
(only specify goals)

Benefits of Reinforcement Learning



Autonomous behaviour/learning
(only specify goals)



Solve tasks that you can't label
(only need to label the outcome)

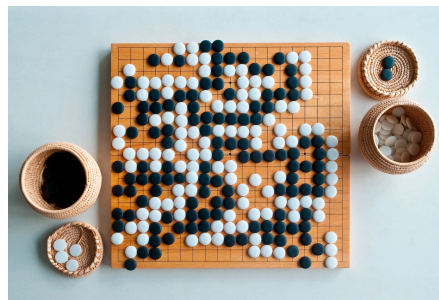
Benefits of Reinforcement Learning



Autonomous behaviour/learning
(only specify goals)



Solve tasks that you can't label
(only need to label the outcome)



Outperform human solution
(only need to label the outcome)

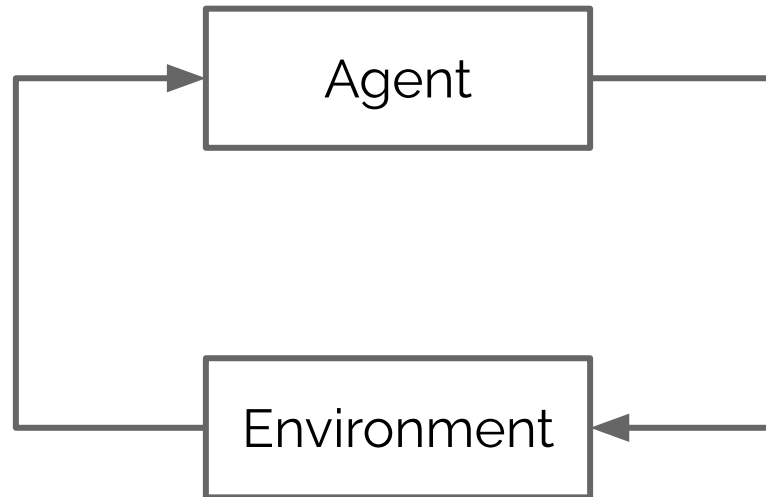
Part II

Problem Formulation

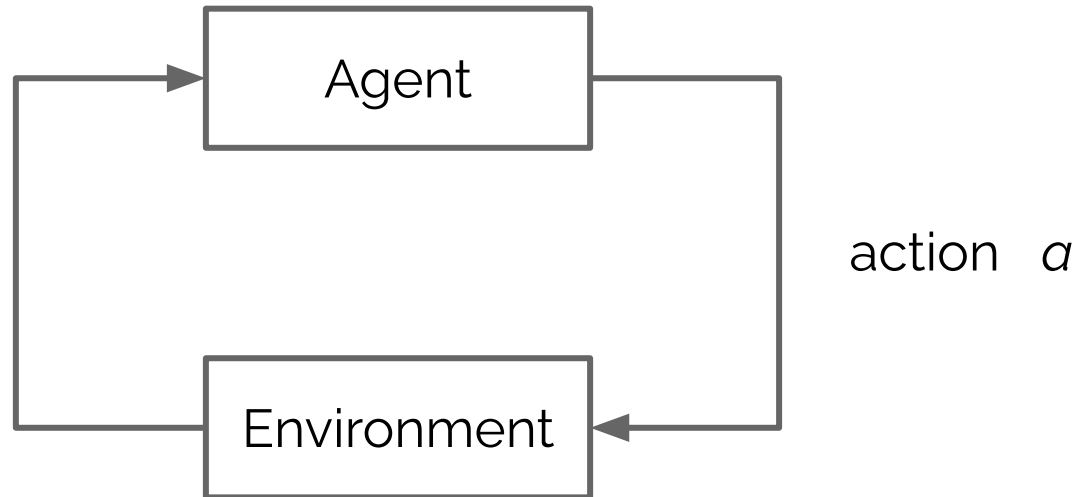
Agent-Environment loop



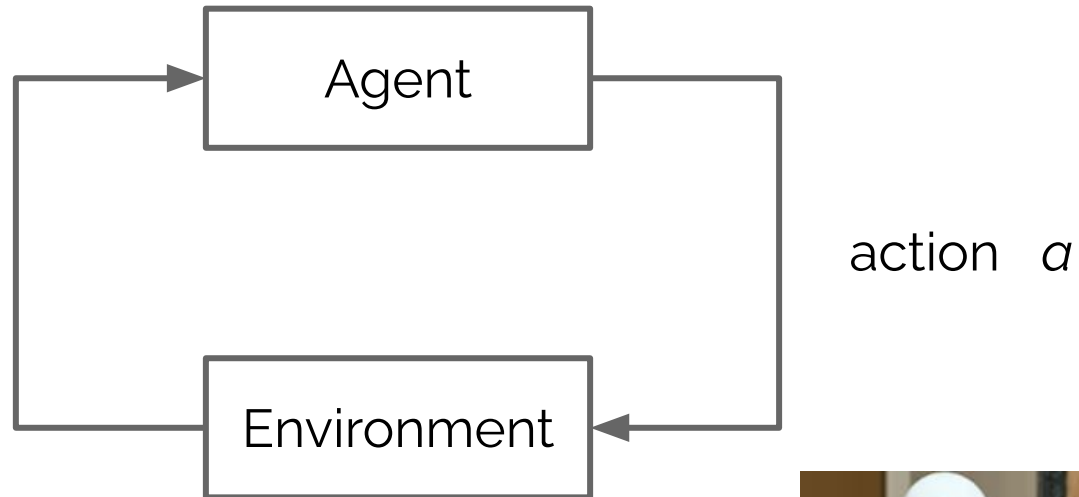
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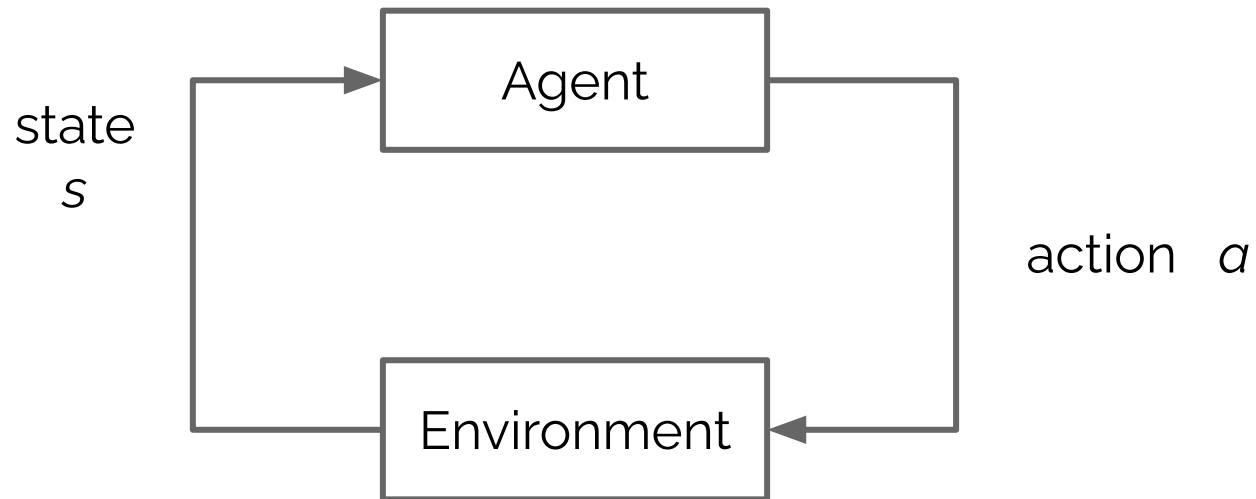
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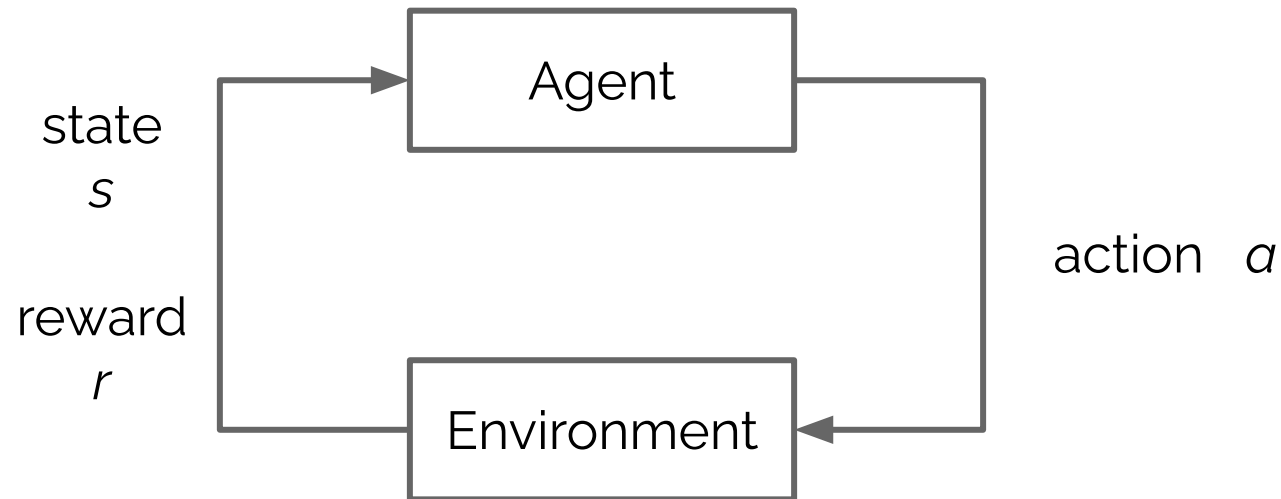
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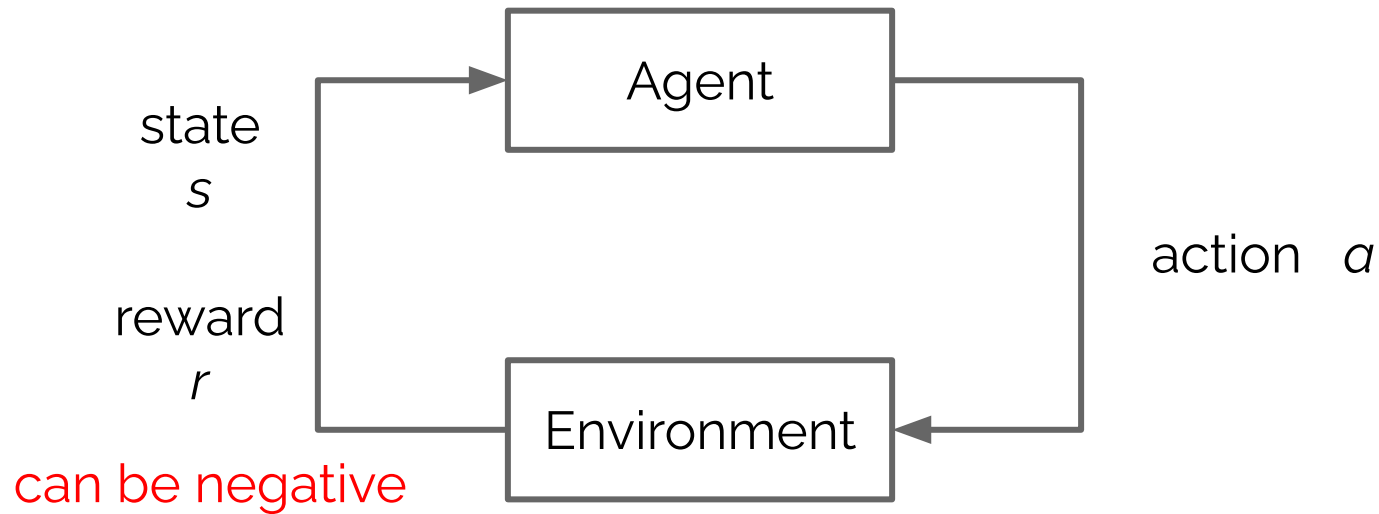
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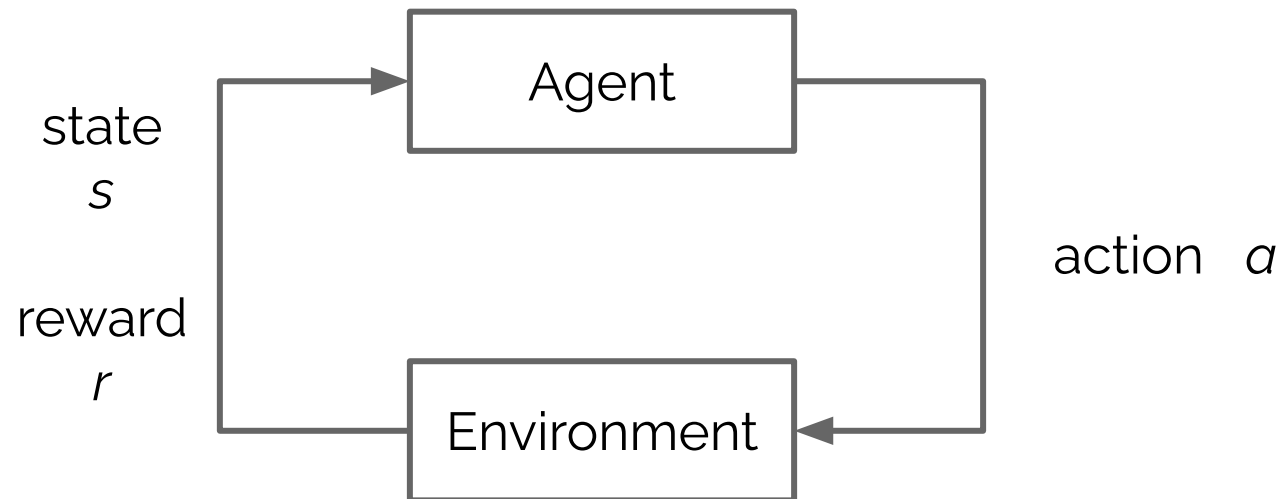
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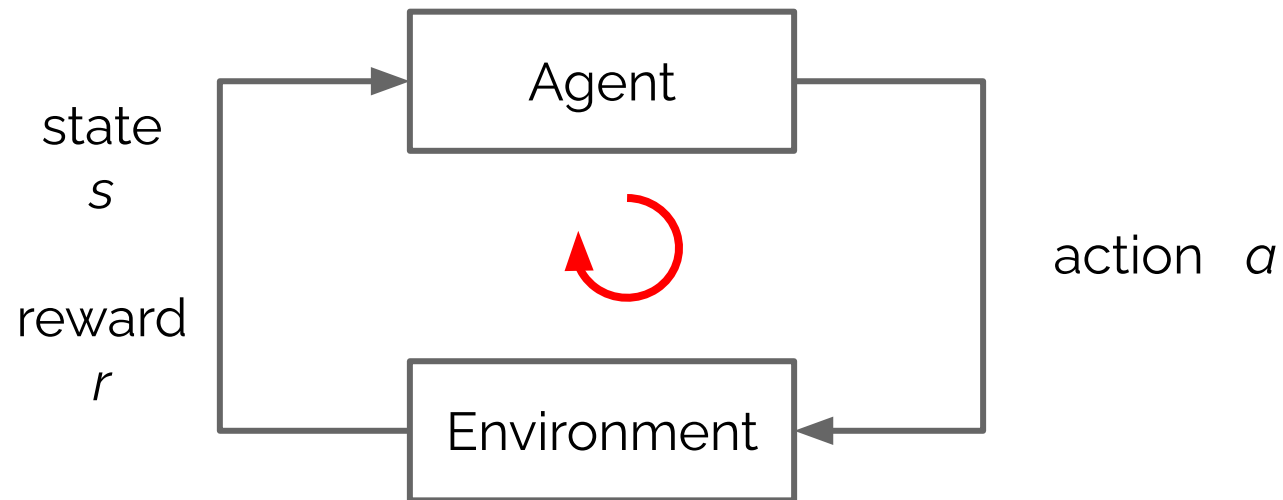
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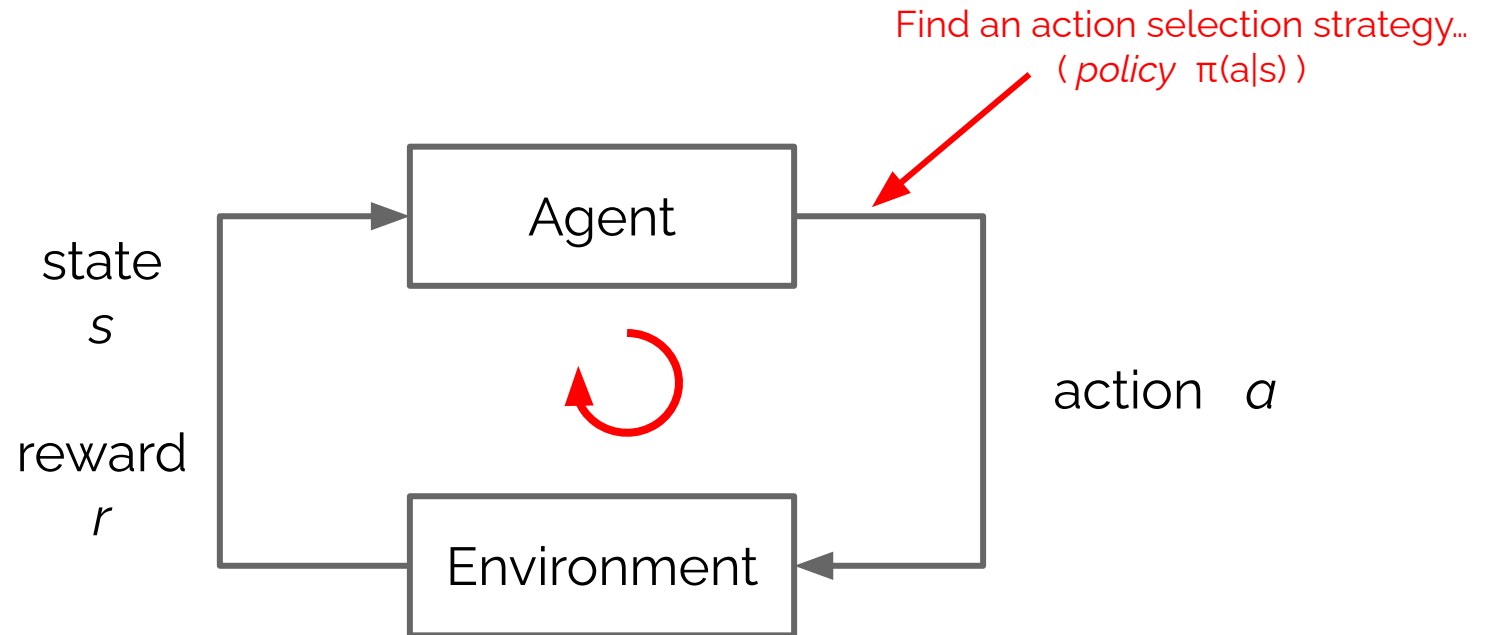
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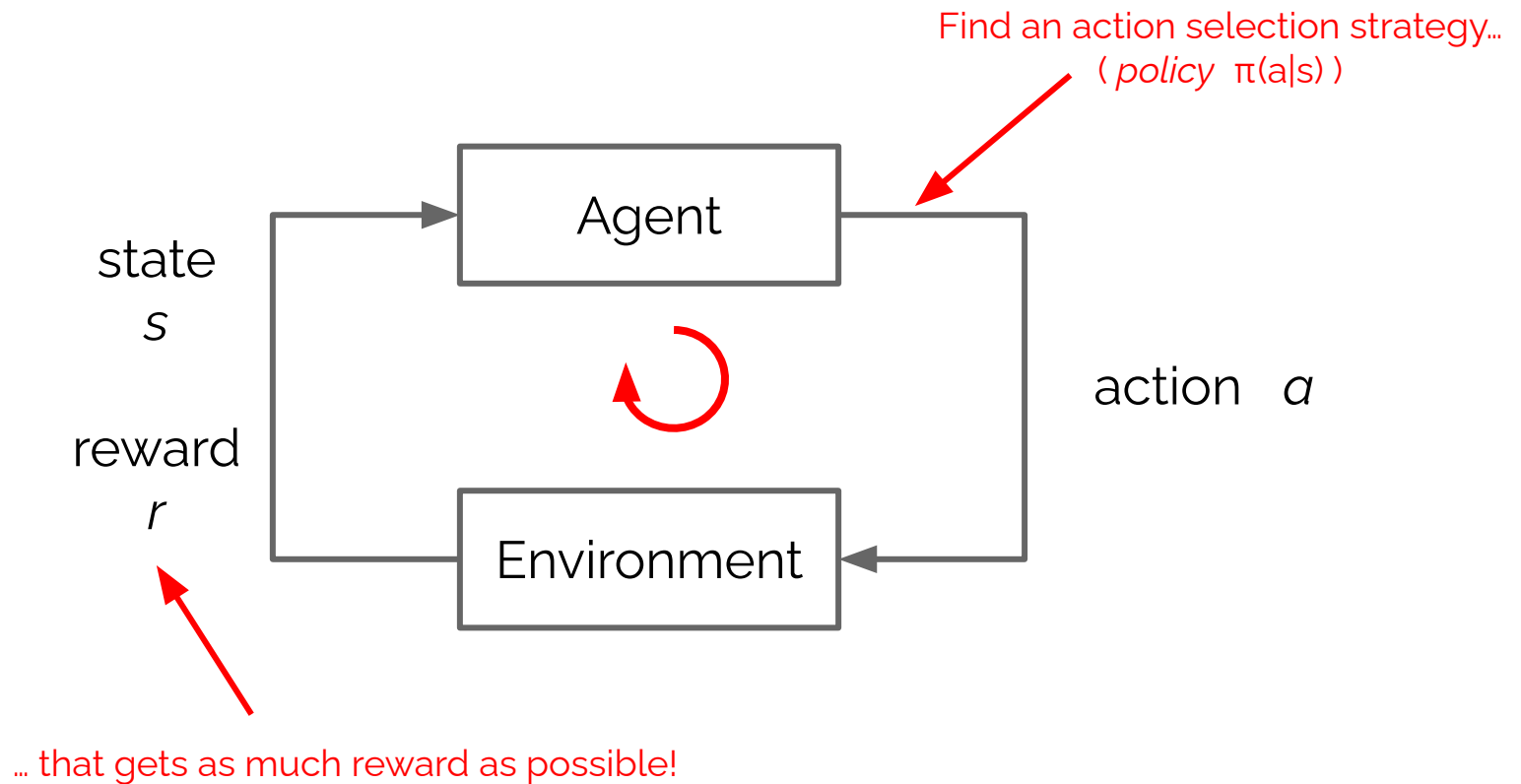
Agent-Environment loop



Agent-Environment loop



Agent-Environment loop



Reward

Reward

Immediate reward

$$r_t$$

Reward

~~Immediate reward~~
Cumulative reward

$$r_t + r_{t+1} + r_{t+2} + \dots$$

Reward

~~Immediate reward~~

~~Cumulative reward~~

Expected cumulative reward

$$\mathbb{E}[r_t + r_{t+1} + r_{t+2} + \dots]$$

Reward

~~Immediate reward~~

~~Cumulative reward~~

Expected cumulative reward

$$\mathbb{E}[r_t + r_{t+1} + r_{t+2} + \dots]$$



Average over stochasticity in 1) environment and 2) own policy.

Reward

~~Immediate reward~~

~~Cumulative reward~~

Expected cumulative reward

= Value

$$Q^{\pi}(s, a) = \mathbb{E}[r_t + r_{t+1} + r_{t+2} + \dots | s_t = s, a_t = a]$$

Reward

~~Immediate reward~~

~~Cumulative reward~~

Expected cumulative reward

= Value

$$Q^{\pi}(s, a) = \mathbb{E}[r_t + r_{t+1} + r_{t+2} + \dots | s_t = s, a_t = a]$$



Q-value: total reward we get on average after taking action a in state s .

Reward

~~Immediate reward~~

~~Cumulative reward~~

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- Depends on our own future behaviour π (if we act stupid, reward will be low)

Reward

~~Immediate reward~~

~~Cumulative reward~~

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Q-value: total reward we get on average after taking action a in state s .
- Depends on our own future behaviour π (if we act stupid, reward will be low)

Can show each state-action has one optimal value, denoted by $Q^*(s,a)$.
- These are the quantities we want to know!

Illustration: Optimal Value



Illustration: Optimal Value

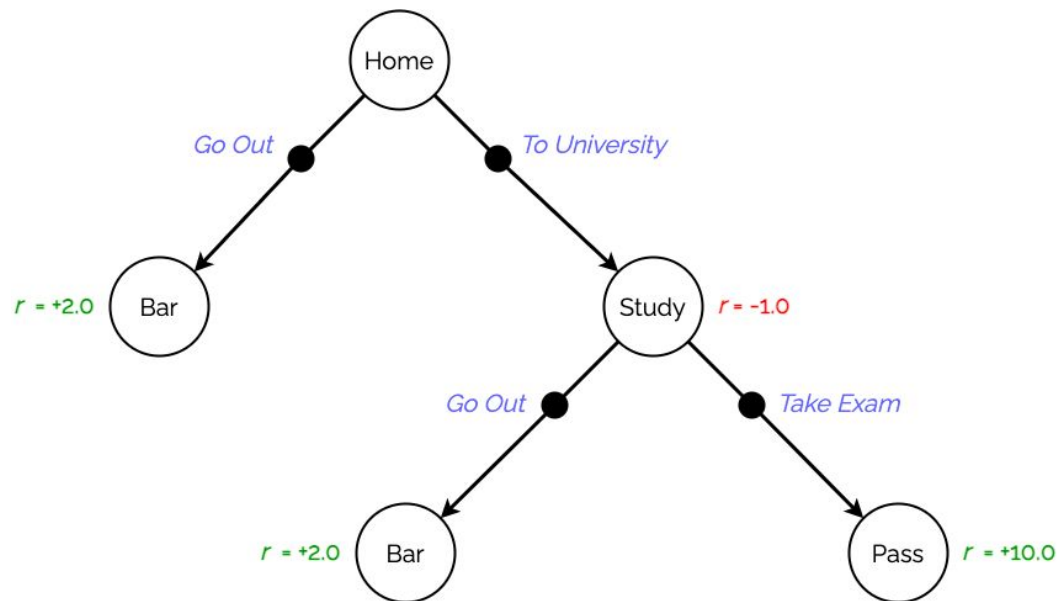
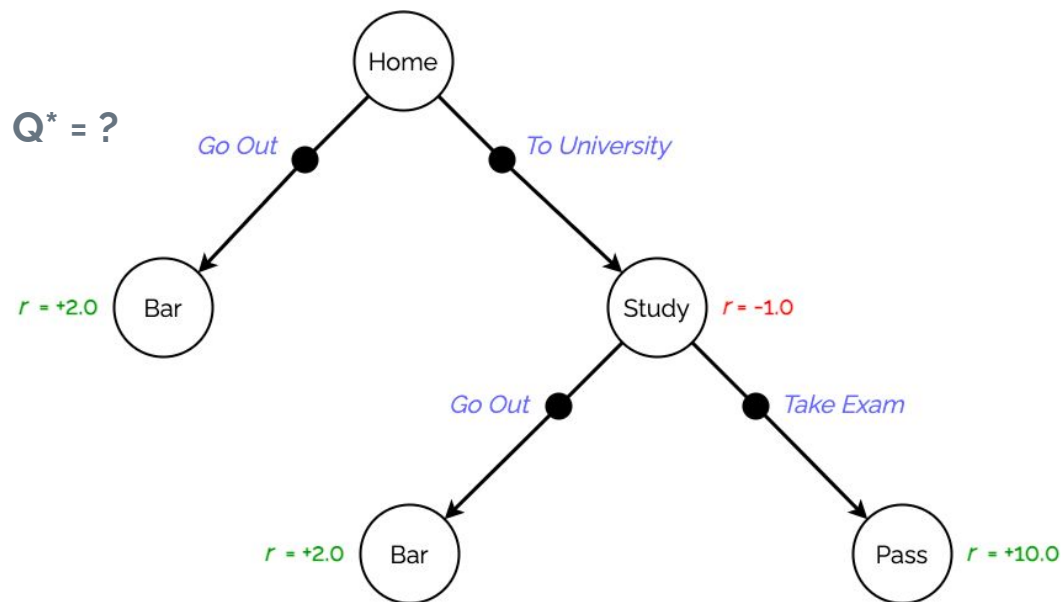
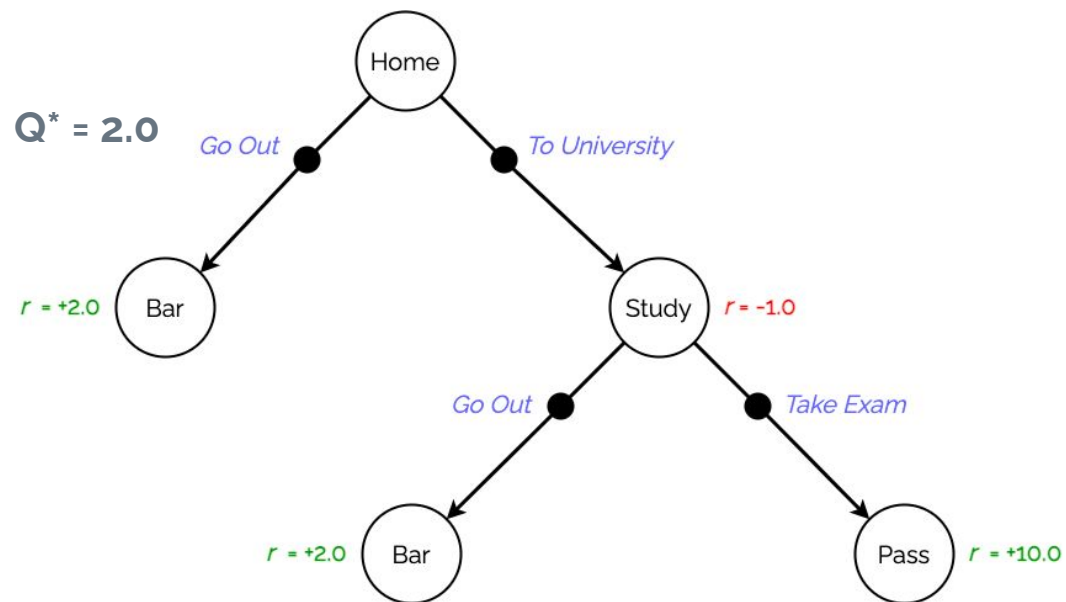


Illustration: Optimal Value



Question: What is $Q^*(\text{Home}, \text{Go Out})$?

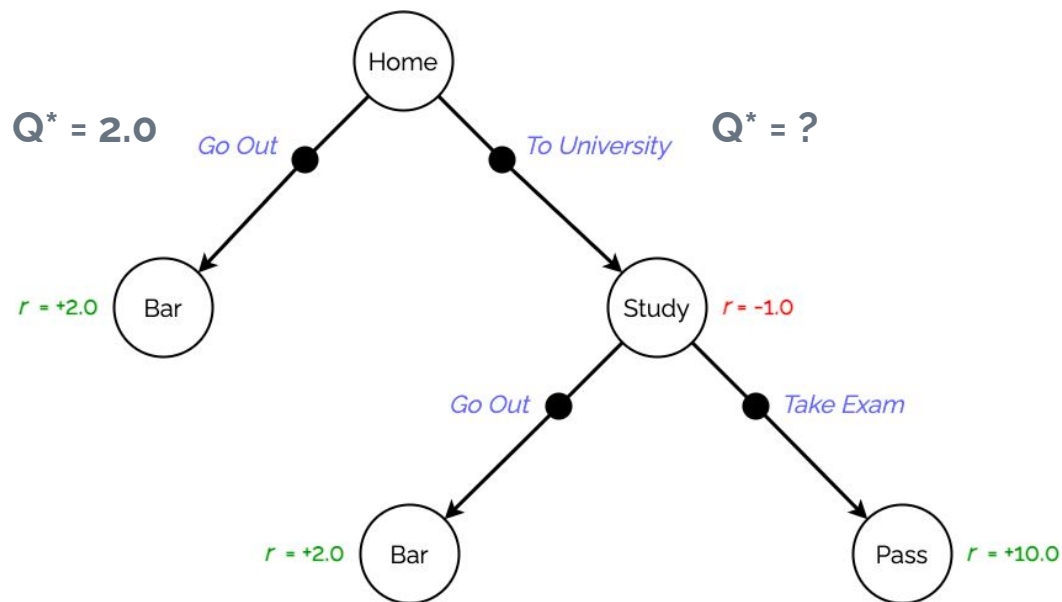
Illustration: Optimal Value



Question: What is $Q^*(\text{Home}, \text{Go Out})$?

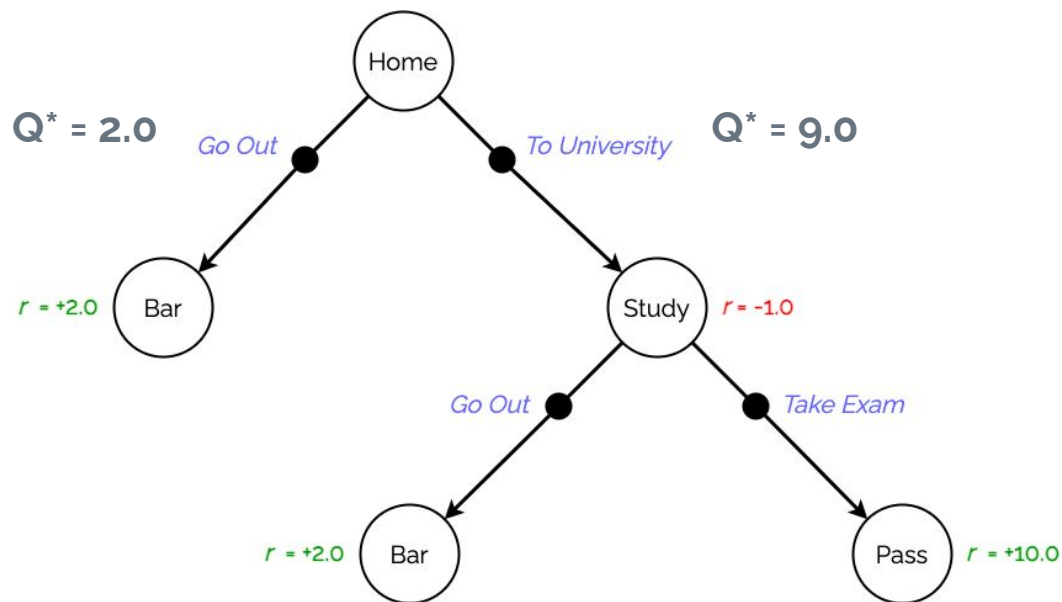
Answer: 2.0

Illustration: Optimal Value



Question: What is $Q^*(\text{Home}, \text{To University})$?

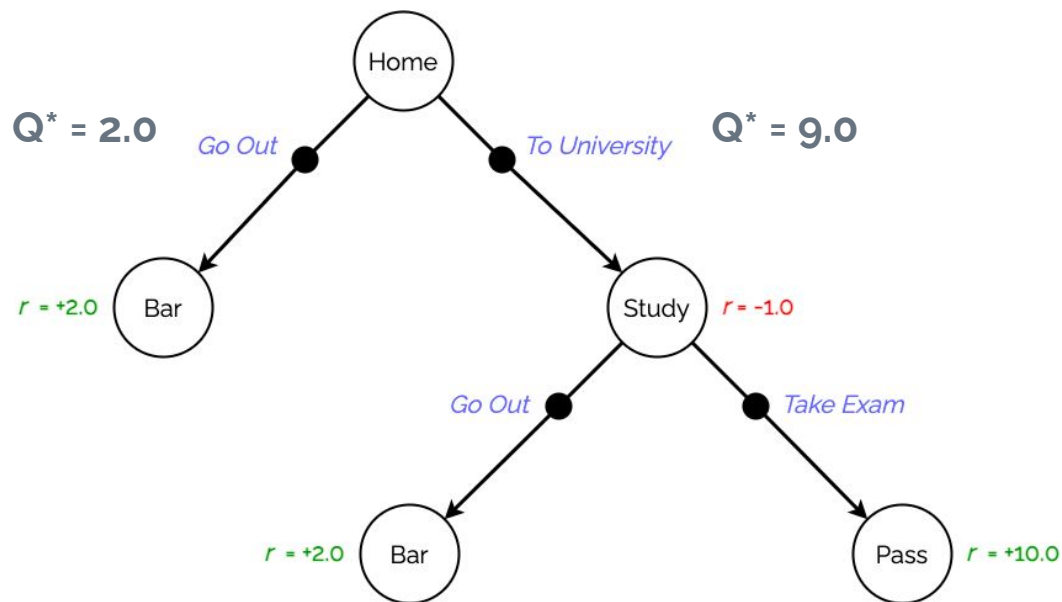
Illustration: Optimal Value



Question: What is $Q^*(\text{Home}, \text{To University})$?

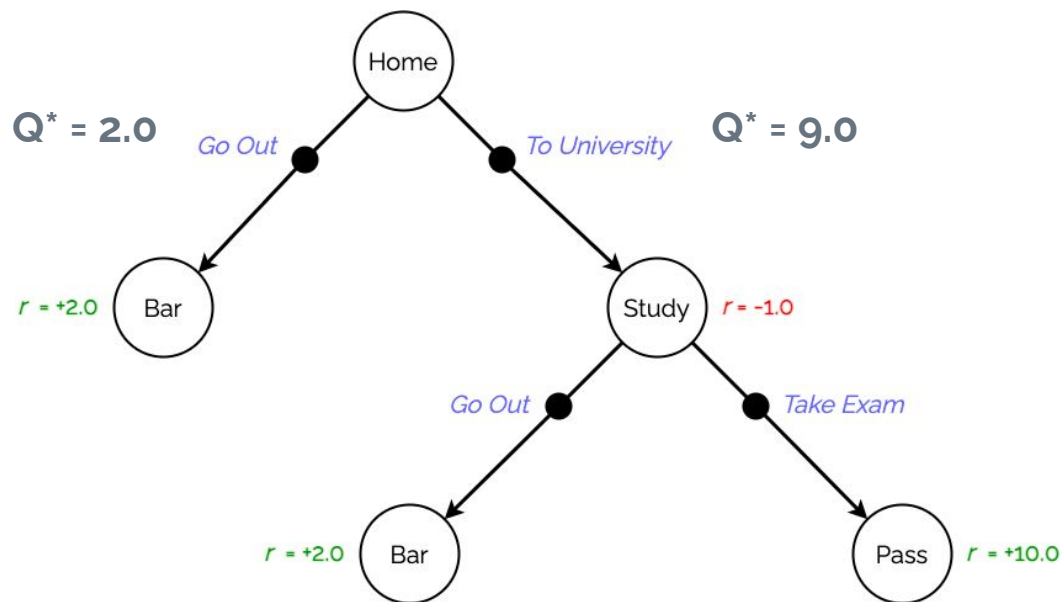
Answer: $-1.0 + 10.0 = 9.0$

Illustration: Optimal Value



Question: What should you do at Home?

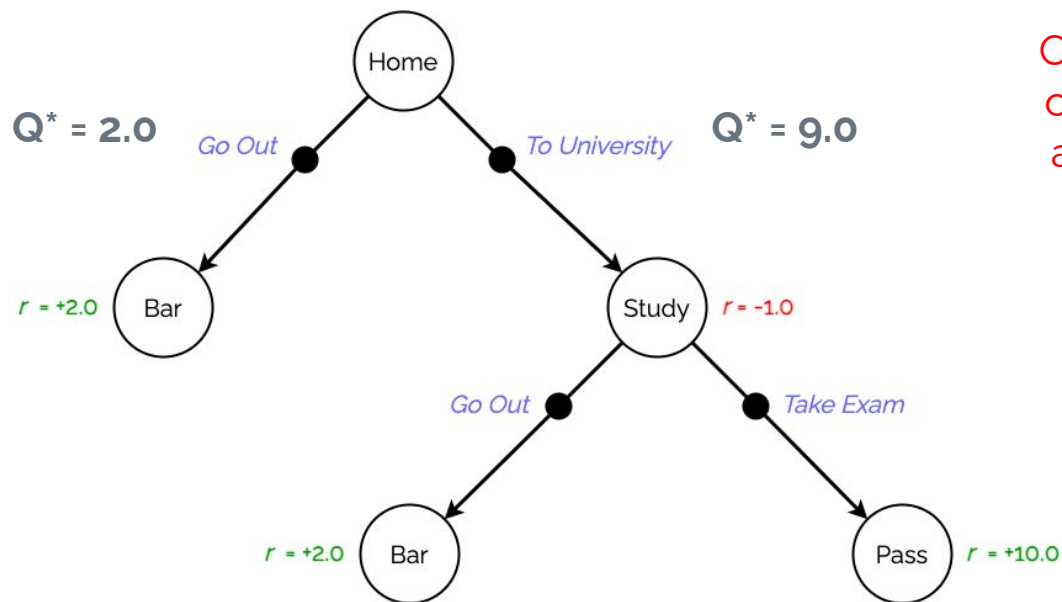
Illustration: Optimal Value



Question: What should you do at Home?

Answer: Come to University!

Illustration: Optimal Value



Once we know the optimal values we also know how to act optimally

Question: What should you do at Home?

Answer: Come to University!

Part III

The Reinforcement Learning Cycle

Challenge

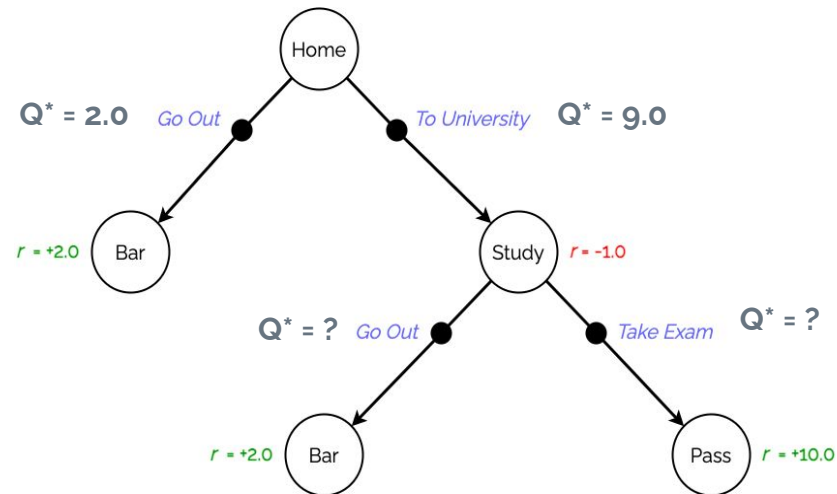


Challenge

Problem: In practice we don't know the problem structure and optimal Q-values.

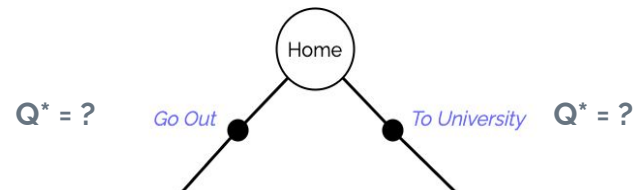
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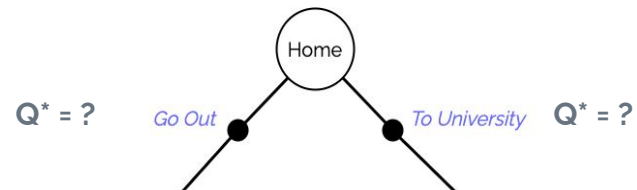
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Challenge

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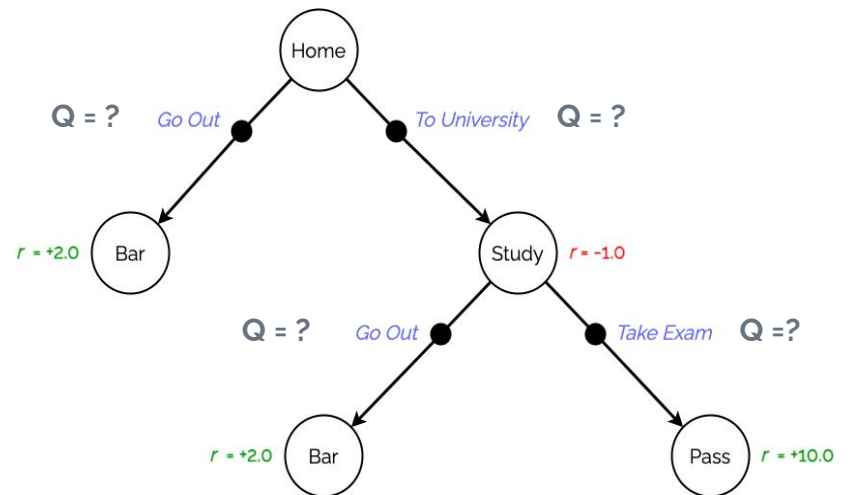
Solution: Learn through trial and error.

The Reinforcement Learning Cycle



The Reinforcement Learning Cycle

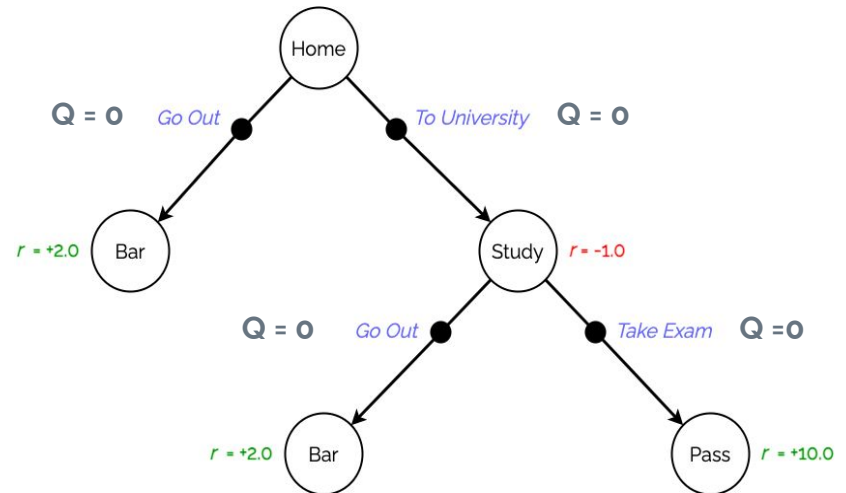
Pseudocode



The Reinforcement Learning Cycle

Pseudocode

Initialize $Q(s,a)$ solution estimates for all states and actions (e.g. to 0)

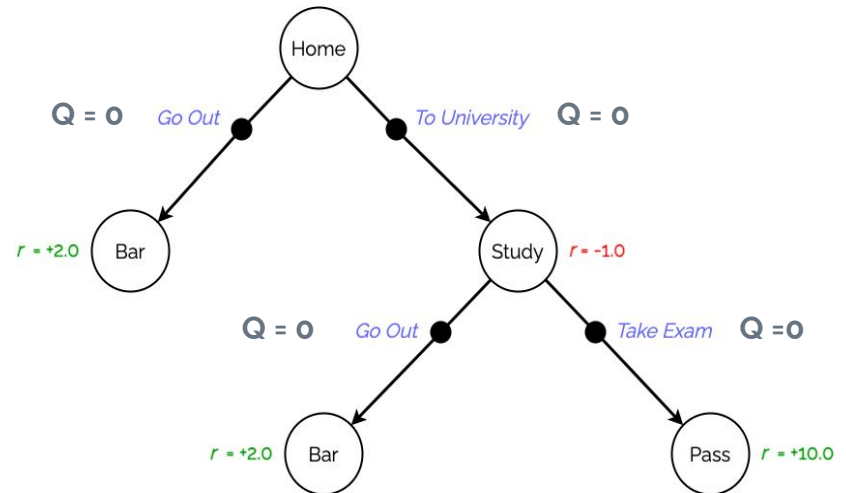


The Reinforcement Learning Cycle

Pseudocode

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Repeat:



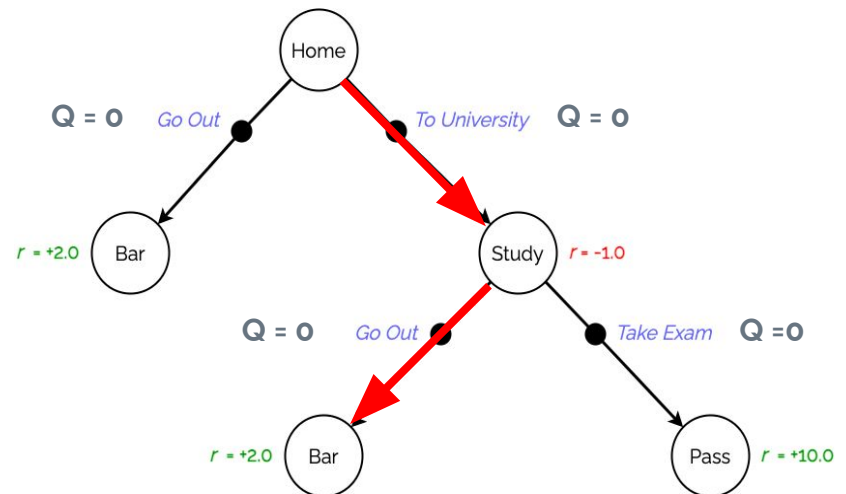
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- 1) Exploration: Sample a sequence of actions.



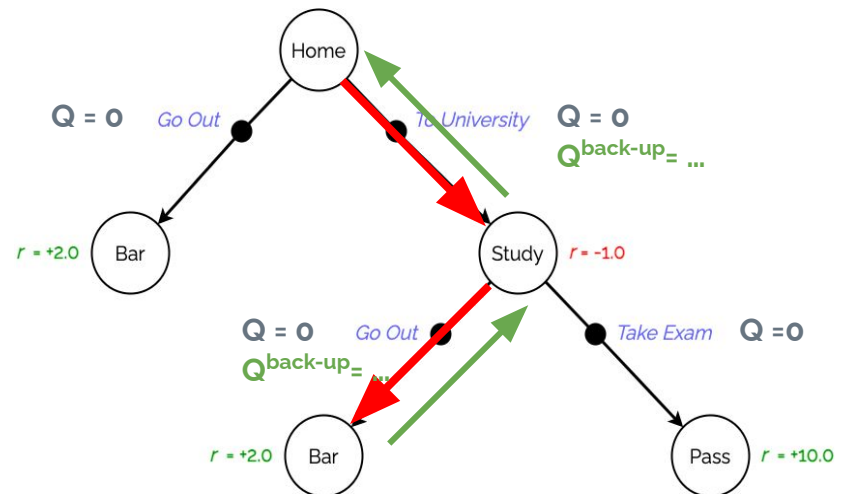
The Reinforcement Learning Cycle

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Initialize $Q(s,a)$ solution estimates for all states and actions (e.g. to 0)

Repeat:

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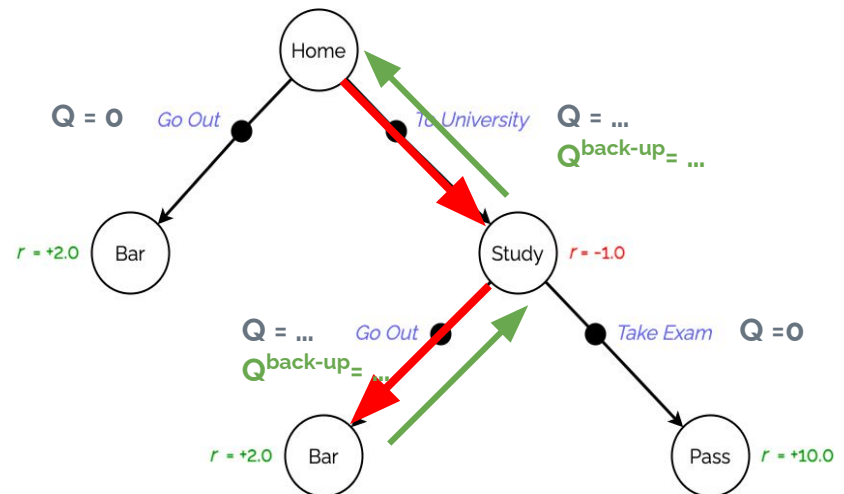
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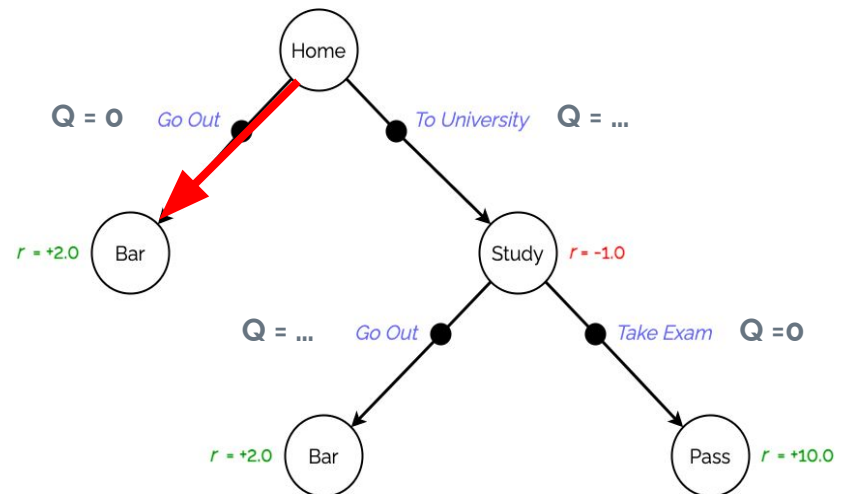
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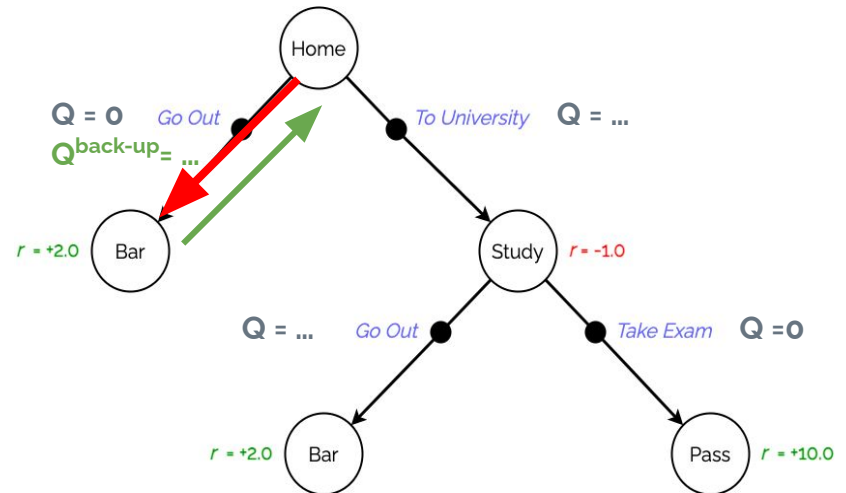
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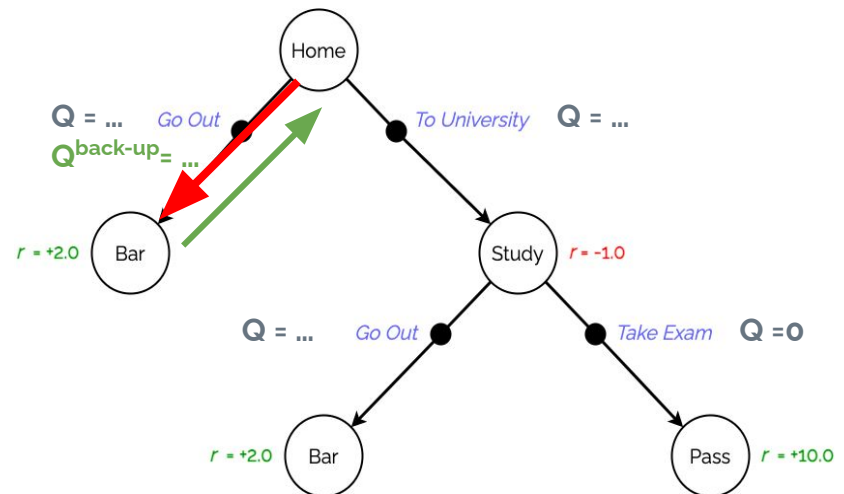
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The Reinforcement Learning Cycle

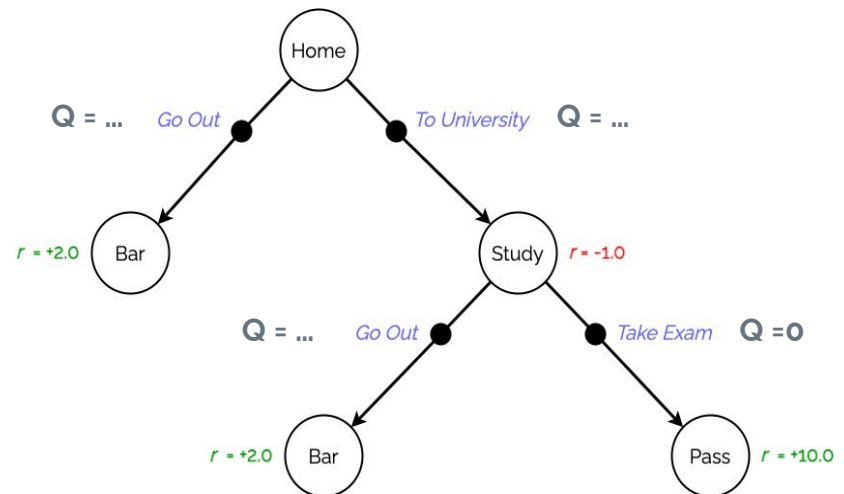
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etc.



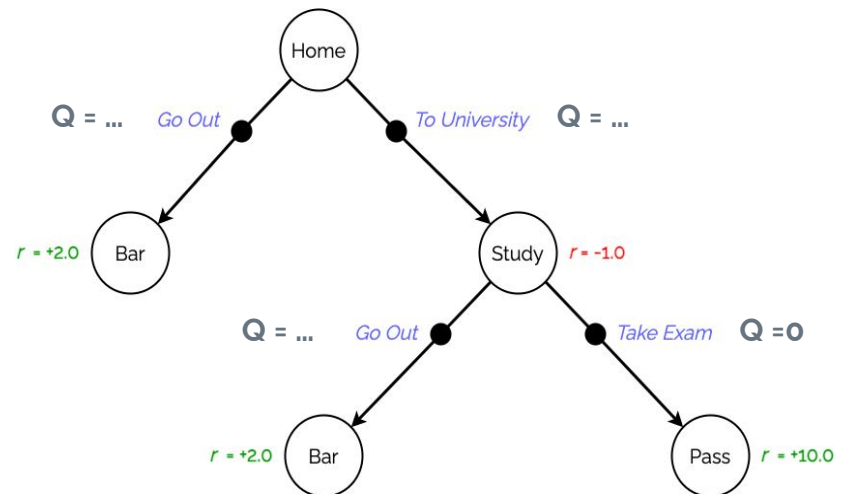
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We will discuss all three steps, but in reverse order

Part III A

Learning Update

Learning update (tabular)



Learning update (tabular)

(Really a supervised learning topic, we will briefly discuss this in one slide.)

Learning update (tabular)

$$Q(s, a) \leftarrow Q(s, a) + \eta \cdot \left(Q^{\text{back-up}}(s, a) - Q(s, a) \right)$$

Learning update (tabular)

$$Q(s, a) \leftarrow Q(s, a) + \boxed{\eta} \cdot \left(Q^{\text{back-up}}(s, a) - Q(s, a) \right)$$

learning rate: $\eta \in [0, 1]$

Learning update (tabular)

$$Q(s, a) \leftarrow Q(s, a) + \eta \cdot \left(Q^{\text{back-up}}(s, a) - Q(s, a) \right)$$

To update our solution...

Learning update (tabular)

$$Q(s, a) \leftarrow \boxed{Q(s, a)} + \eta \cdot \left(Q^{\text{back-up}}(s, a) - Q(s, a) \right)$$

To update our solution we take the current solution...

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To update our solution we take the current solution and move it a (small) step...

Learning update (tabular)

$$Q(s, a) \leftarrow Q(s, a) + \eta \cdot \left(Q^{\text{back-up}}(s, a) - Q(s, a) \right)$$

To update our solution we take the current solution and move it a (small) step...

...in the direction of the back-up estimate.

Learning update (tabular)

'training target'



$$Q(s, a) \leftarrow Q(s, a) + \eta \cdot \left(Q^{\text{back-up}}(s, a) - Q(s, a) \right)$$

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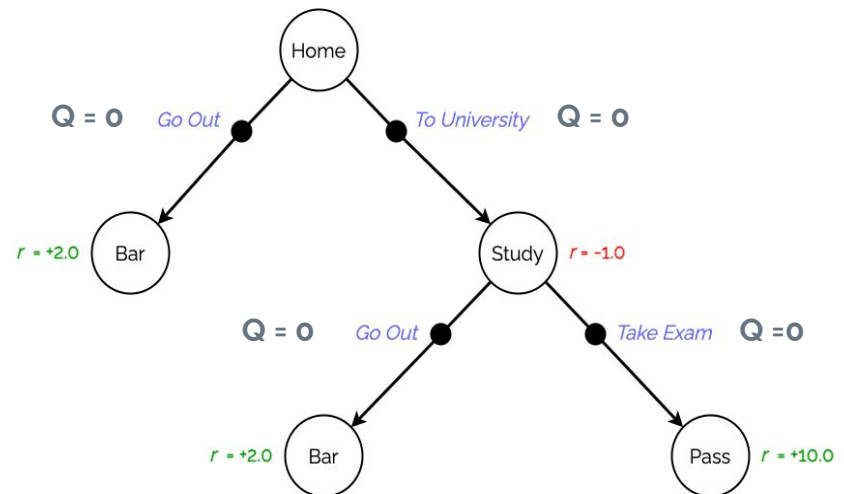
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Repeat:

- 1) Exploration: Sample a sequence of actions.
- 2) Credit assignment: Compute new value estimates $Q^{\text{back-up}}(s,a)$ for all actions along the path.
- 3) Learning update: Adjust our $Q(s,a)$ solution based on the back-up estimates $Q^{\text{back-up}}(s,a)$.



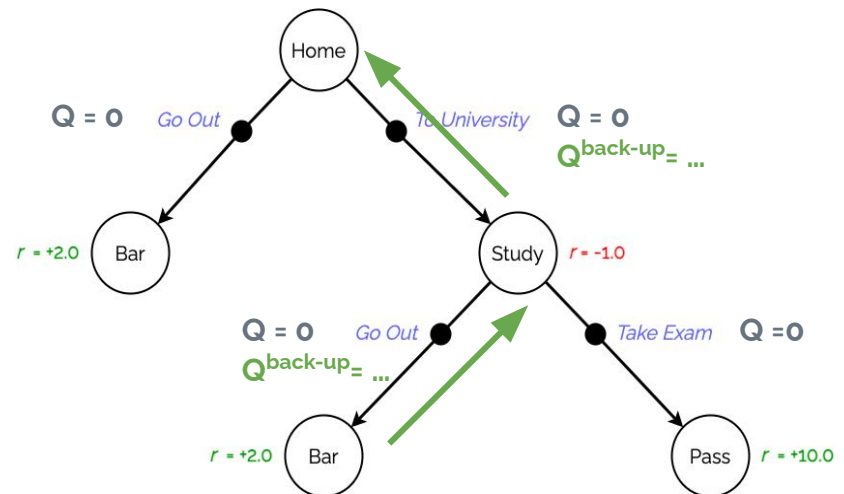
The Reinforcement Learning Cycle

Pseudocode

Initialize $Q(s,a)$ solution estimates for all states and actions (e.g. to 0)

Repeat:

- 1) Exploration: Sample a sequence of actions.
- 2) Credit assignment: Compute new value estimates $Q^{\text{back-up}}(s,a)$ for all actions along the path.
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Part III B

Credit Assignment

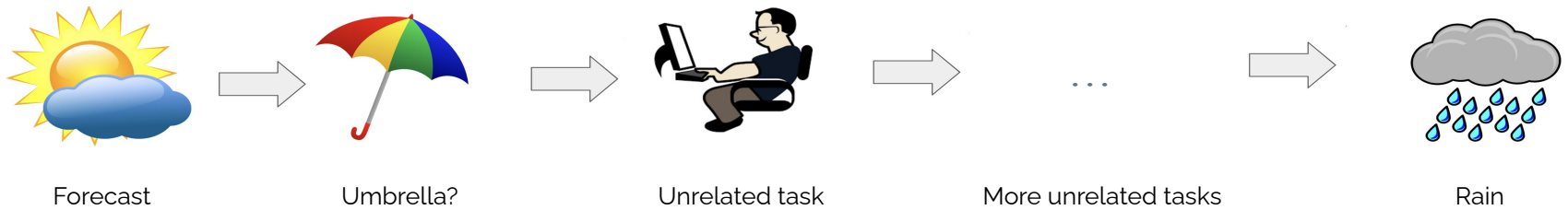
Credit assignment



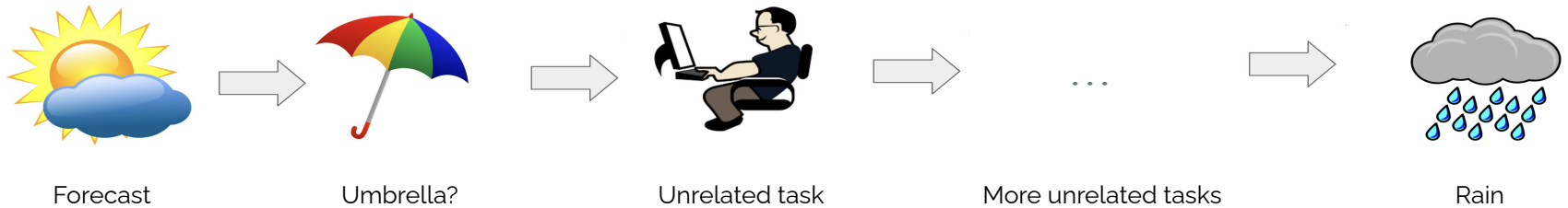
Credit assignment

(Also a topic in neural network training, but then the objective is differentiable)

Credit assignment



Credit assignment



Question: You get the reward (not soaked), but which of your previous actions deserve credit?

Credit assignment

You think this is easy, but humans actually also struggle:



Credit assignment

You think this is easy, but humans actually also struggle:



Credit assignment

You think this is easy, but humans actually also struggle:



Credit assignment

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Credit assignment

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Credit assignment

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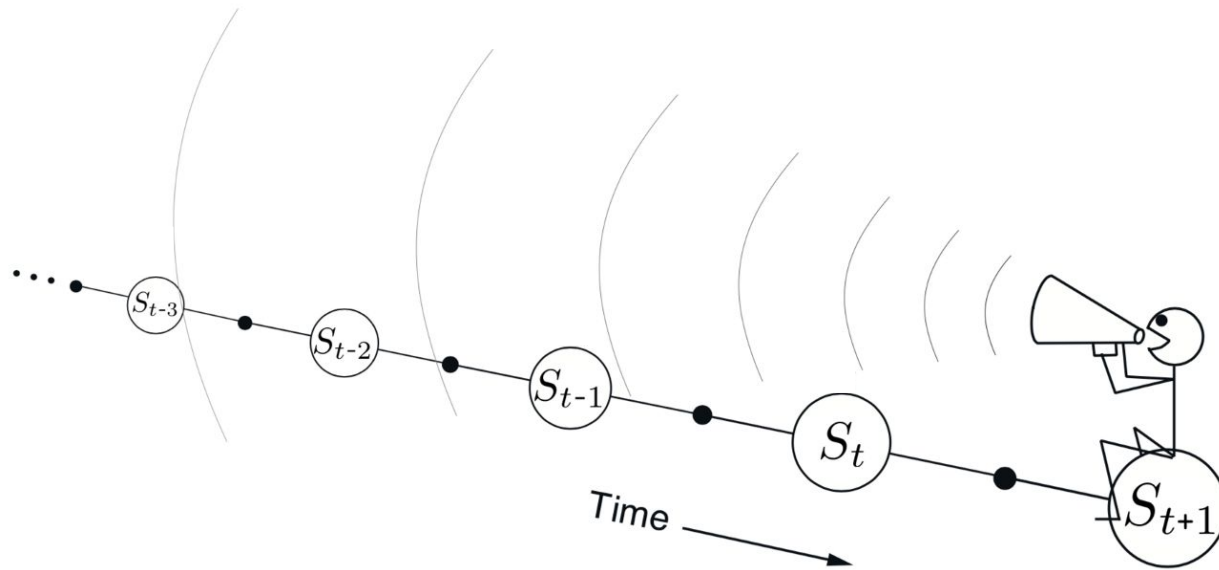


Superstition
=
failed credit assignment

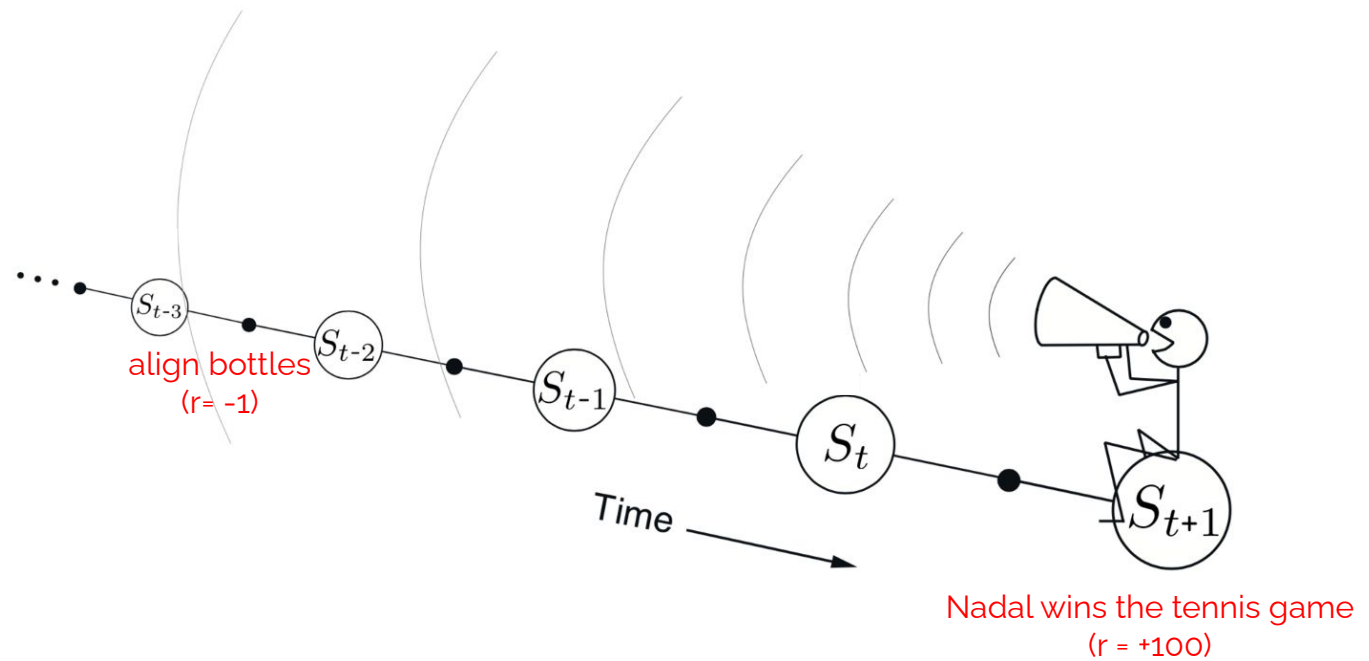
Credit assignment



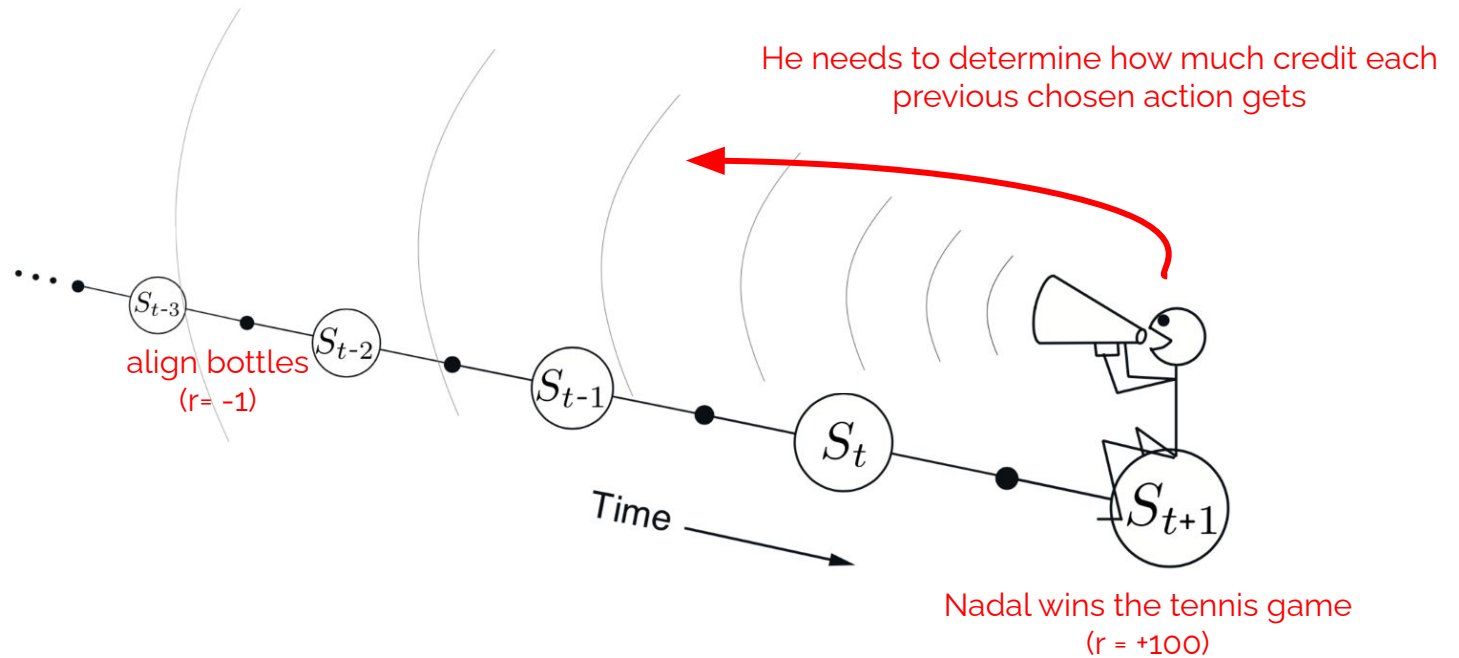
Credit assignment



Credit assignment

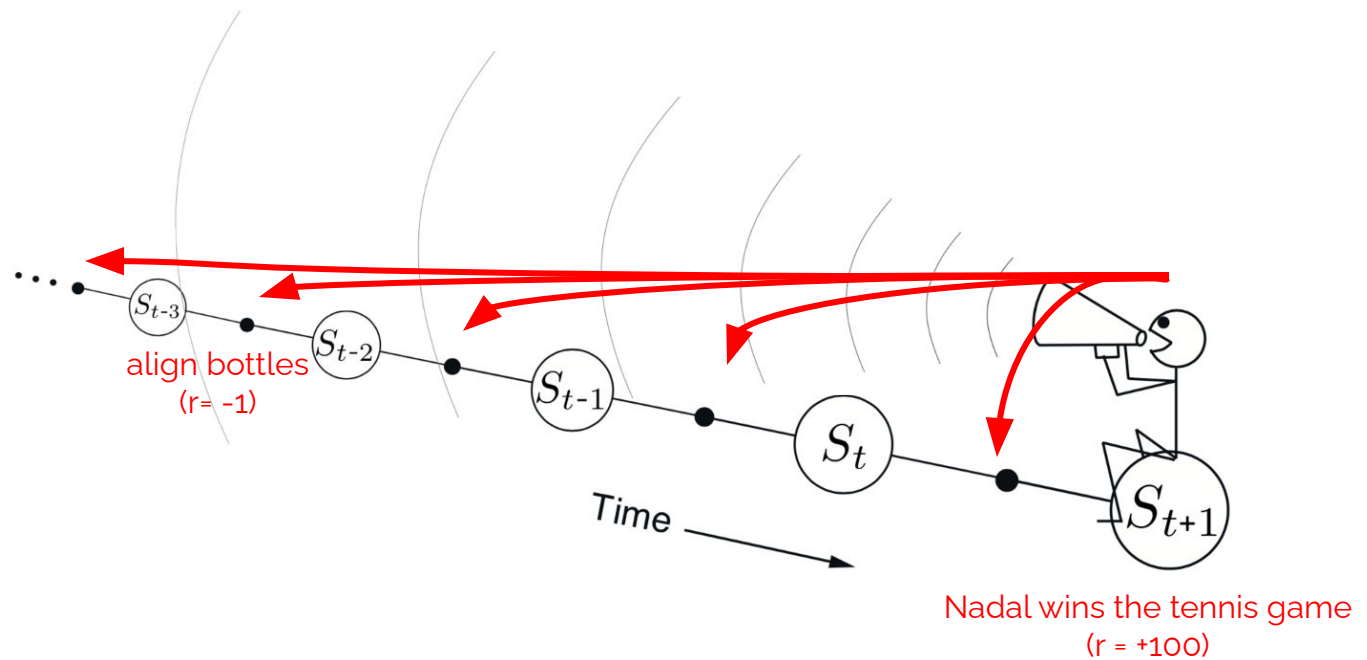


Credit assignment



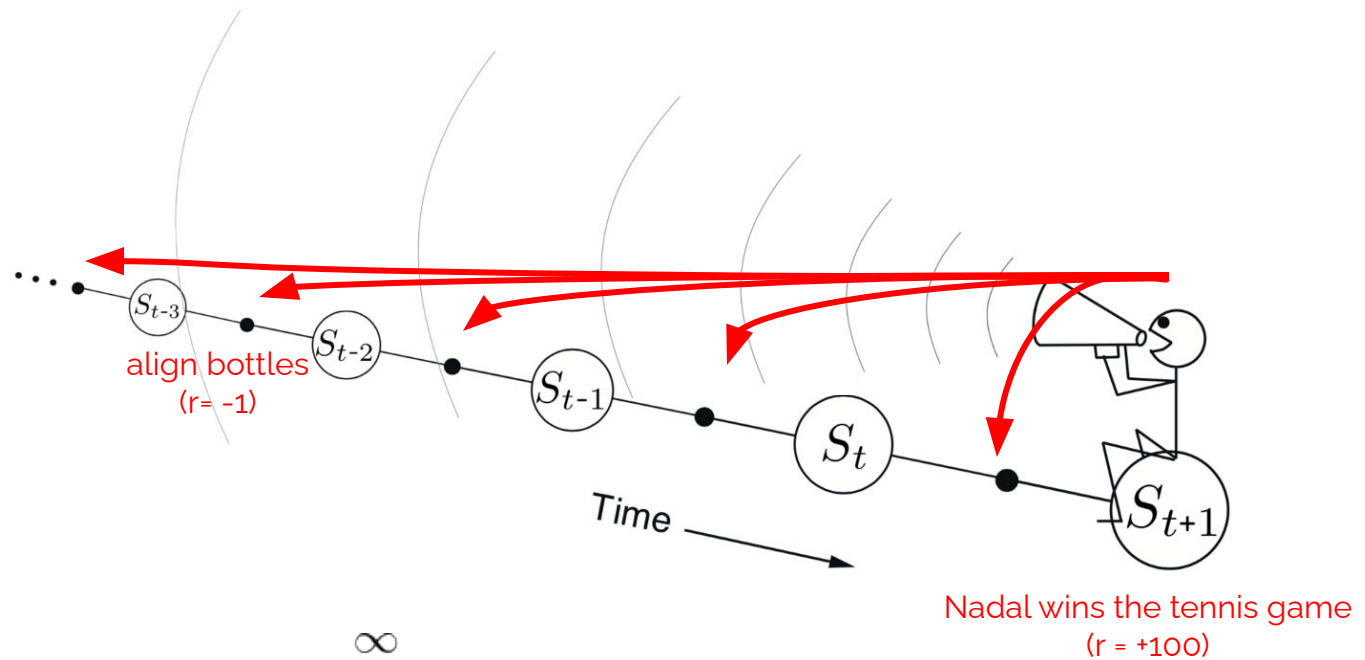
Credit assignment

One extreme: each action along the way gets full credit



Credit assignment

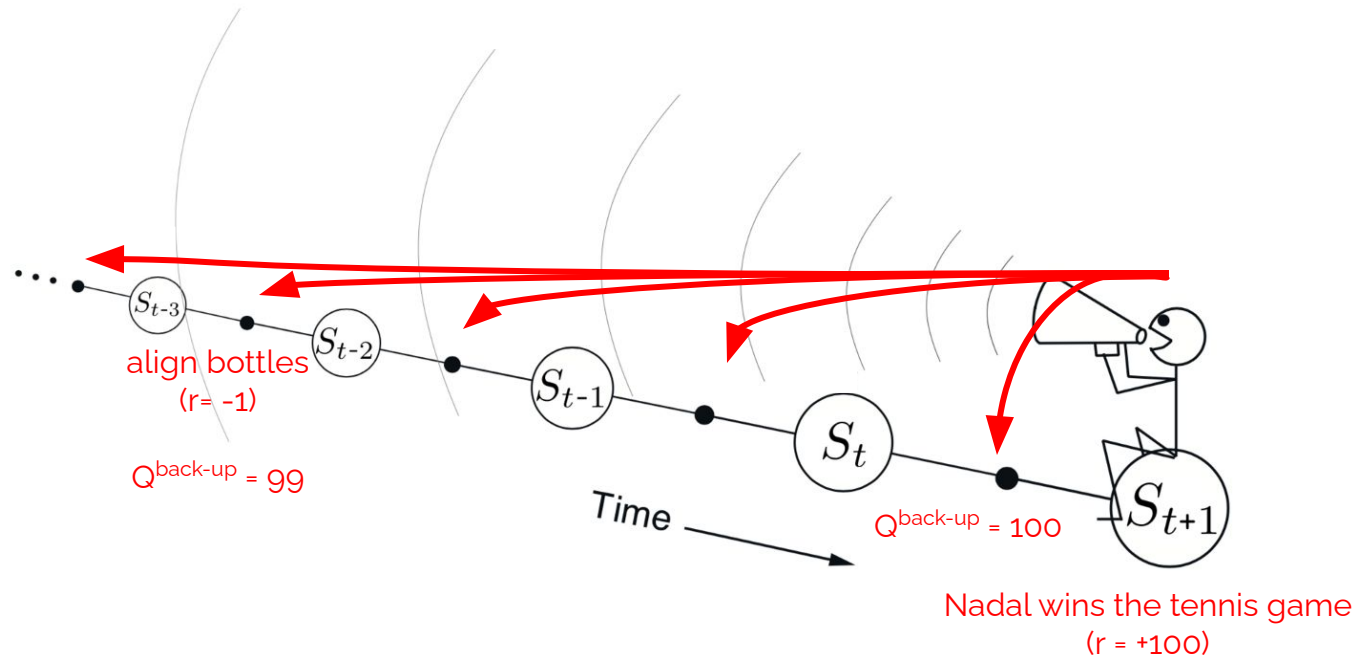
One extreme: each action along the way gets full credit



$$Q^{back-up}(s_t, a_t) = \sum_{i=0}^{\infty} r_{t+i}$$

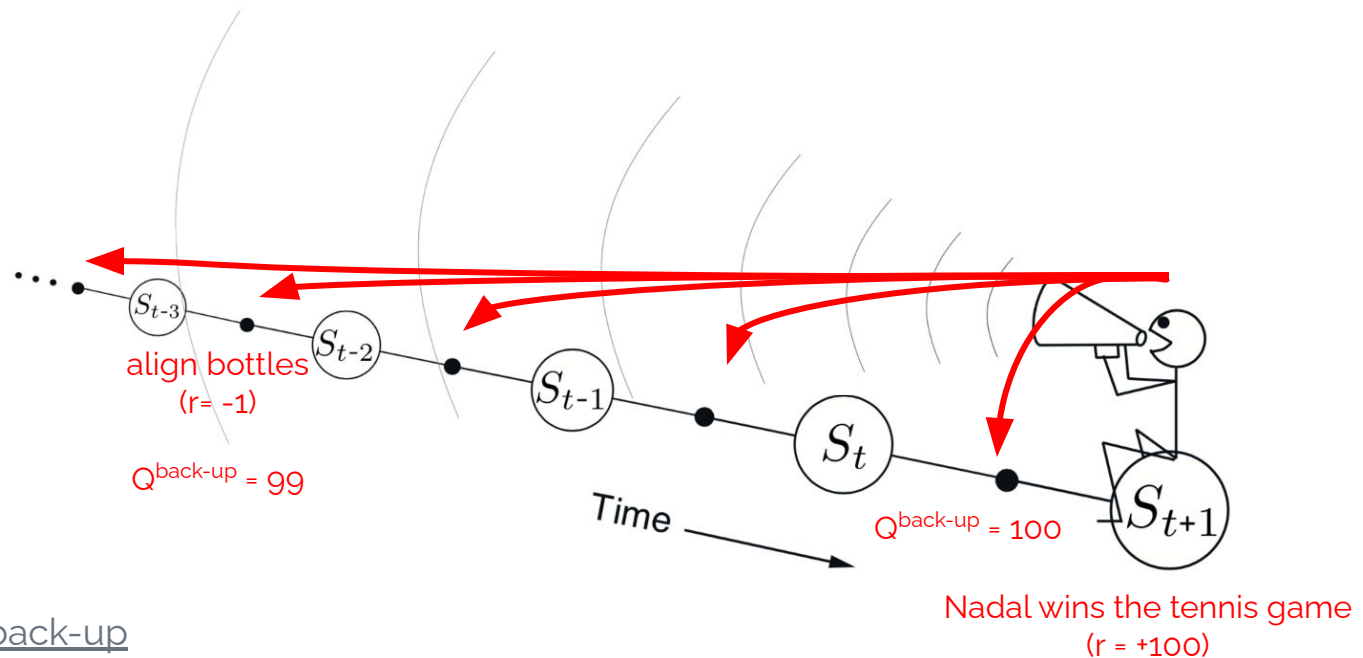
Credit assignment

One extreme: each action along the way gets full credit



Credit assignment

One extreme: each action along the way gets full credit

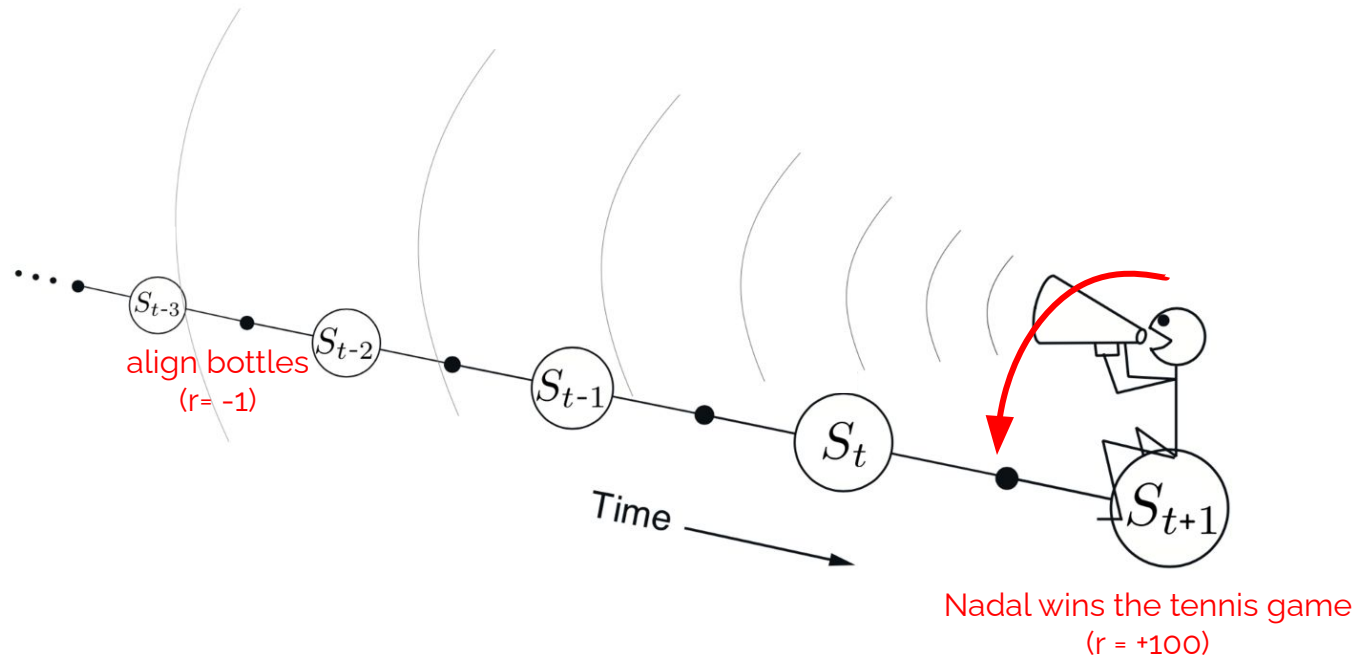


Monte Carlo back-up

- + Fast propagation.
- High variance (action may seem better or worse than it really is)

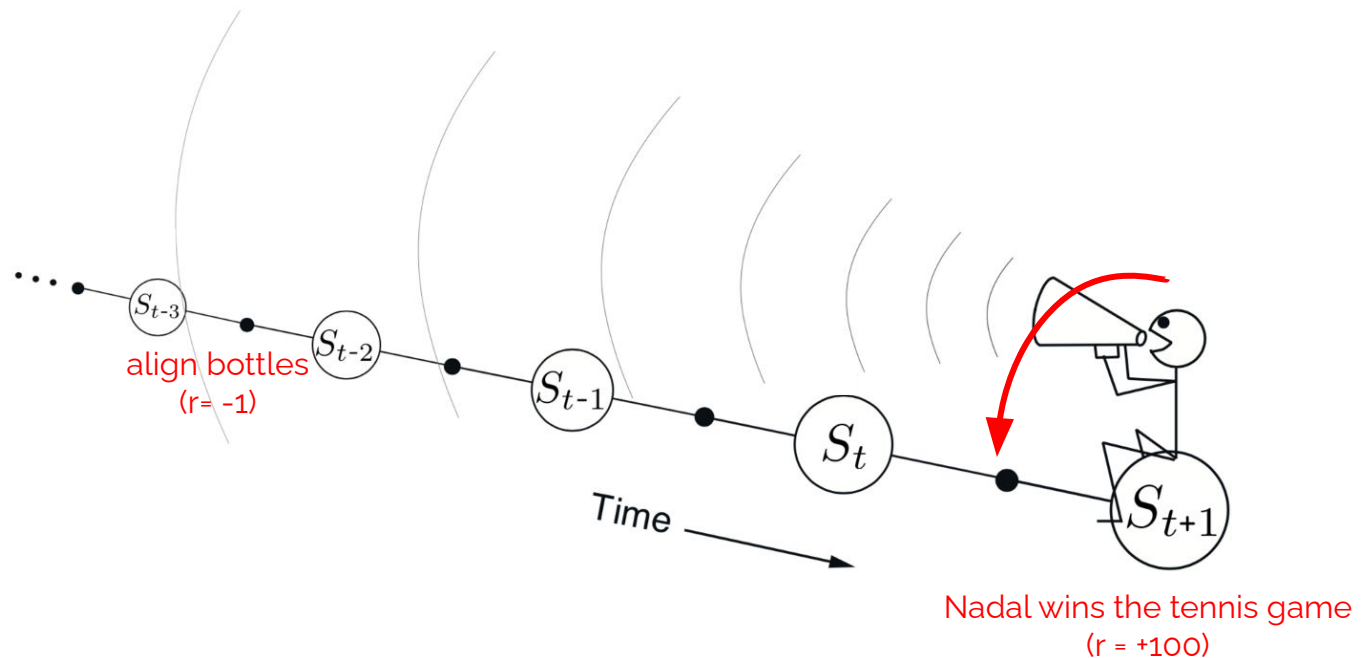
Credit assignment

Other extreme: only last action gets credit (for now).



Credit assignment

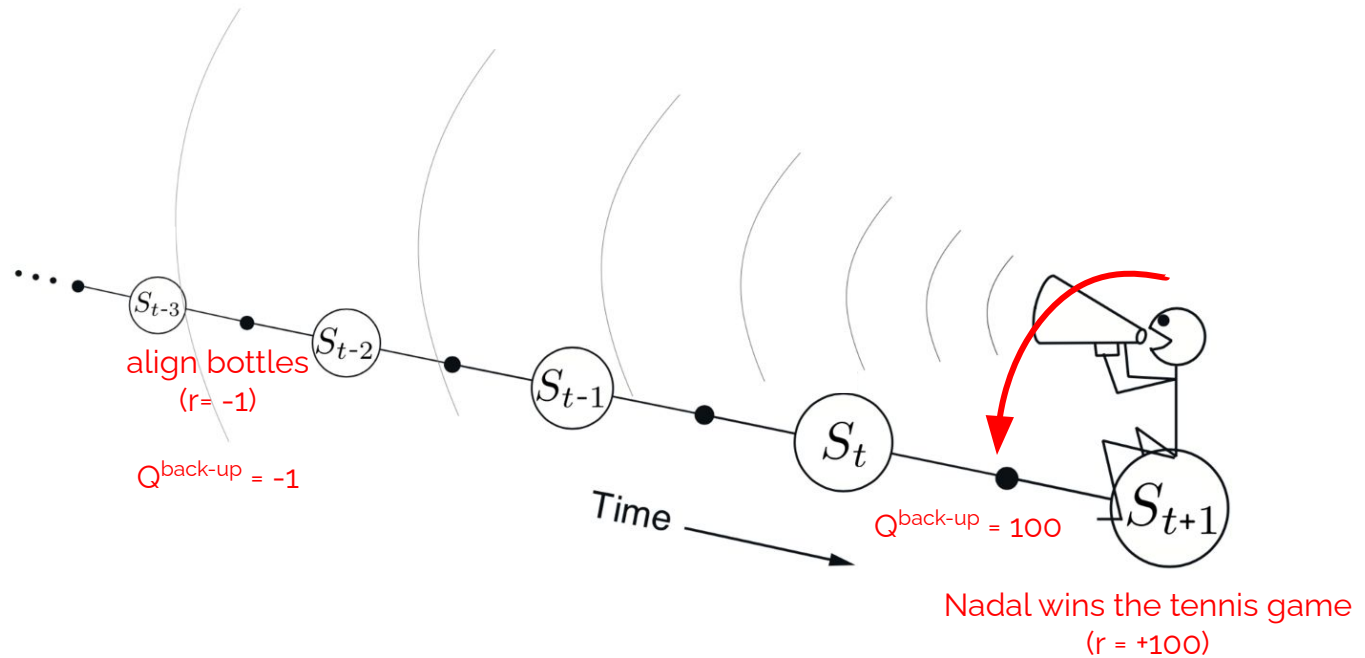
Other extreme: only last action gets credit (for now).



$$Q^{back-up}(s_t, a_t) = r_t + Q(s_{t+1}, a_{t+1})$$

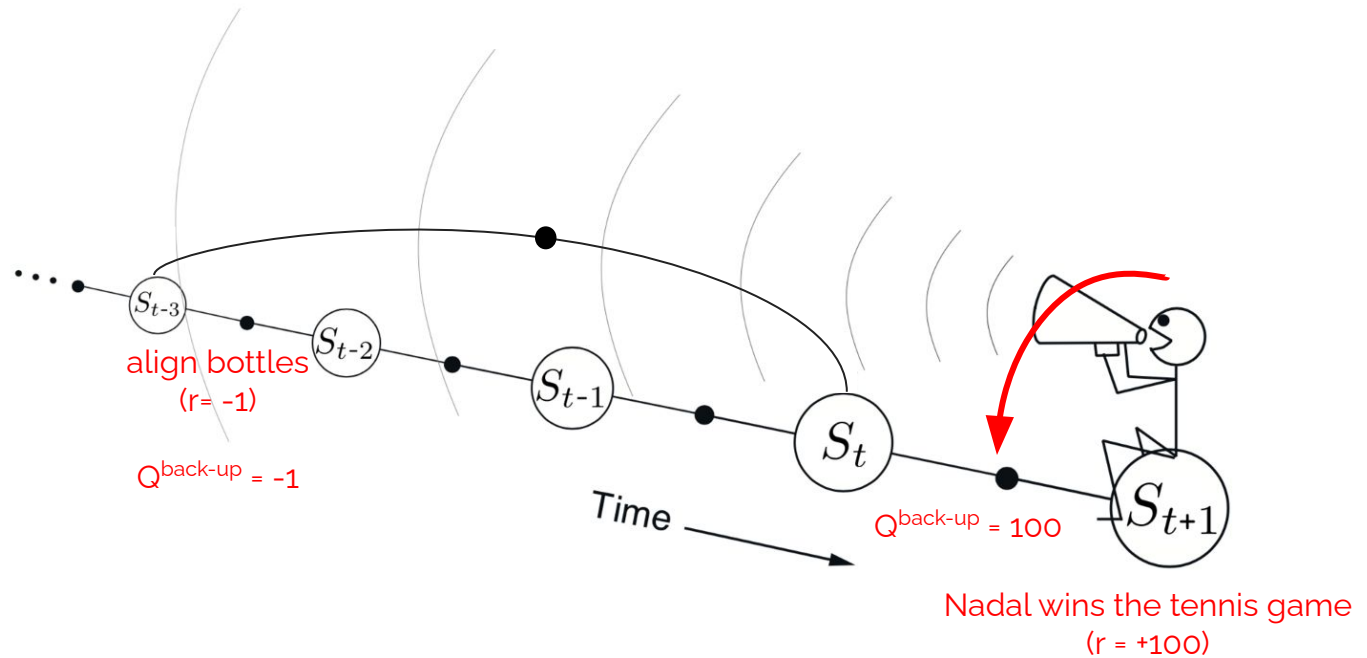
Credit assignment

Other extreme: only last action gets credit (for now).



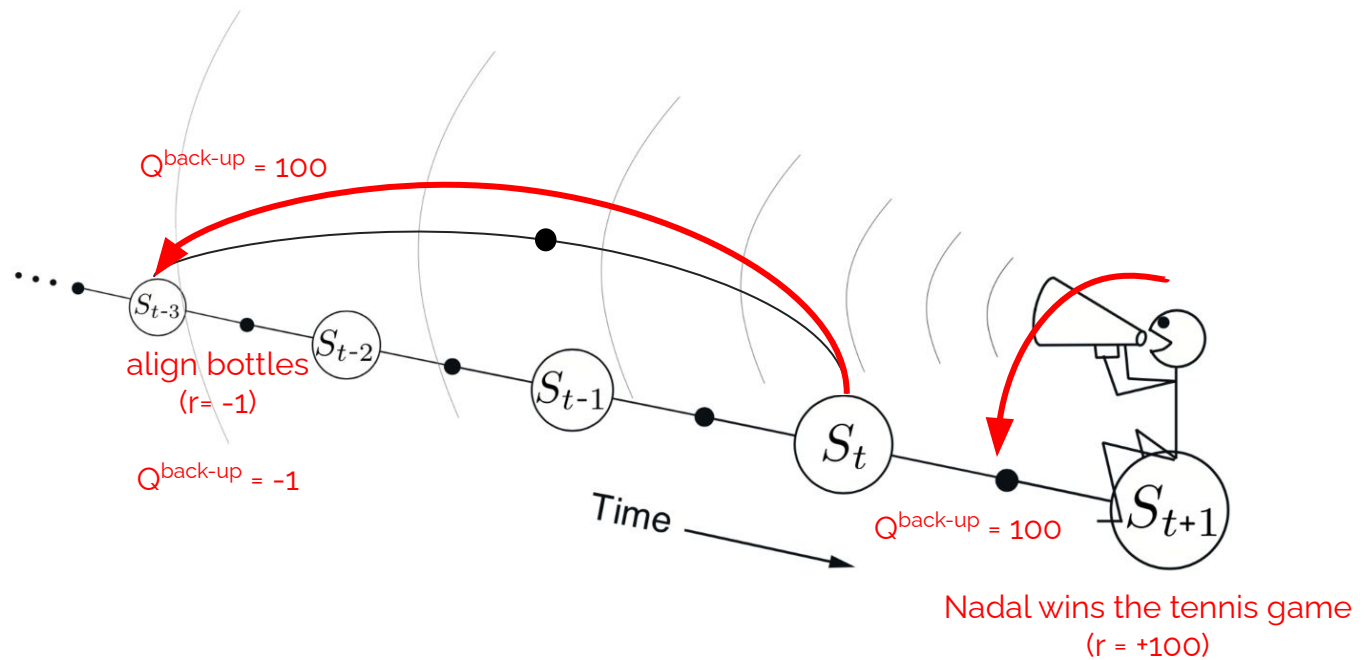
Credit assignment

Other extreme: only last action gets credit (for now).



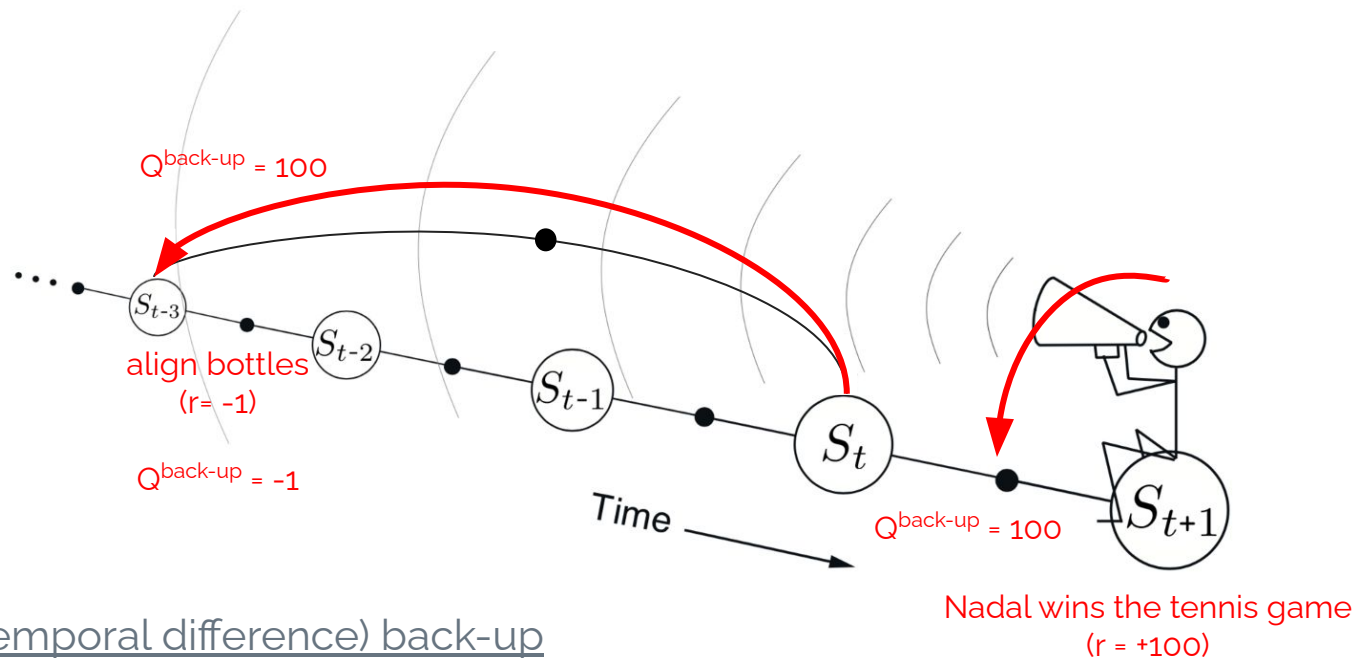
Credit assignment

Other extreme: only last action gets credit (for now).



Credit assignment

Other extreme: only last action gets credit (for now).



One-step (temporal difference) back-up

- + Low variance.
- Slow propagation.

Credit assignment

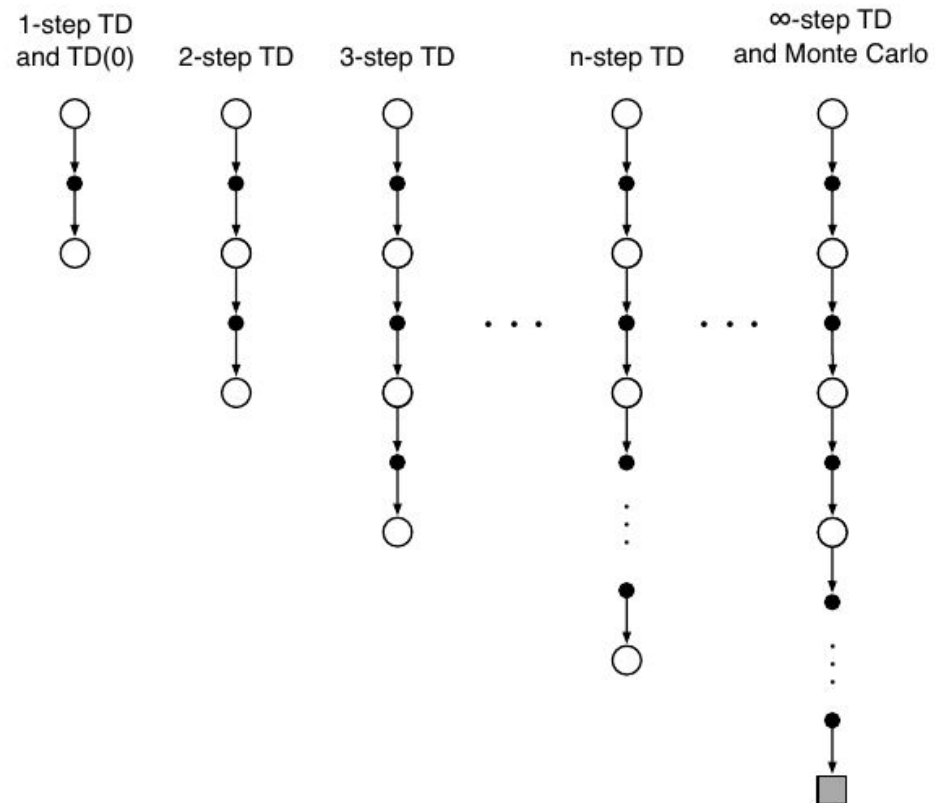


Credit assignment

Spectrum of back-up estimators

Credit assignment

Spectrum of back-up estimators



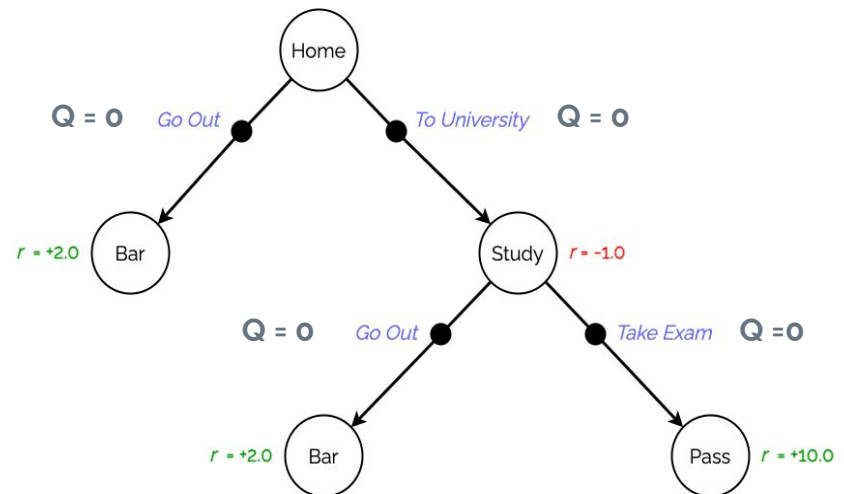
The Reinforcement Learning Cycle

Pseudocode

Initialize $Q(s,a)$ estimates for all states,actions (e.g. to 0)

Repeat:

- 1) Exploration: Sample a sequence of actions.
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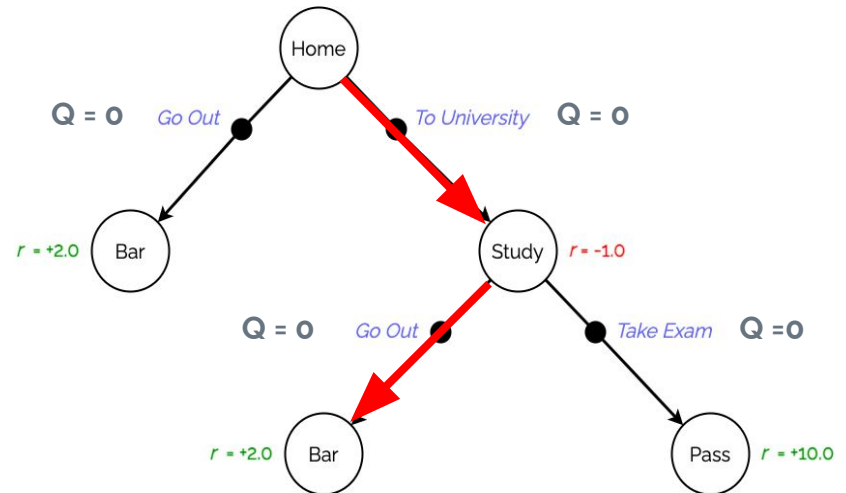
The Reinforcement Learning Cycle

Pseudocode

Initialize $Q(s,a)$ estimates for all states,actions
(e.g. to 0)

Repeat:

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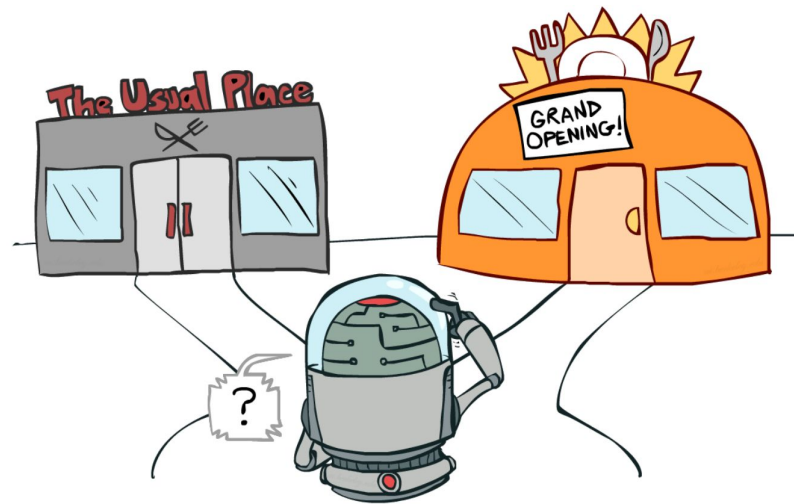
Part III C

Exploration

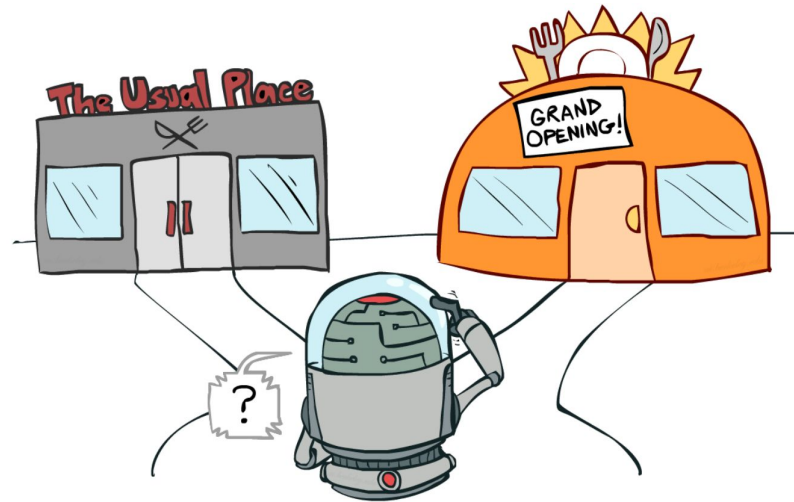
Exploration versus exploitation



Exploration versus exploitation

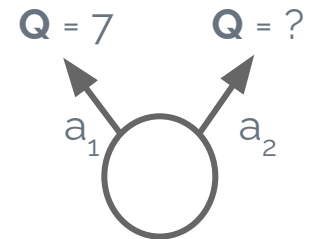
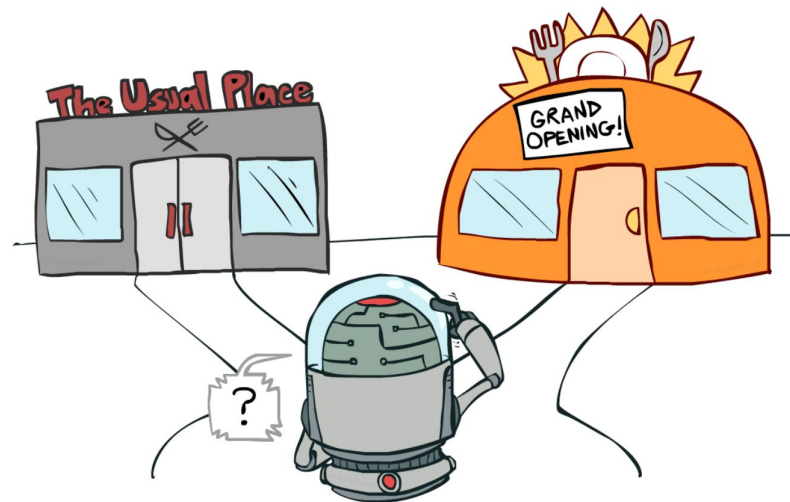


Exploration versus exploitation



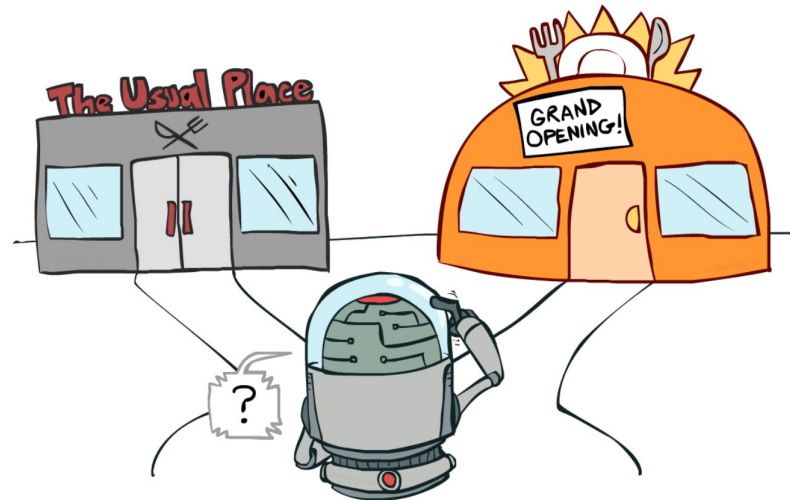
Question: The usual place scores a 7/10 on average. Which place would you choose?

Exploration versus exploitation



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Exploration versus exploitation



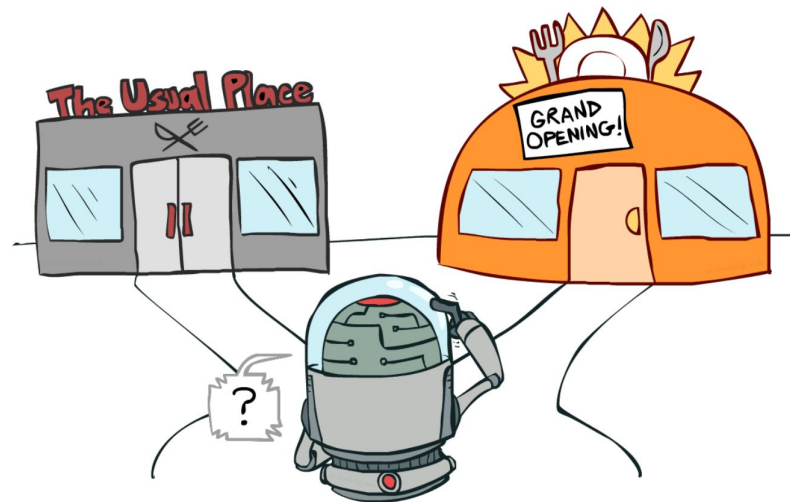
Exploitation

(commit to the current best option)

Exploration

(try something which is new or – currently – seems suboptimal)

Exploration versus exploitation



Exploitation

(commit to the current best option)

Exploration

(try something which is new or – currently – seems suboptimal)

We actually need to balance both

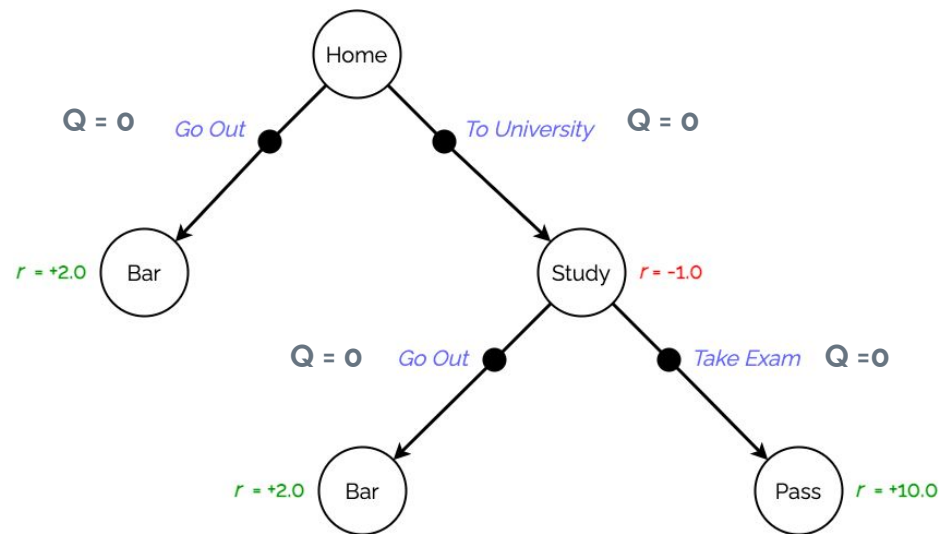
Exploration/Exploitation trade-off

We need **exploration** because actions may look worse than they are.

Exploration/Exploitation trade-off

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Reasons:

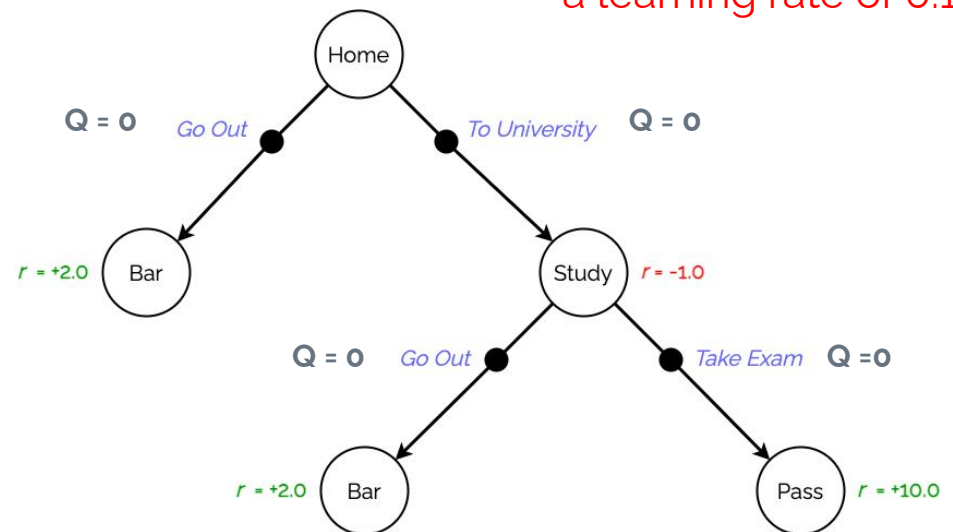


Exploration/Exploitation trade-off

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Reasons:

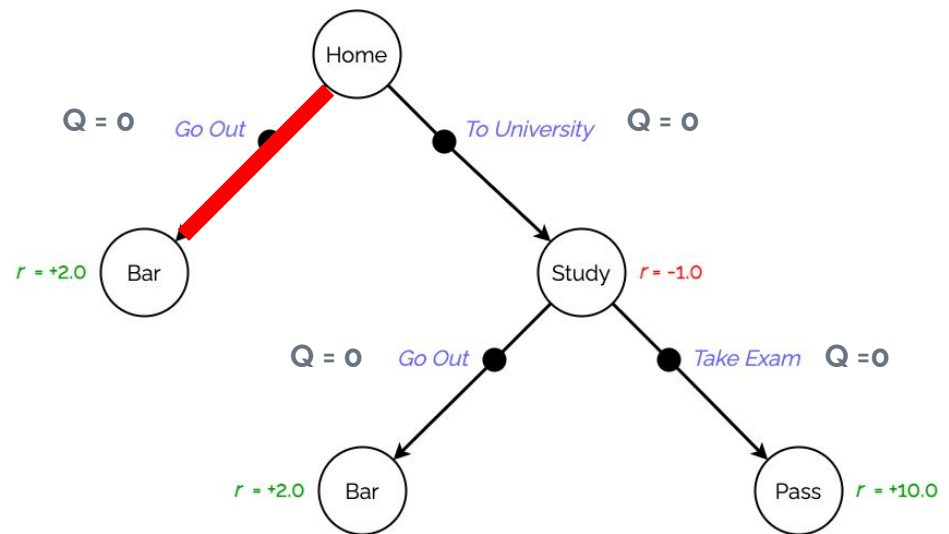
We will use Monte Carlo back-ups and a learning rate of 0.1



Exploration/Exploitation trade-off

We need **exploration** because actions may look worse than they are.

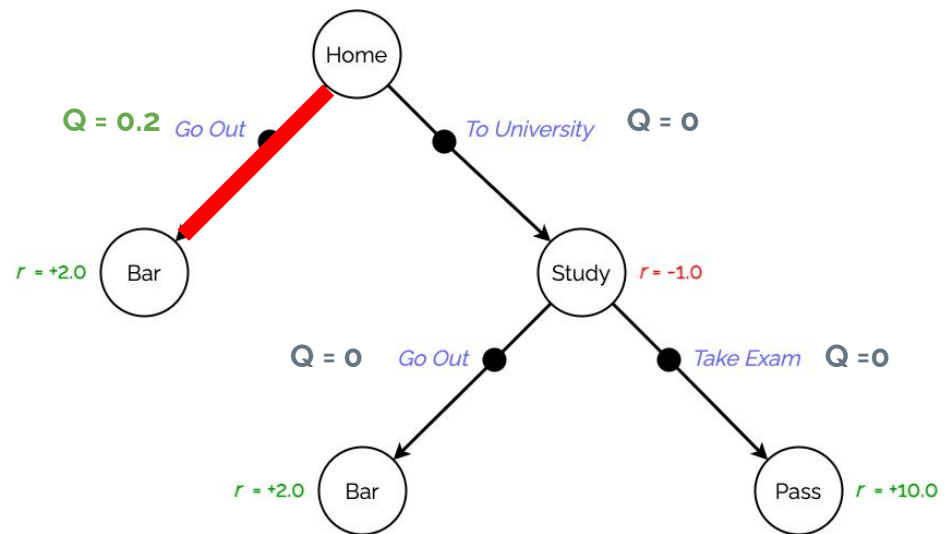
Reasons:



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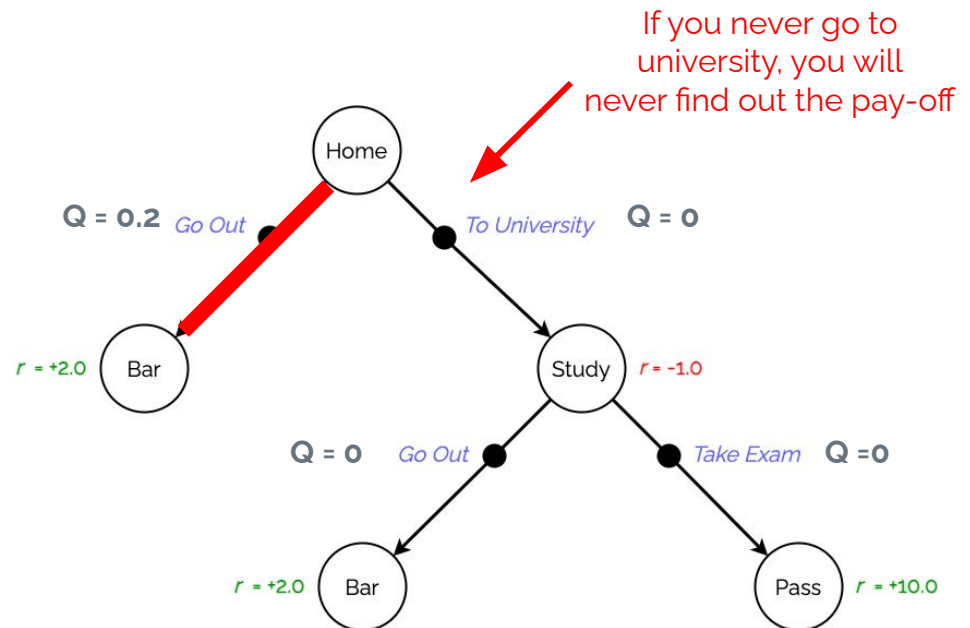
Reasons:



Exploration/Exploitation trade-off

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Reasons:

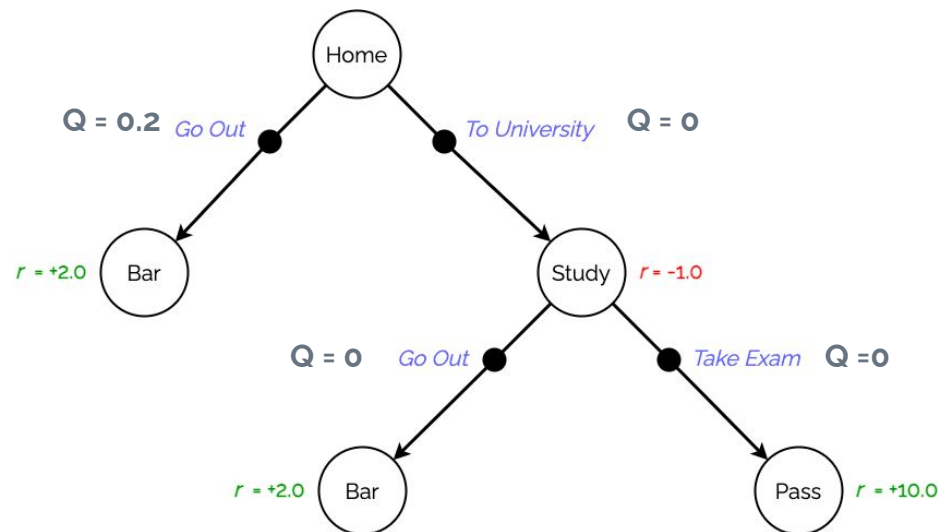


Exploration/Exploitation trade-off

We need **exploration** because actions may look worse than they are.

Reasons:

1. We need to collect our own data

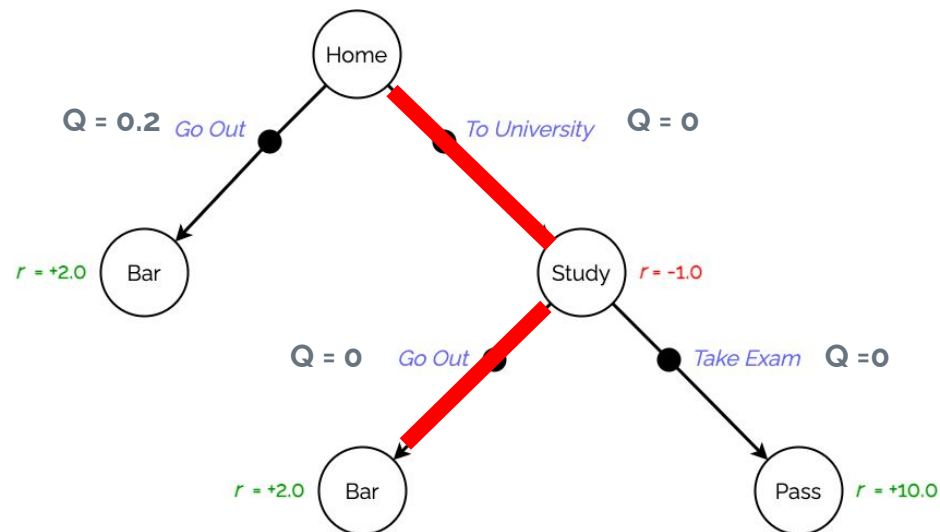


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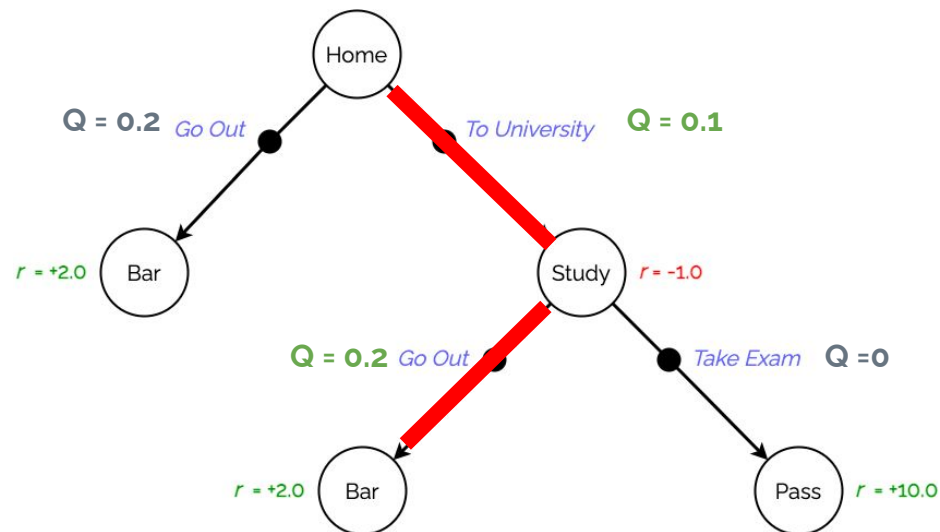


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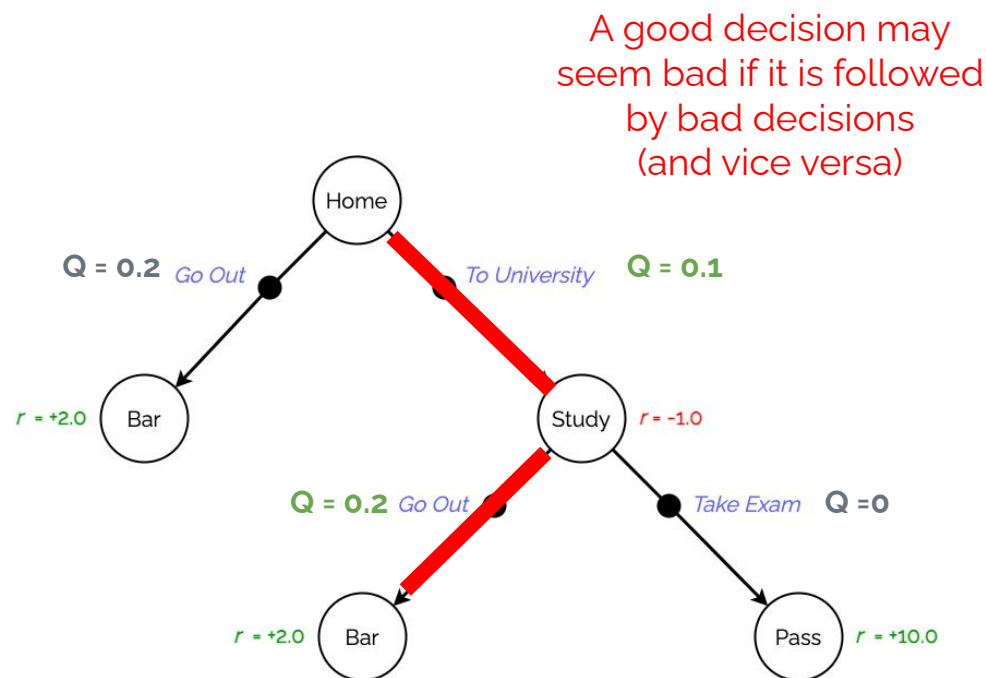


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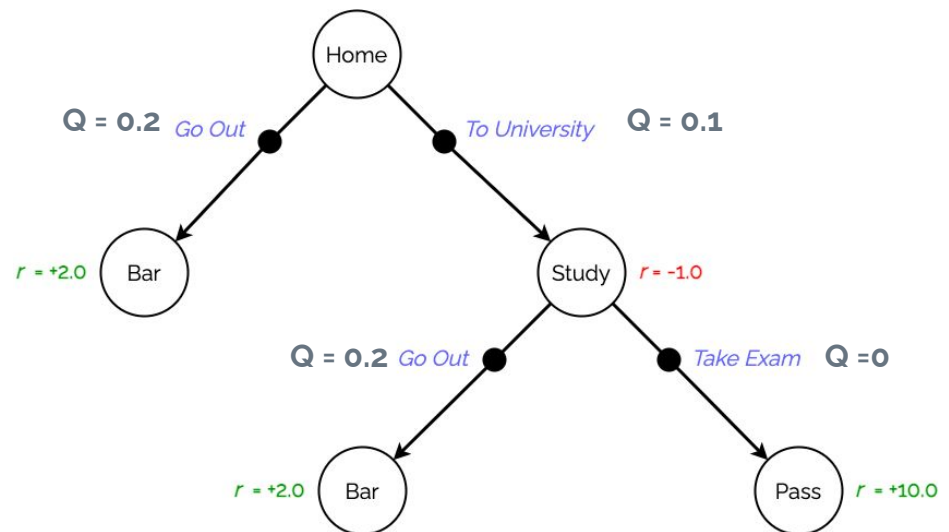


Exploration/Exploitation trade-off

We need **exploration** because actions may look worse than they are.

Reasons:

1. We need to collect our own data
2. Good action may seem bad if followed by bad actions

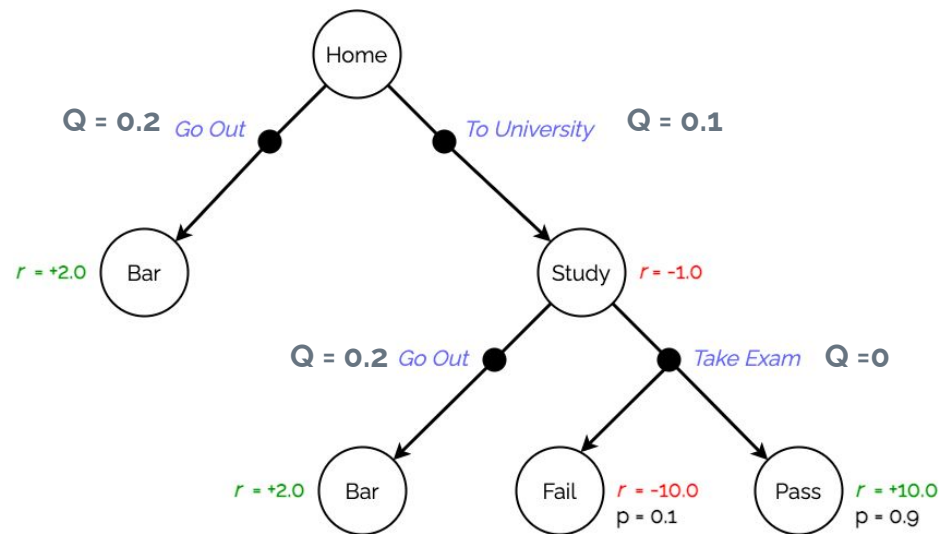


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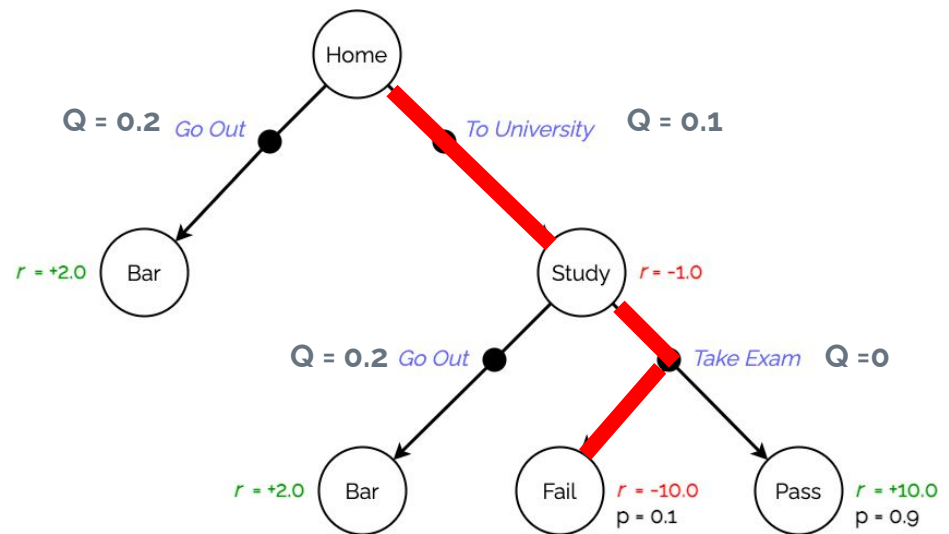


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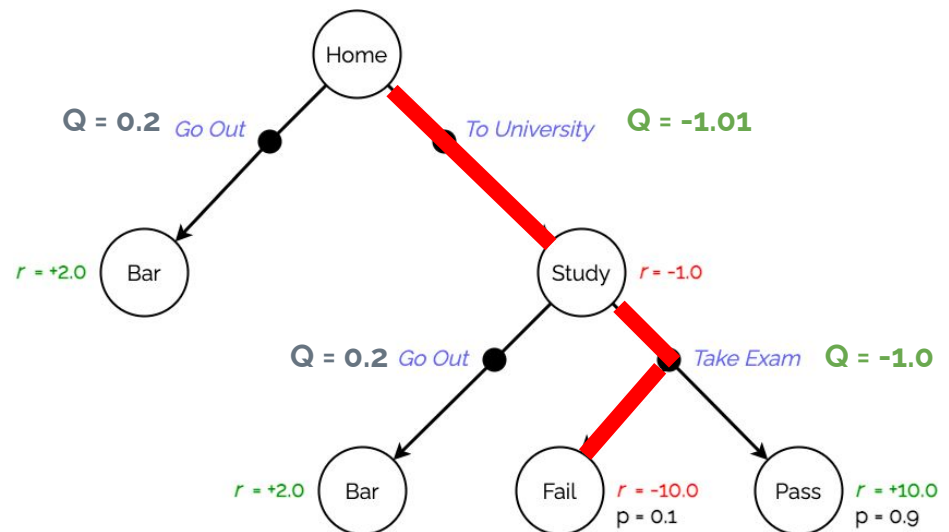


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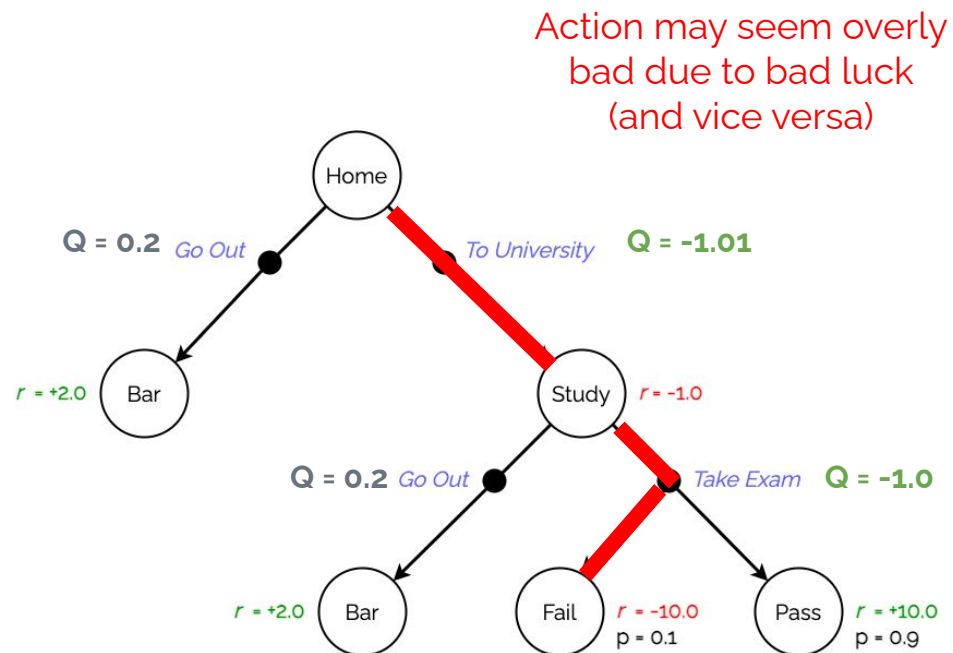


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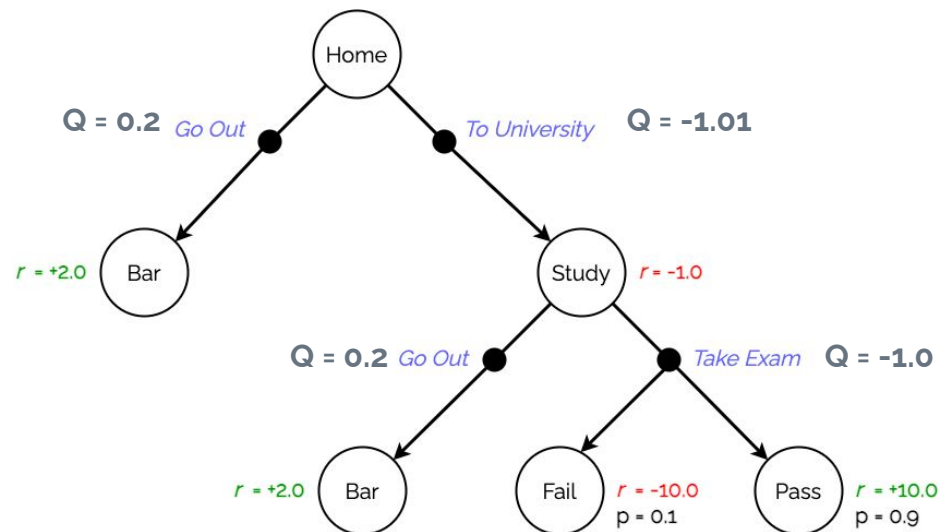


Exploration/Exploitation trade-off

We need **exploration** because actions may look worse than they are.

Reasons:

1. We need to collect our own data
2. Good action may seem bad if followed by bad actions
3. Environment can be stochastic

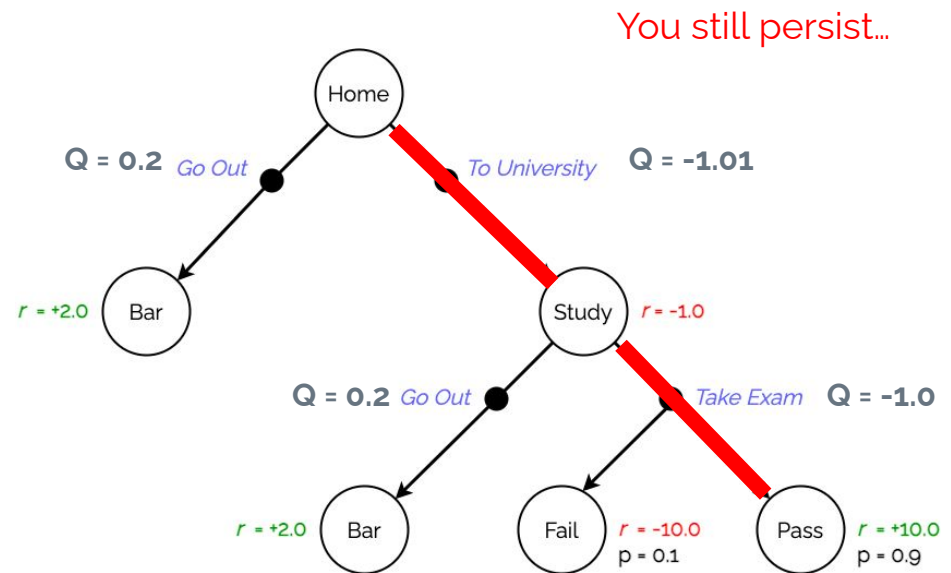


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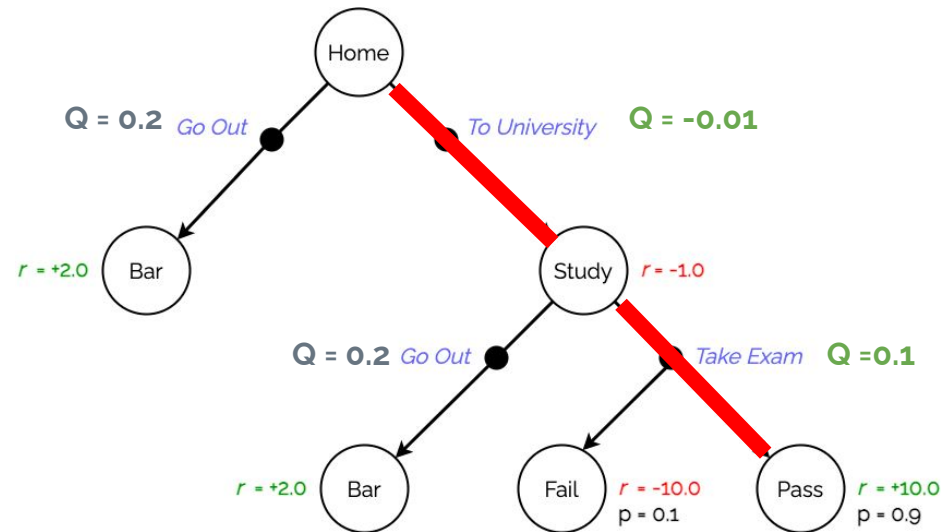


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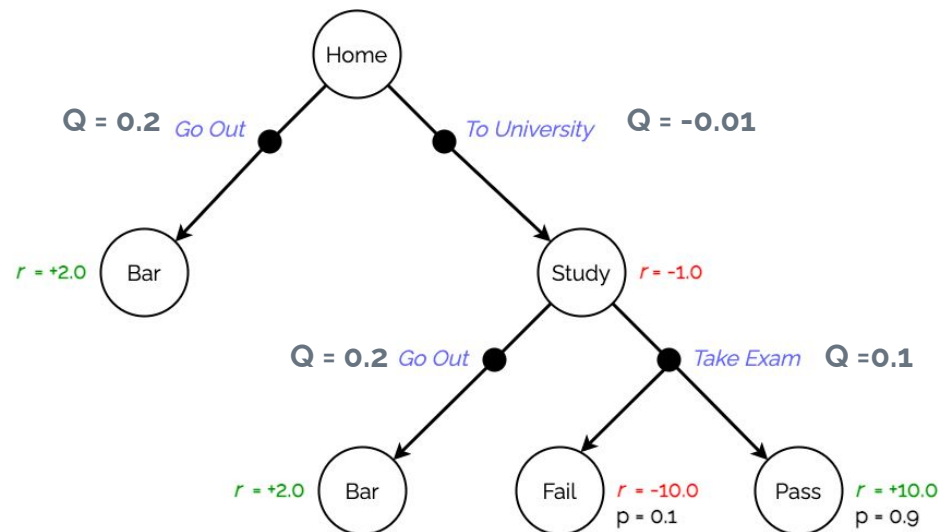


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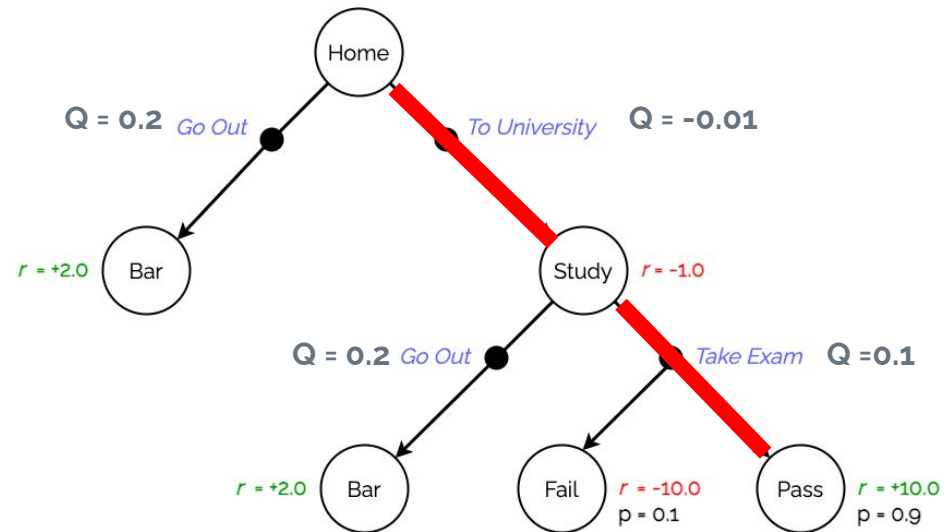


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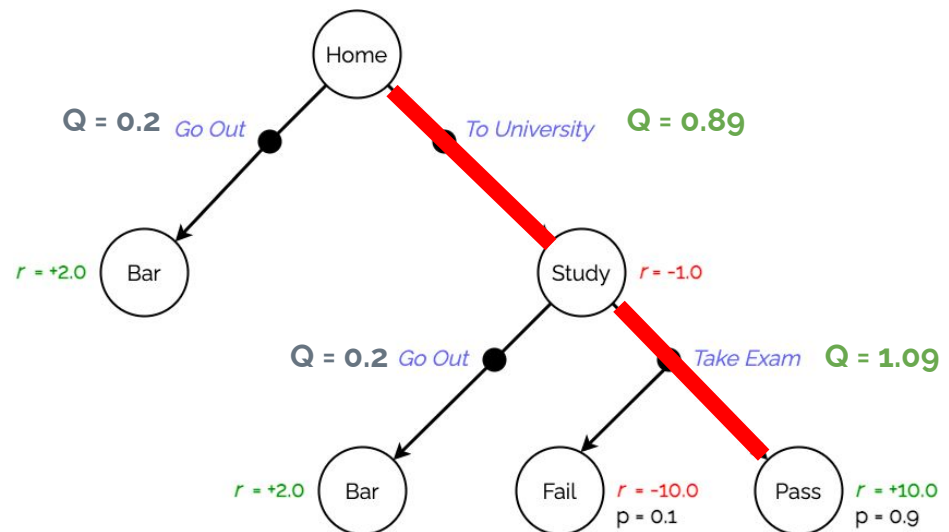


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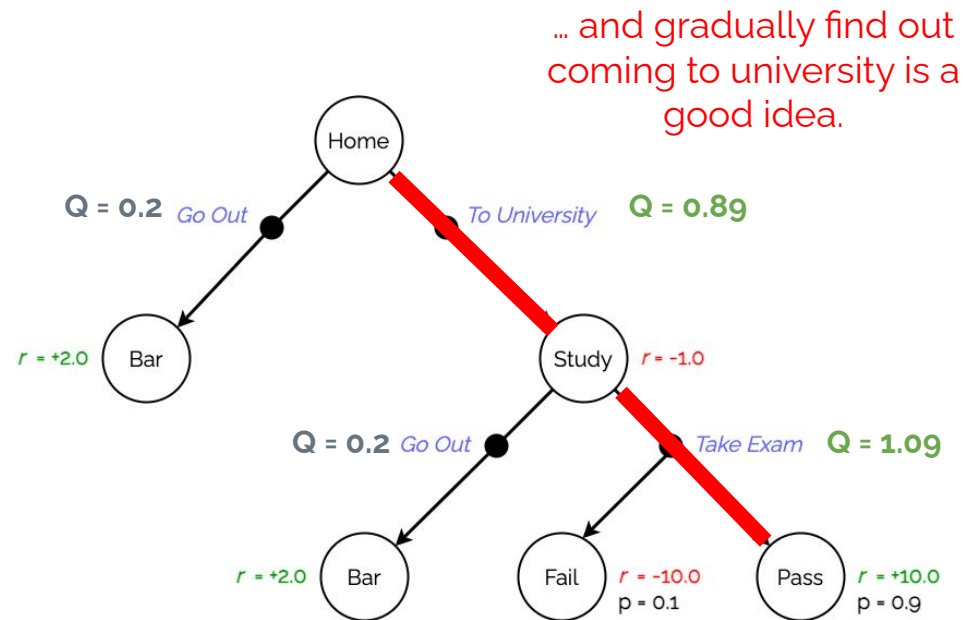


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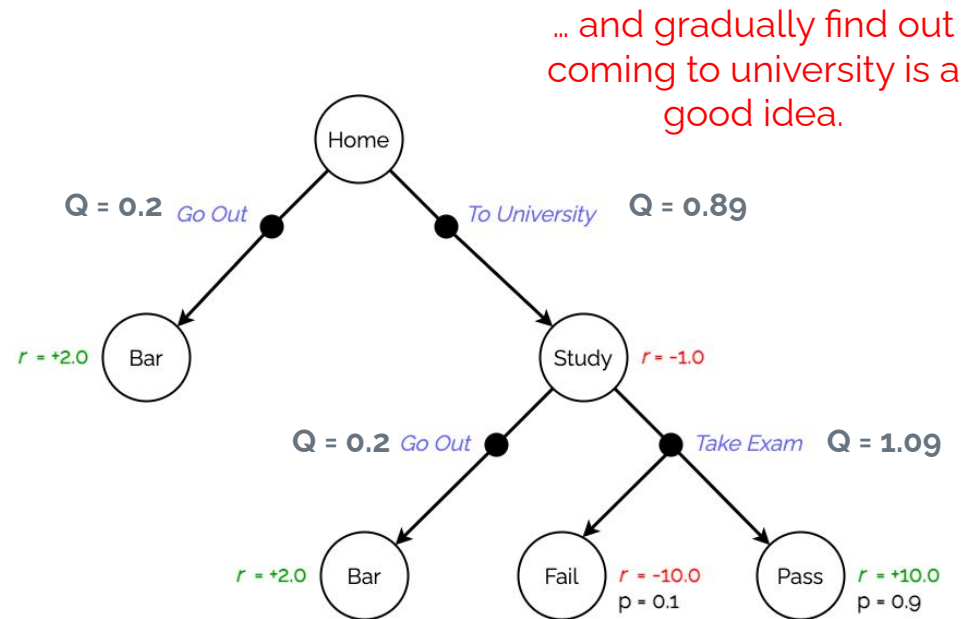
Exploration/Exploitation trade-off

We need **exploration** because actions may look worse than they are.

Reasons:

1. We need to collect our own data
2. Good action may seem bad if followed by bad actions
3. Environment can be stochastic

We also need **exploitation**.



Exploration/Exploitation trade-off

We need **exploration** because actions may look worse than they are.

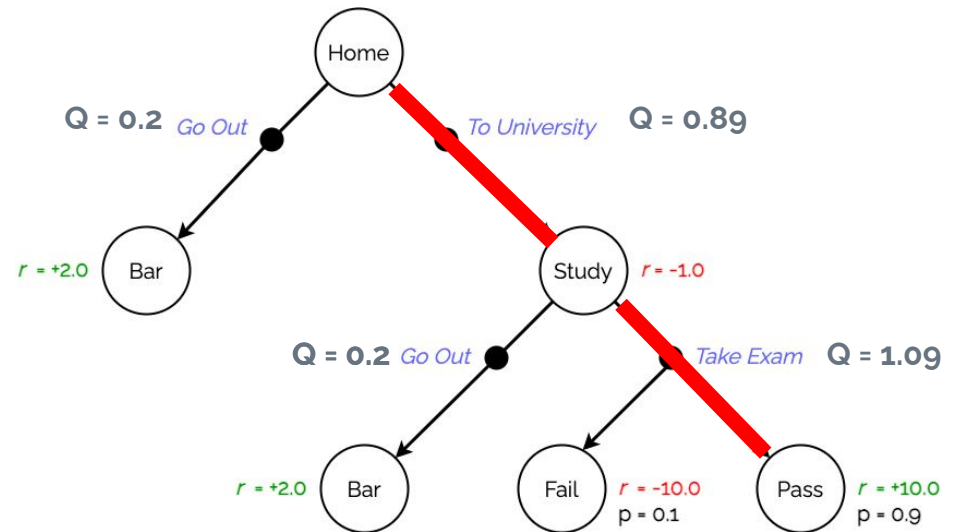
Reasons:

1. We need to collect our own data
2. Good action may seem bad if followed by bad actions
3. Environment can be stochastic

We also need **exploitation**.

Reasons:

1. Want to use what we learned
2. In bigger problems: move in promising directions to further explore.



Exploration/Exploitation strategies



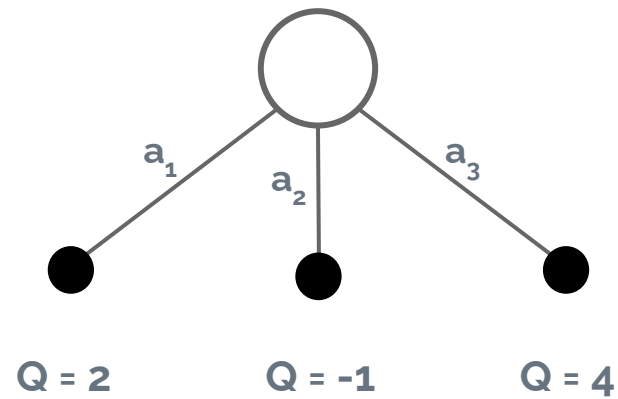
Exploration/Exploitation strategies

Huge amount of strategies, we will here discuss one (simple) example:

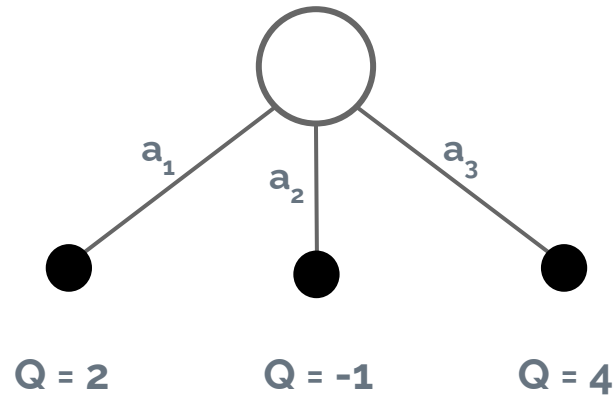
Boltzmann (softmax) exploration

Boltzmann (softmax) exploration

Boltzmann (softmax) exploration



Boltzmann (softmax) exploration



Intuition: give all actions a chance (exploration), but actions with higher Q-estimate deserve a higher probability (exploitation).

Boltzmann (softmax) exploration




Boltzmann (softmax) exploration

$$\pi(a_i|s) = \frac{e^{Q(s,a_i)/\tau}}{\sum_{a \in \mathcal{A}} e^{Q(s,a)/\tau}}$$

Boltzmann (softmax) exploration


To get the probability of
selecting action a_i in state s ...


$$\pi(a_i|s) = \frac{e^{Q(s,a_i)/\tau}}{\sum_{a \in \mathcal{A}} e^{Q(s,a)/\tau}}$$

Boltzmann (softmax) exploration

To get the probability of
selecting action a_i in state s ...

... we exponentiate its Q-value...


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Boltzmann (softmax) exploration

To get the probability of selecting action a_i in state s ...

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$$\pi(a_i|s) = \frac{e^{Q(s,a_i)/\tau}}{\sum_{a \in \mathcal{A}} e^{Q(s,a)/\tau}}$$

... and normalize over the sum of exponentiated Q-values of all actions (to make it a valid probability distribution).

Boltzmann (softmax) exploration

To get the probability of selecting action a_i in state s ...

... we exponentiate its Q-value...

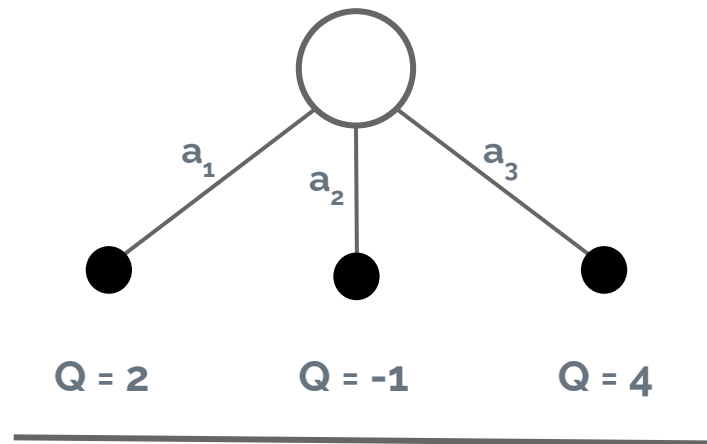
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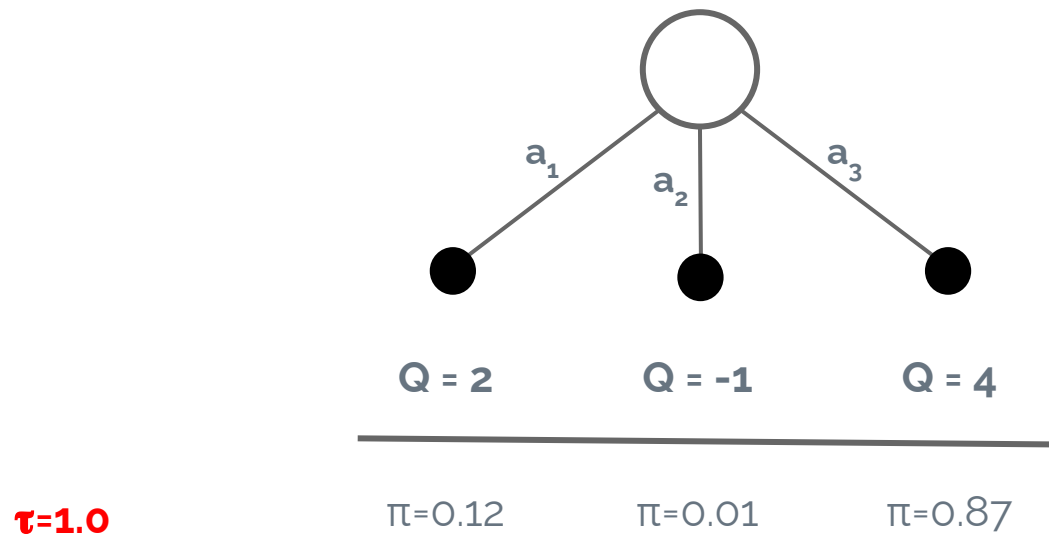
Temperature τ scales the amount of exploration:

$\tau \rightarrow 0$: one-hot (exploit)
 $\tau \rightarrow \infty$: uniform (explore)

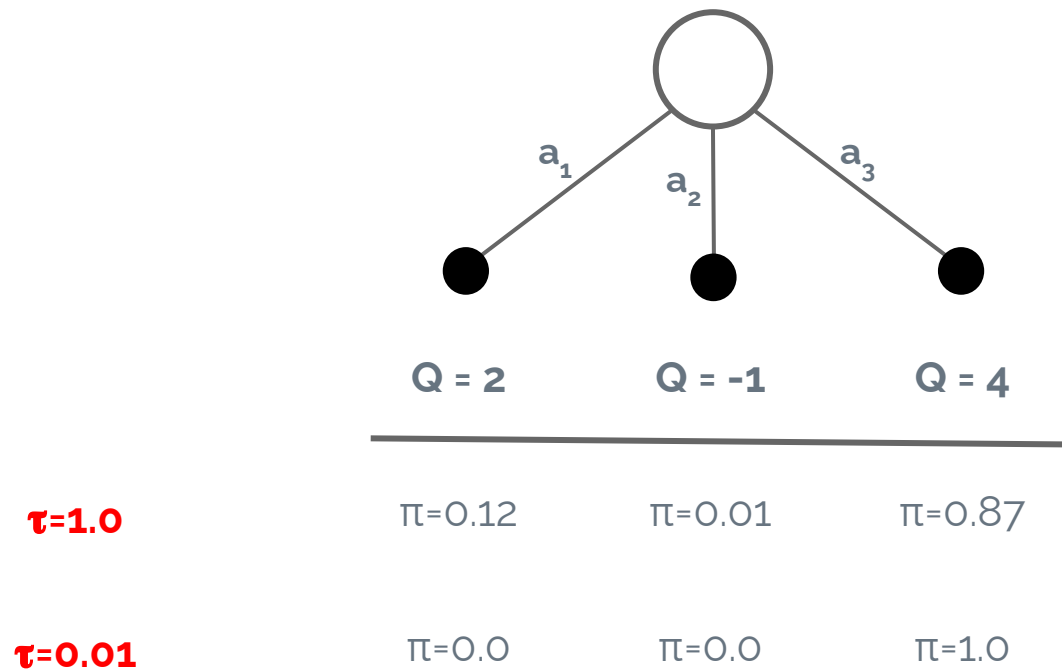
Boltzmann (softmax) exploration



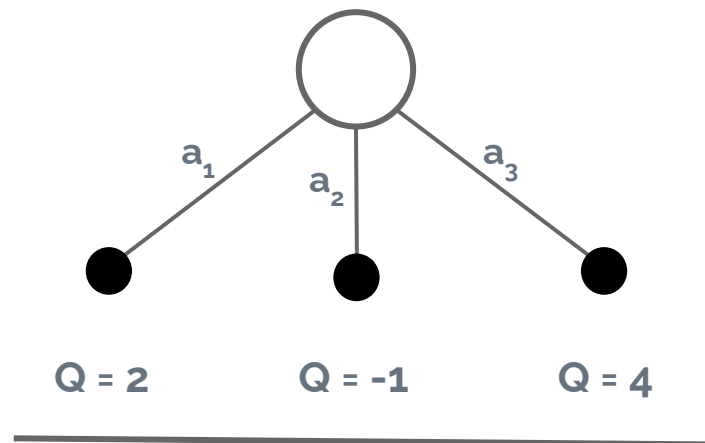
Boltzmann (softmax) exploration



Boltzmann (softmax) exploration



Boltzmann (softmax) exploration



$\tau=1.0$

$\pi=0.12$

$\pi=0.01$

$\pi=0.87$

$\tau=0.01$

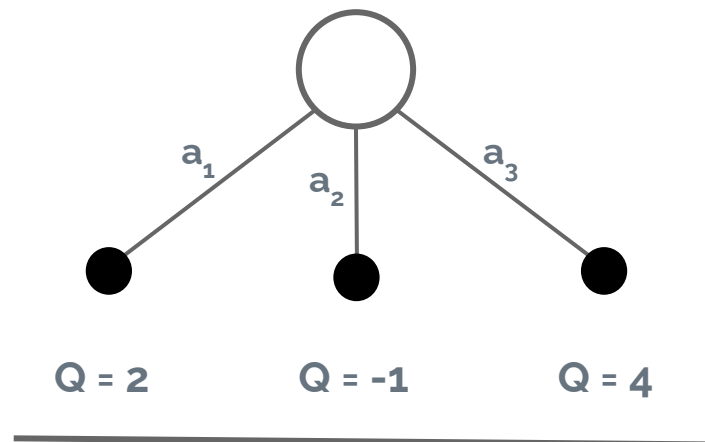
$\pi=0.0$

$\pi=0.0$

$\pi=1.0$

full exploitation

Boltzmann (softmax) exploration



$\tau=1.0$

$\pi=0.12$

$\pi=0.01$

$\pi=0.87$

$\tau=0.01$

$\pi=0.0$

$\pi=0.0$

$\pi=1.0$

full exploitation

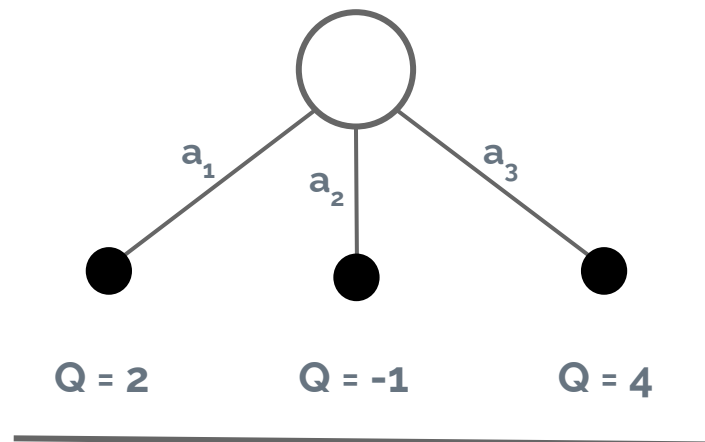
$\tau=100$

$\pi=0.33$

$\pi=0.32$

$\pi=0.34$

Boltzmann (softmax) exploration



$\tau=1.0$

$\pi=0.12$

$\pi=0.01$

$\pi=0.87$

$\tau=0.01$

$\pi=0.0$

$\pi=0.0$

$\pi=1.0$

full exploitation

$\tau=100$

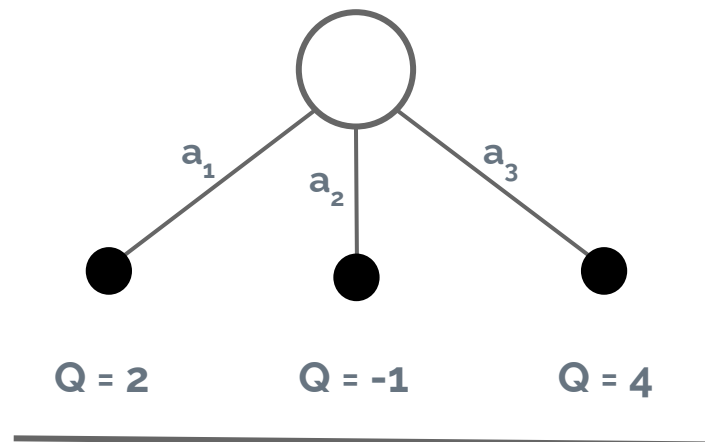
$\pi=0.33$

$\pi=0.32$

$\pi=0.34$

full exploration

Boltzmann (softmax) exploration



Can anneal τ during training to gradually transition from exploration to exploitation

$\tau=1.0$

$\pi=0.12$

$\pi=0.01$

$\pi=0.87$

$\tau=0.01$

$\pi=0.0$

$\pi=0.0$

$\pi=1.0$

full exploitation

$\tau=100$

$\pi=0.33$

$\pi=0.32$

$\pi=0.34$

full exploration

Exploration

(video)

The Reinforcement Learning Cycle

Pseudocode

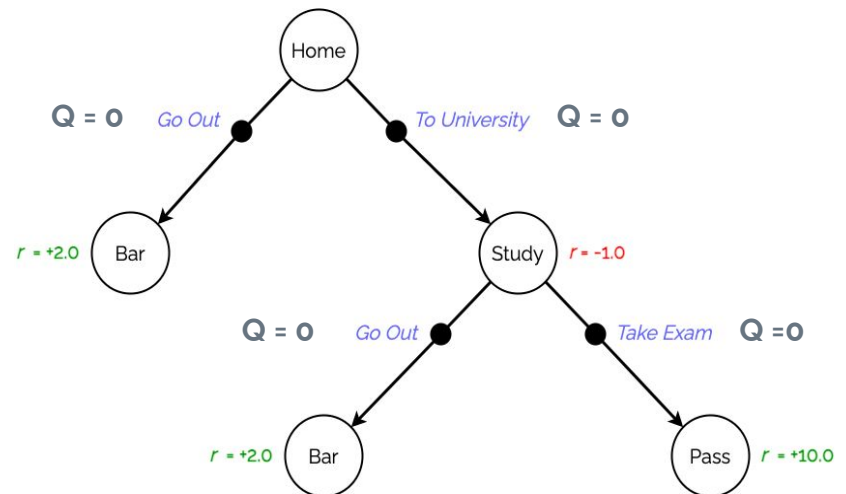
Initialize $Q(s,a)$ estimates for all states,actions
(e.g. to 0)

Repeat:

1) Exploration:

2) Credit assignment:

3) Update:



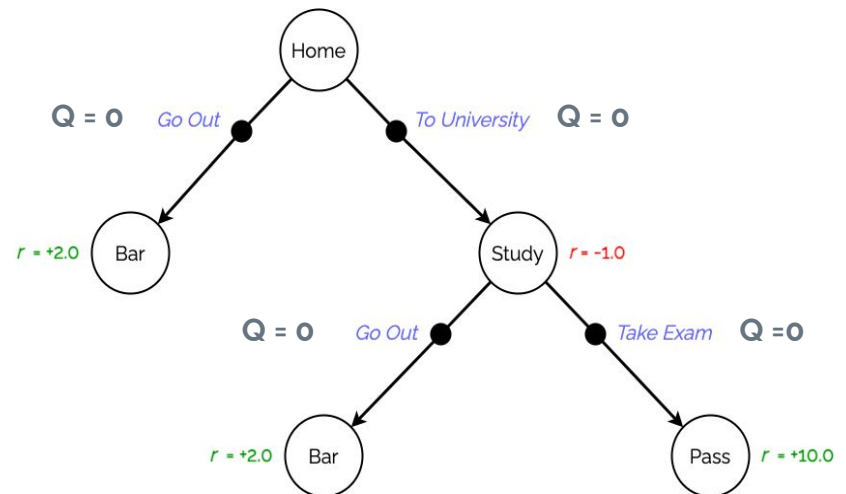
The Reinforcement Learning Cycle

Pseudocode

Initialize $Q(s,a)$ estimates for all states,actions
(e.g. to 0)

Repeat:

- 1) Exploration: Boltzmann policy with annealing temperature.
- 2) Credit assignment:
- 3) Update:



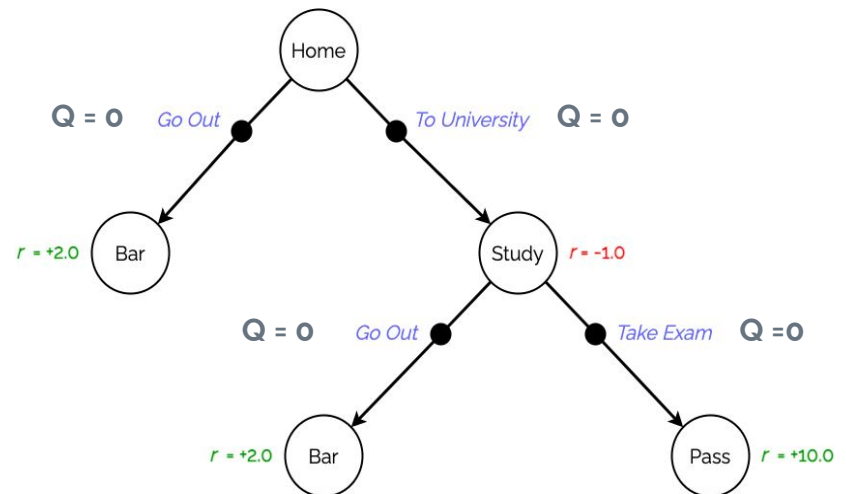
The Reinforcement Learning Cycle

Pseudocode

Initialize $Q(s,a)$ estimates for all states,actions (e.g. to 0)

Repeat:

- 1) Exploration: Boltzmann policy with annealing temperature.
- 2) Credit assignment: Monte Carlo back-up.
- 3) Update:



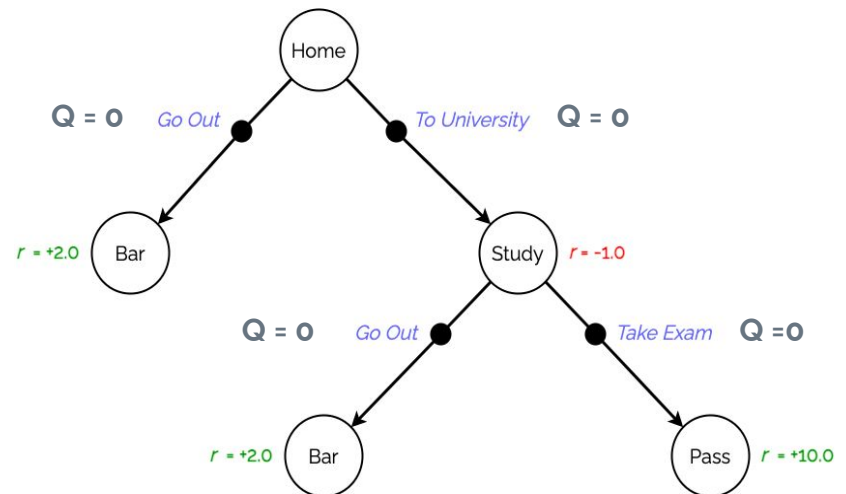
The Reinforcement Learning Cycle

Pseudocode

Initialize $Q(s,a)$ estimates for all states,actions
(e.g. to 0)

Repeat:

- 1) Exploration: Boltzmann policy with annealing temperature.
- 2) Credit assignment: Monte Carlo back-up.
- 3) Update: Tabular learning rule with learning rate 0.1



Part IV

Deep reinforcement learning

Deep reinforcement learning

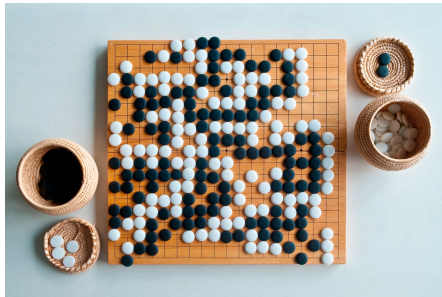


Deep reinforcement learning

Deep reinforcement learning = deep learning + reinforcement learning

Deep reinforcement learning

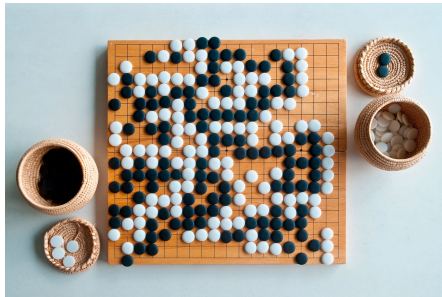
Deep reinforcement learning = deep learning + reinforcement learning



Observation spaces in reinforcement are usually high-dimensional

Deep reinforcement learning

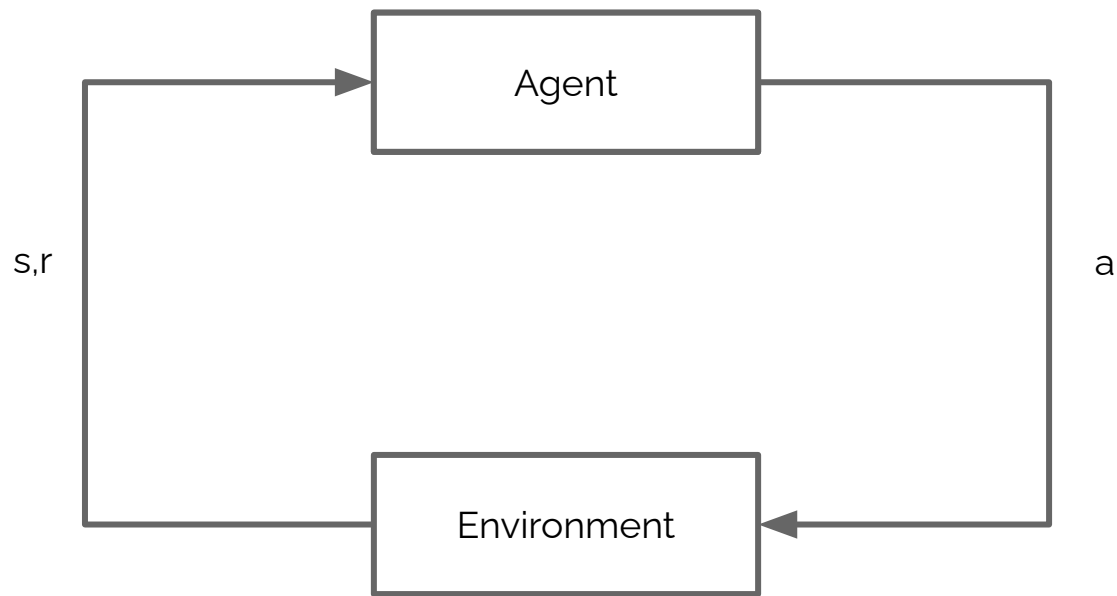
Deep reinforcement learning = deep learning + reinforcement learning



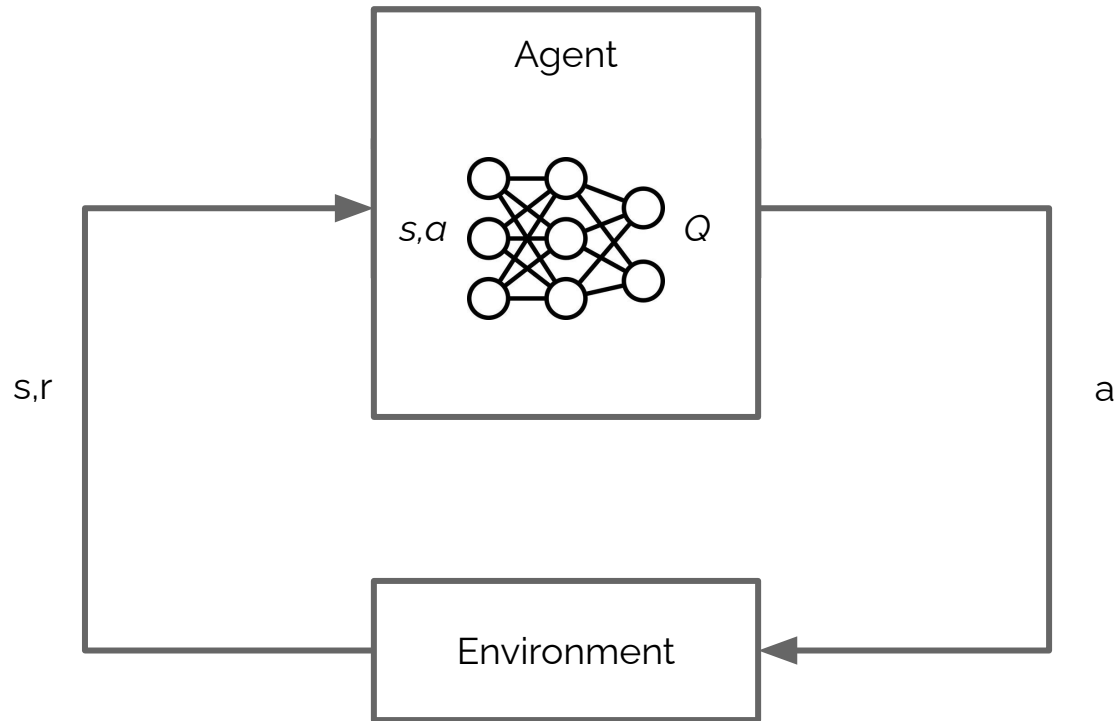
Observation spaces in reinforcement are usually high-dimensional

We need to use *function approximation*, e.g., deep learning, to store our solution
(to fit it in memory & profit from generalization)

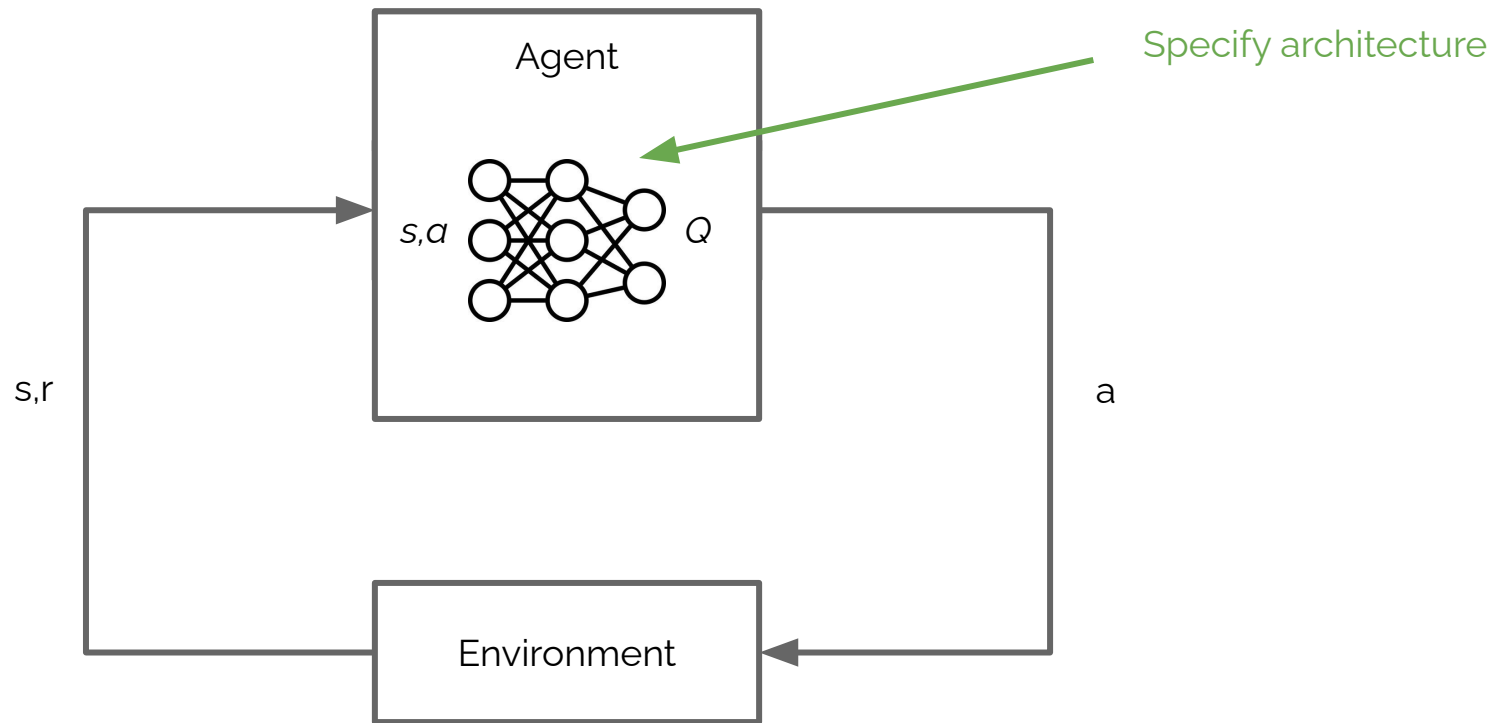
Deep Reinforcement Learning



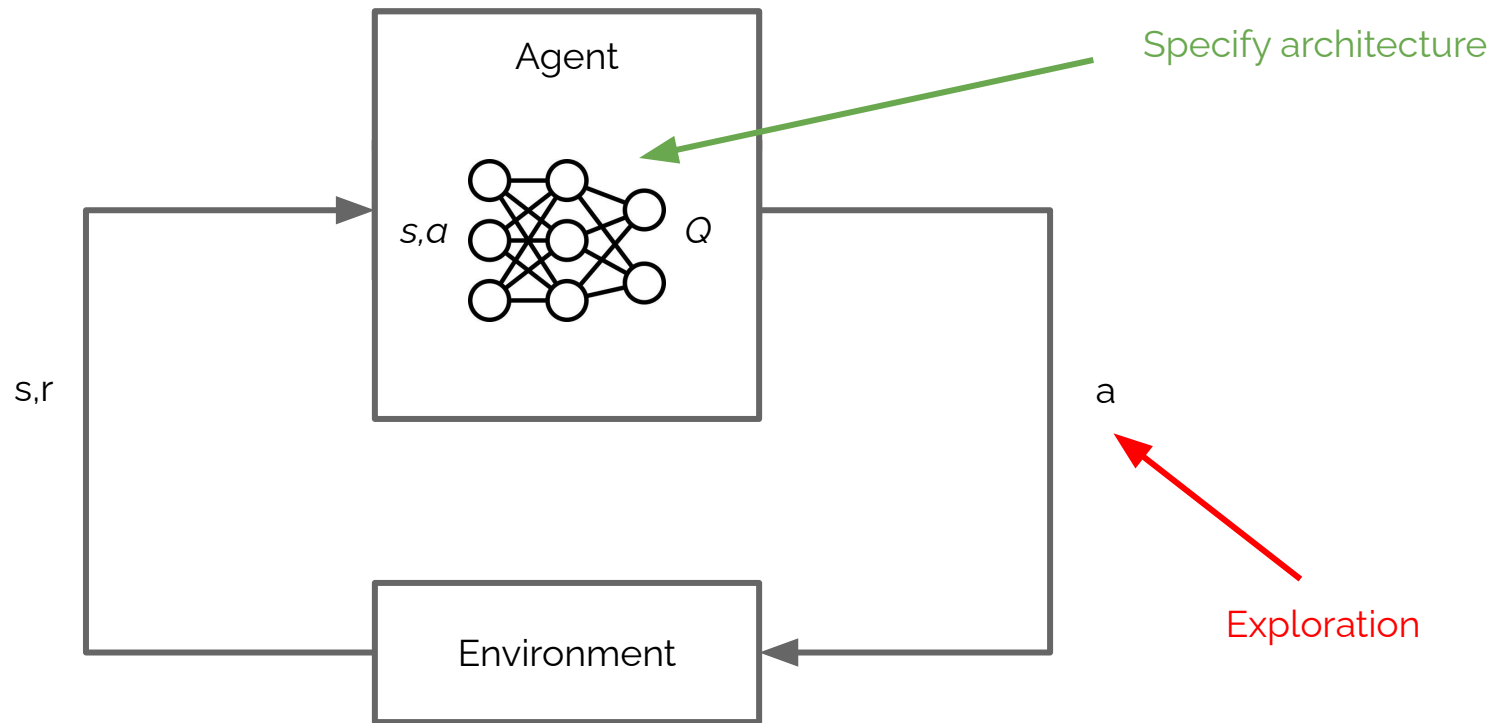
Deep Reinforcement Learning



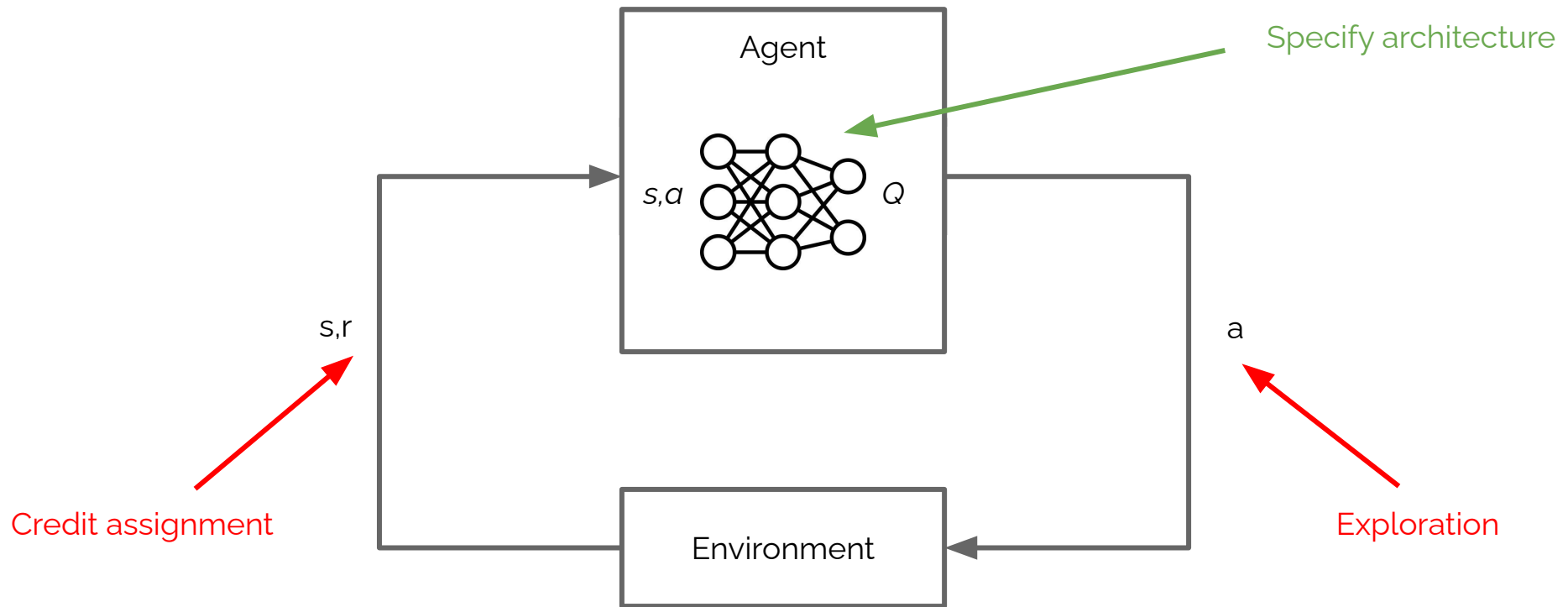
Deep Reinforcement Learning



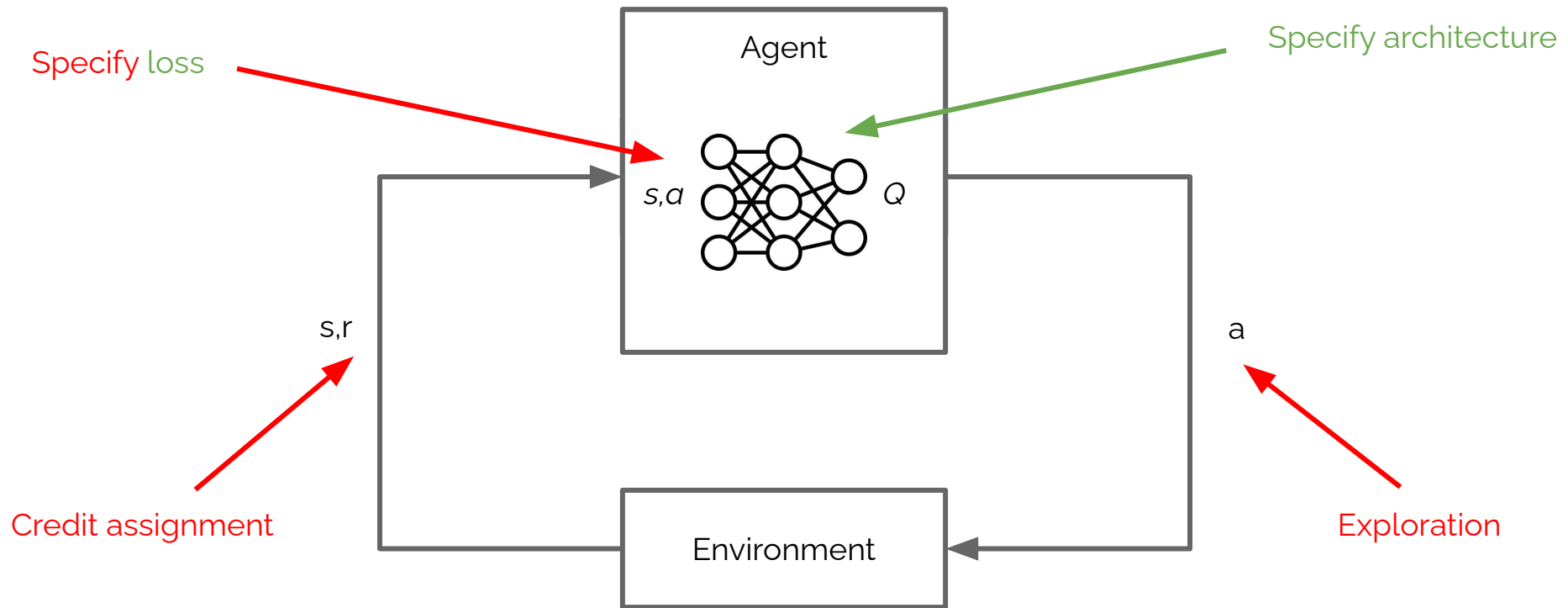
Deep Reinforcement Learning



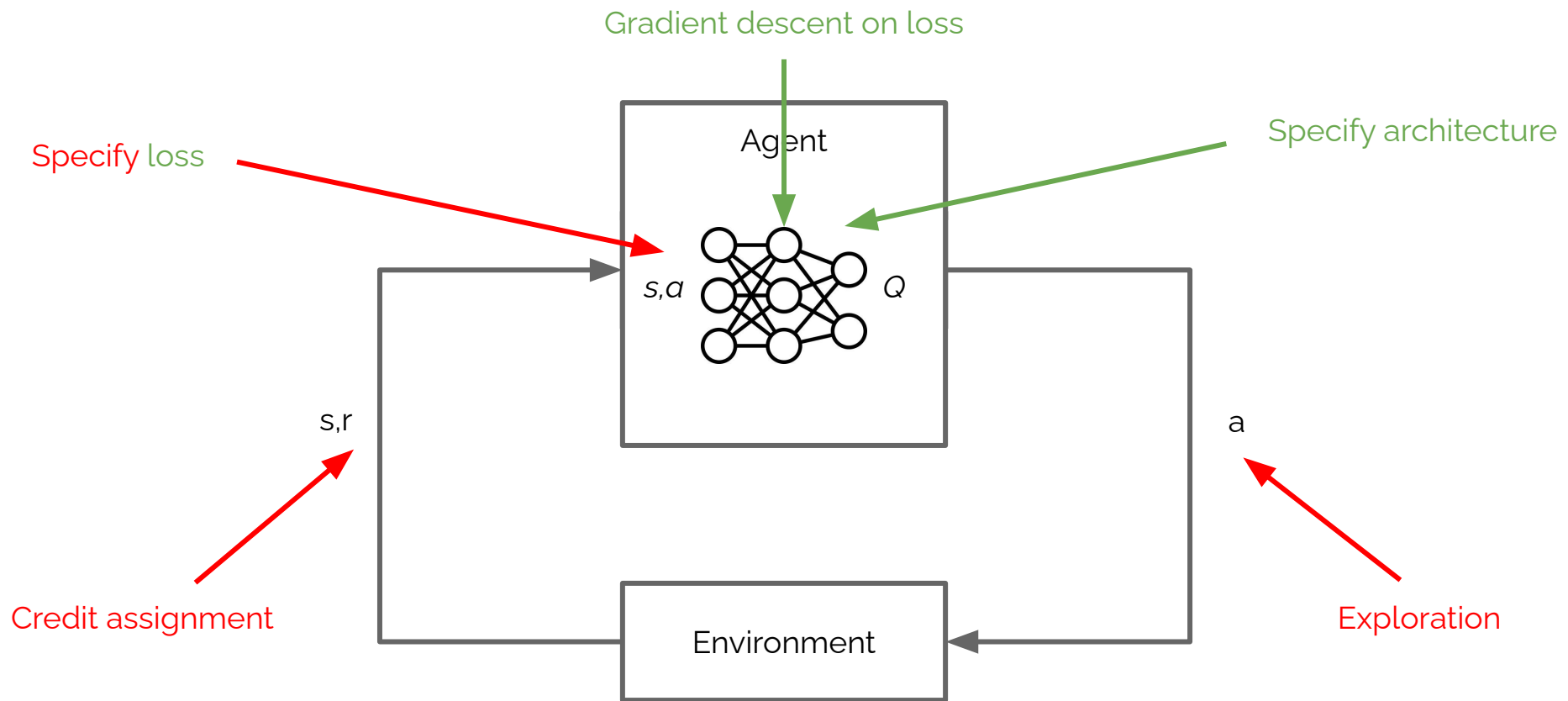
Deep Reinforcement Learning



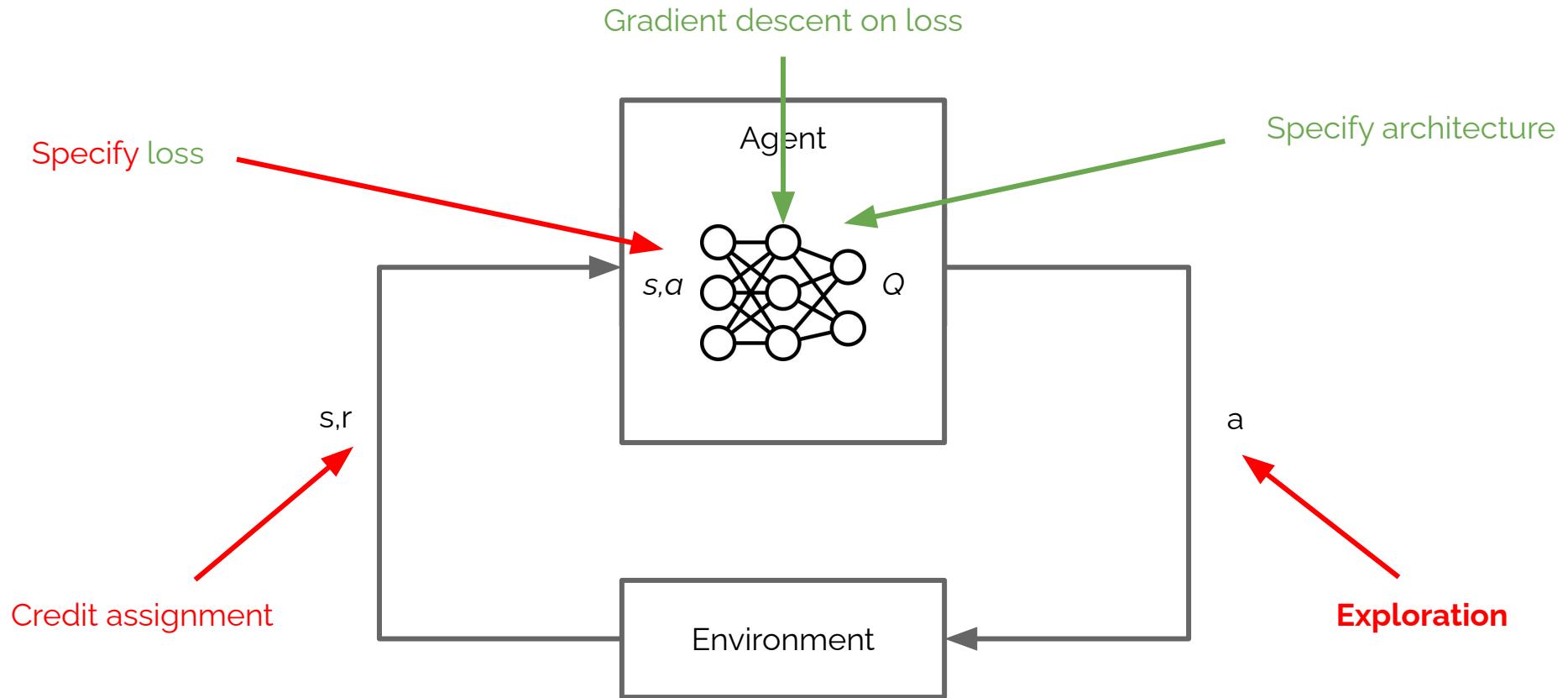
Deep Reinforcement Learning



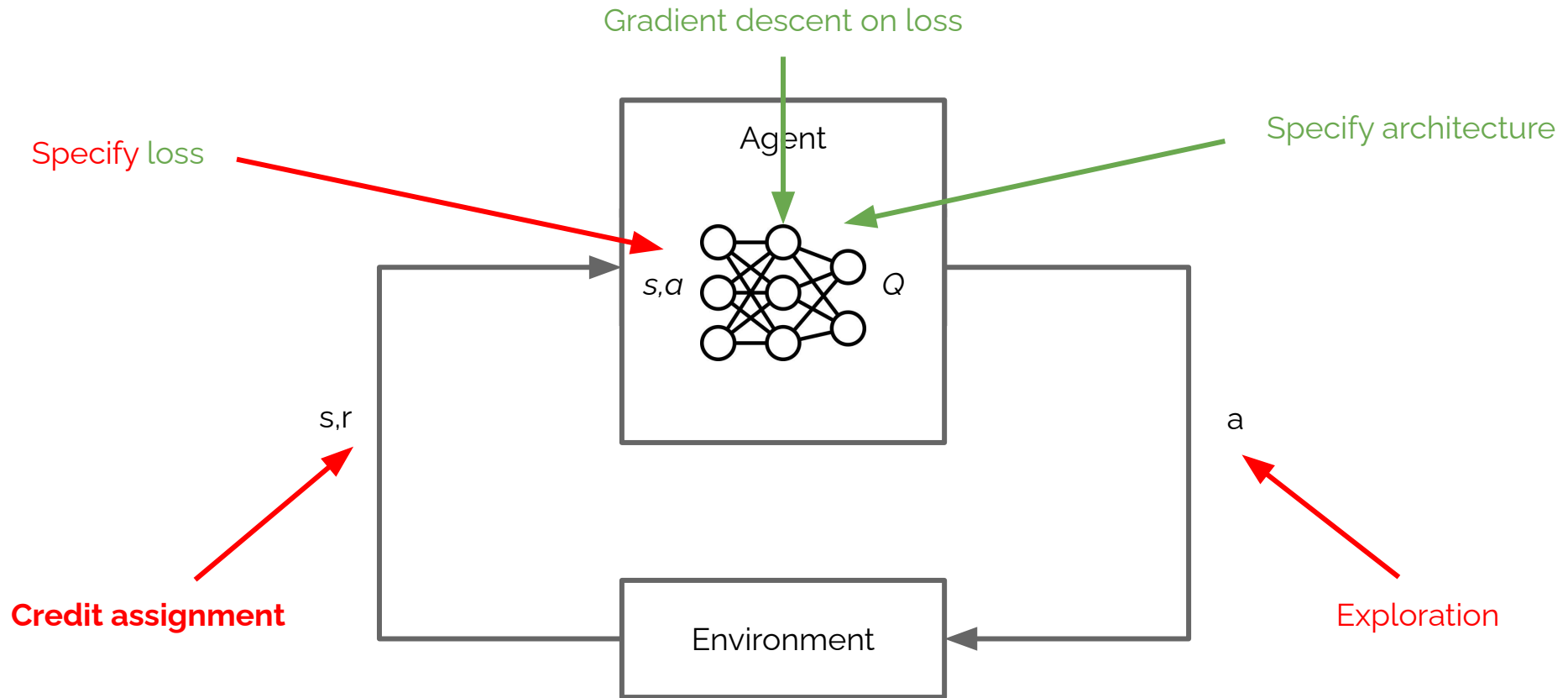
Deep Reinforcement Learning



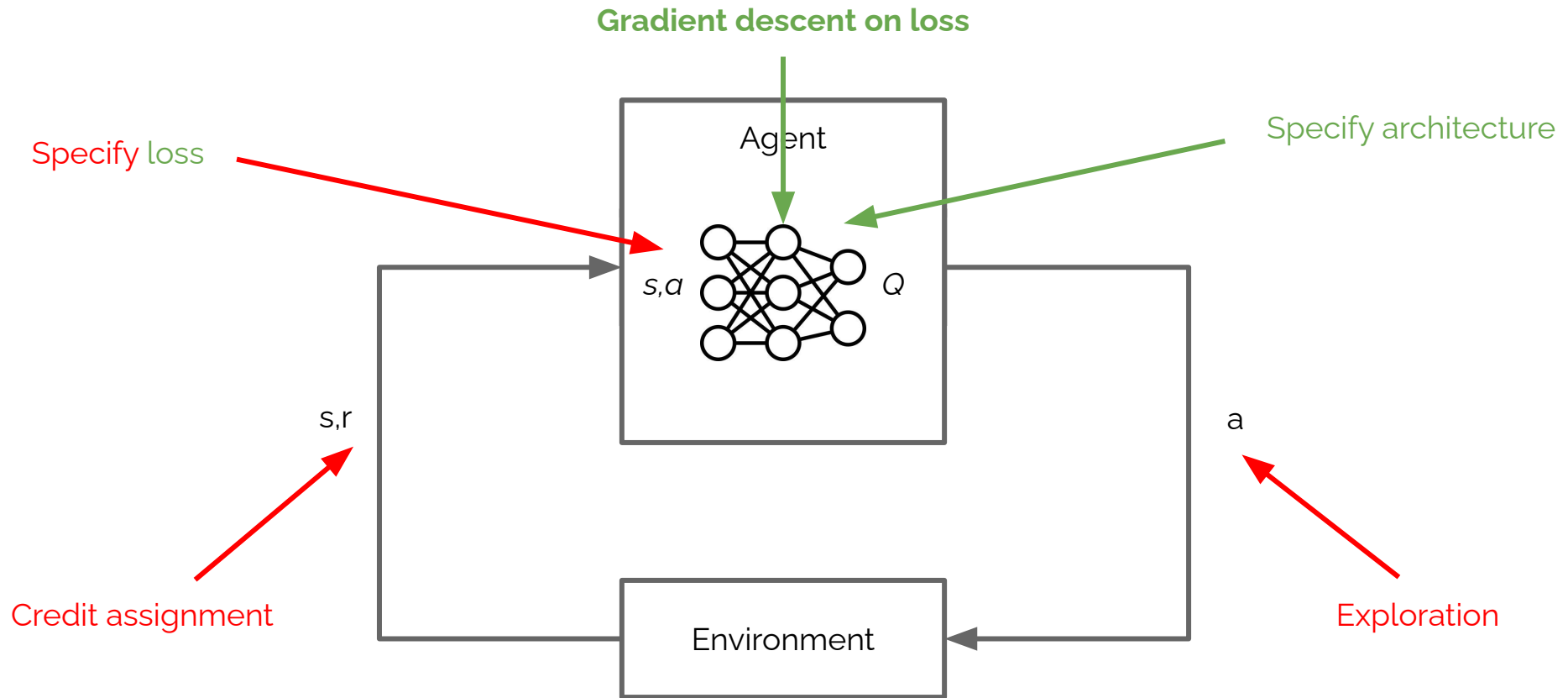
Deep Reinforcement Learning



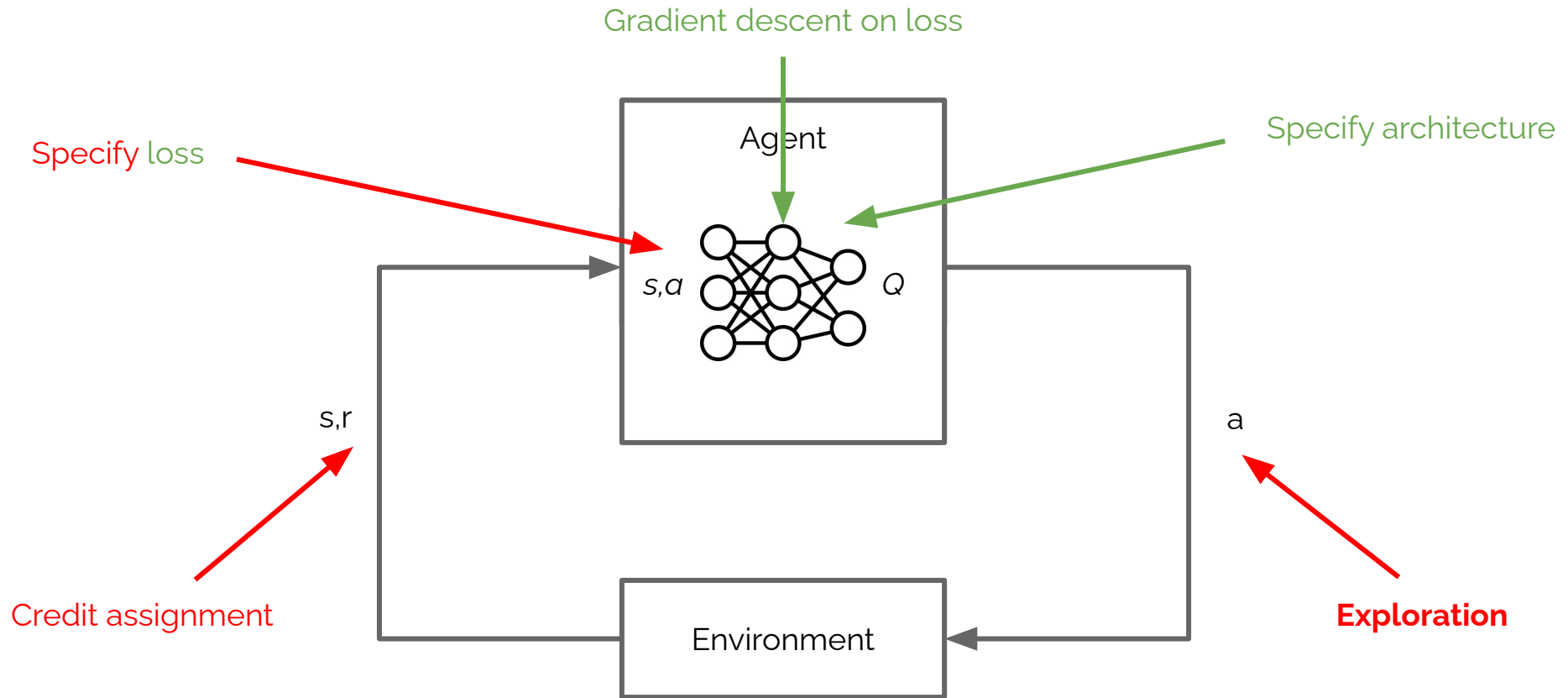
Deep Reinforcement Learning



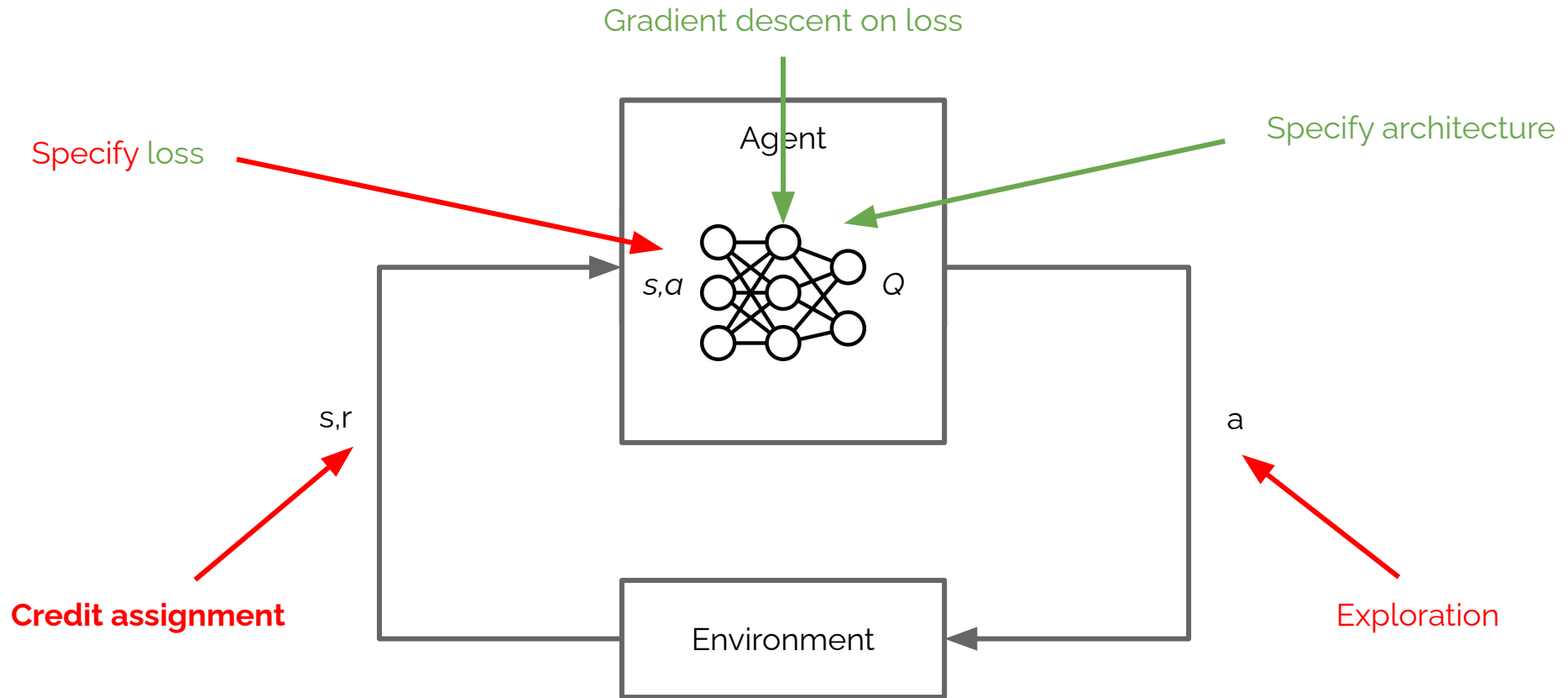
Deep Reinforcement Learning



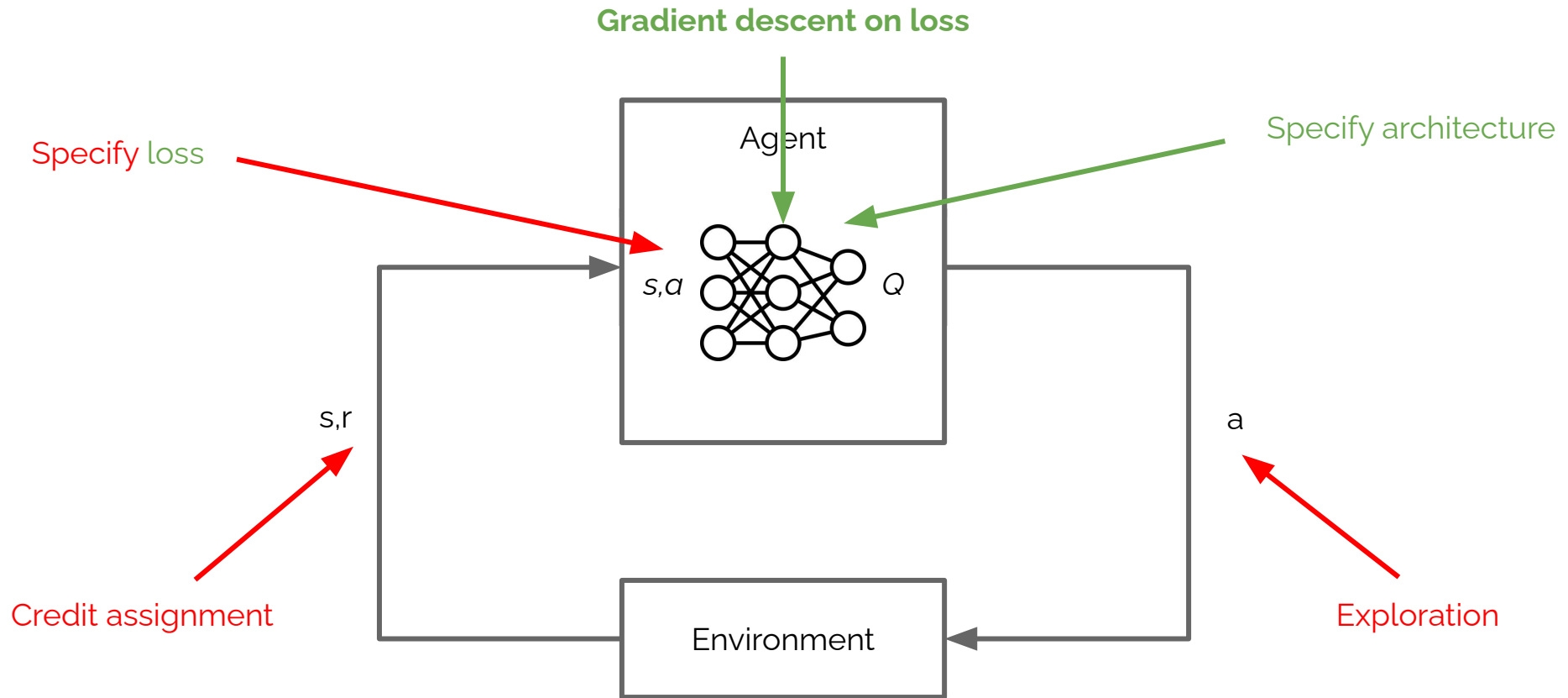
Deep Reinforcement Learning



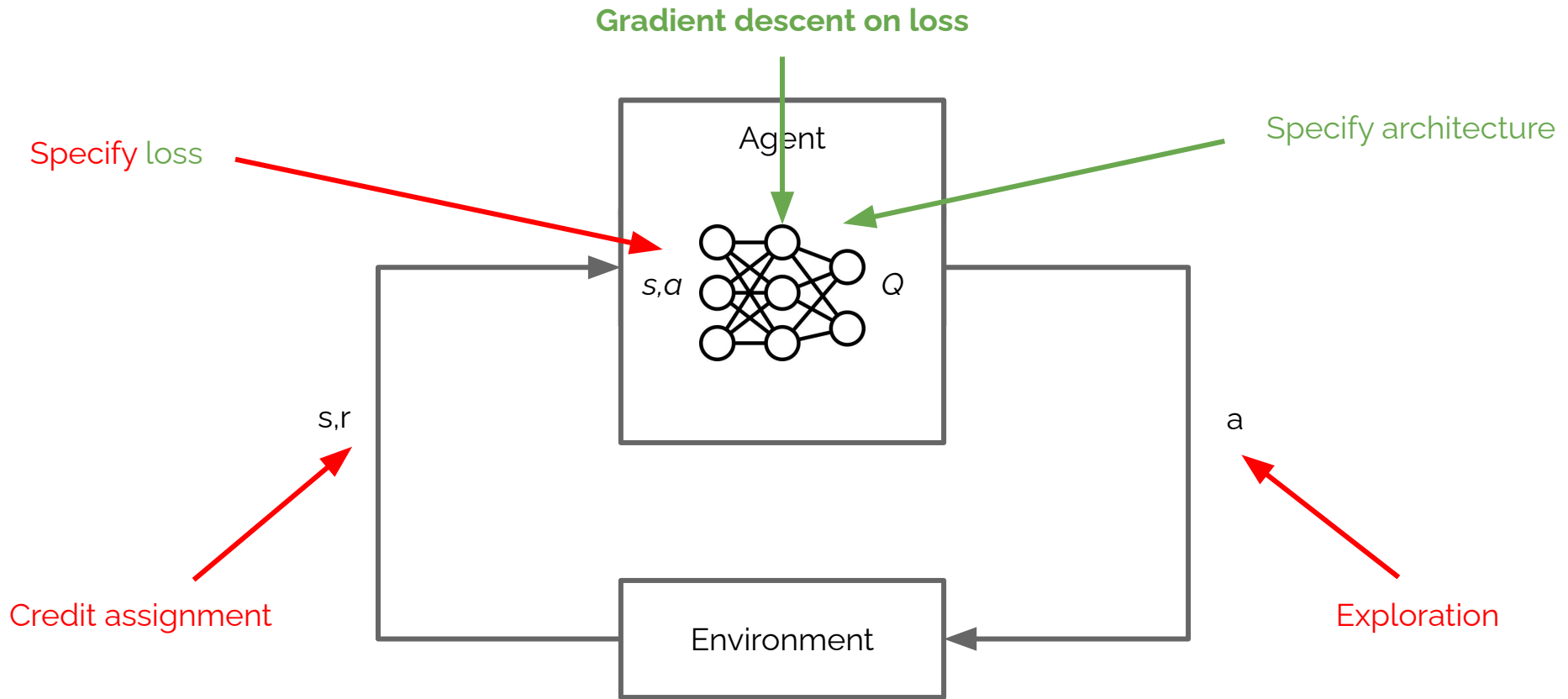
Deep Reinforcement Learning



Deep Reinforcement Learning

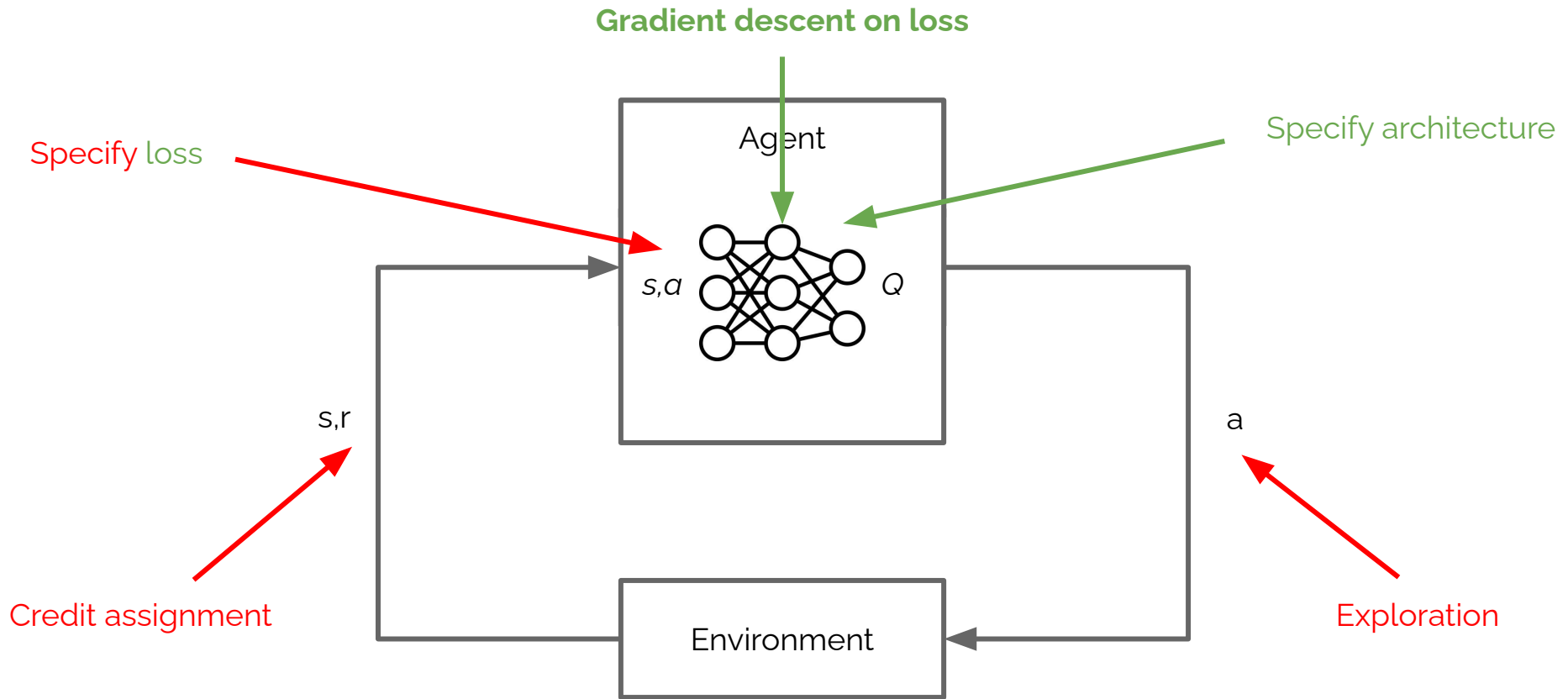


Deep Reinforcement Learning



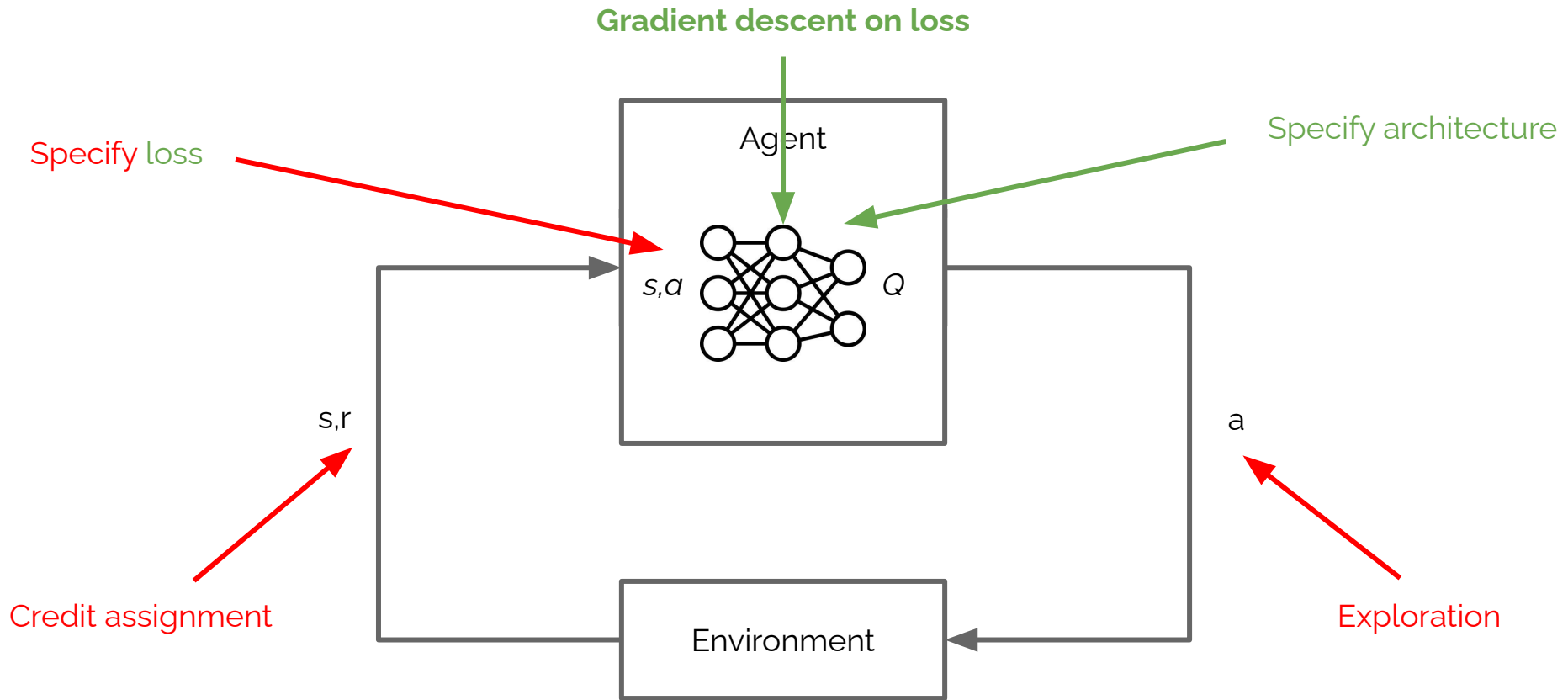
RL is supervised learning

Deep Reinforcement Learning



RL is supervised learning on a moving target function

Deep Reinforcement Learning



RL is supervised learning on a moving target function that influences which data you see.

Conclusion

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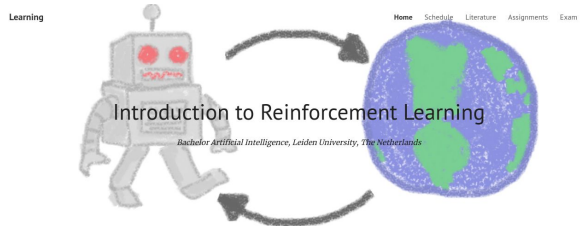
Conclusion

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Courses



Courses

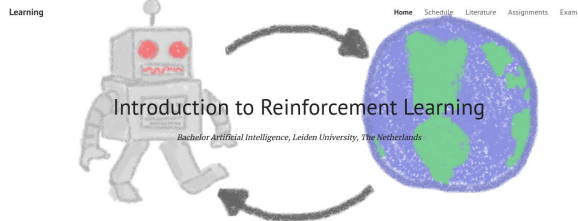


Welcome to the course "Introduction to Reinforcement Learning", which will run in the spring of 2023. The course consists of 14 weeks, in which you hand in 4 assignments, and make a final exam.

Teachers: [Dan Fei](#), [Thomas Moreland](#), [Johel Pinat](#), Serban Vadineanu, Koen Ponsse.

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Courses



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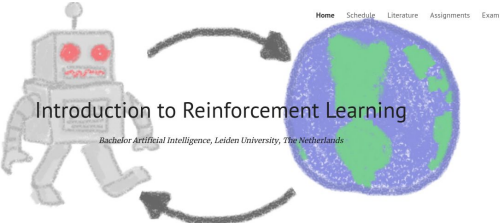
Welcome to the webpage of the master course "Reinforcement Learning" taught at Leiden University

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Courses

Learning



Introduction to Reinforcement Learning


Reinforcement Artificial Intelligence, Leiden University, The Netherlands

Home Schedule Literature Assignments Exam

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Reinforcement Learning


Master Computer Science, Leiden University, The Netherlands

Home Schedule Literature Assignments Exam

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Seminar Advanced Deep Reinforcement Learning

Master Computer Science, Leiden University, The Netherlands

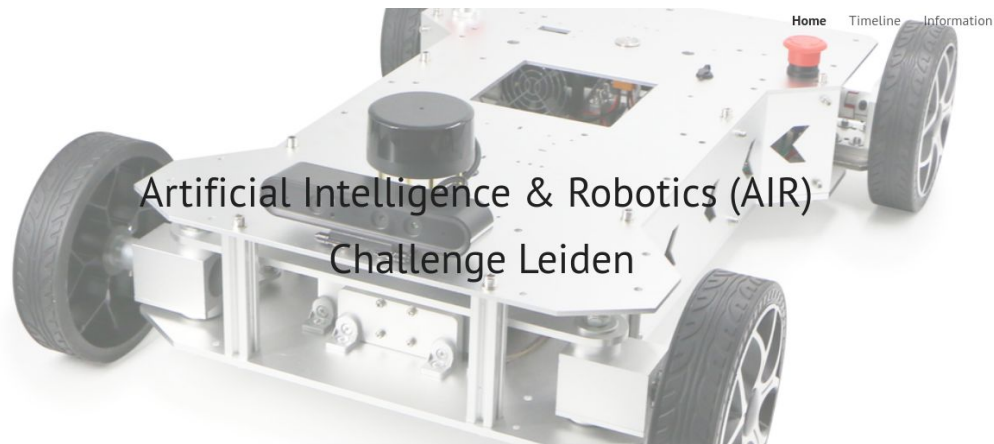
Home Course Schedule Groups 1: Theory 2: Papers 3: Presentations

General information

- The Seminar Advanced Deep Reinforcement Learning (SADRL) is a master level course taught at Leiden University.

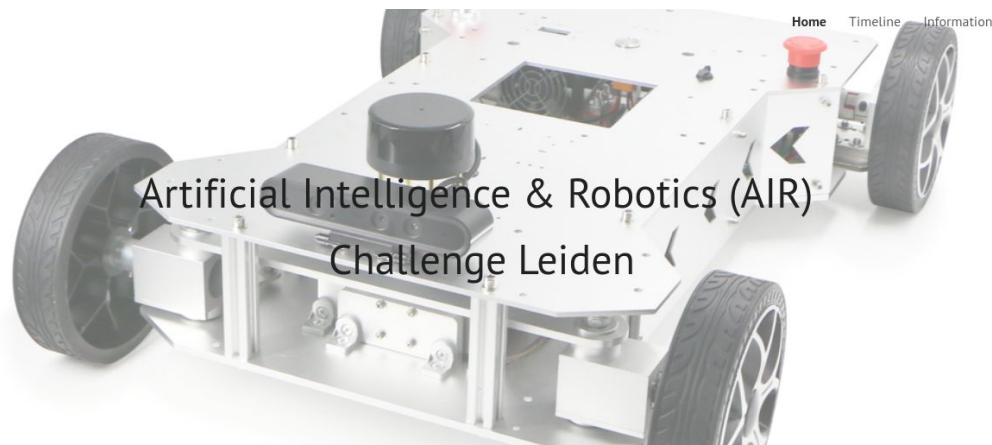
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AI & Robotics challenge



The AI & Robotics Challenge is a yearly bachelor student competition that runs within the [Leiden Institute of Advanced Computer Science \(LIACS\)](#).

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Extra-curricular course (2 ECTS)

Sign-up in September 2023

Questions?